



# Soil water thermodynamic to unify water retention curve by pressure plates and tensiometer

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The pressure plate method is a standard method for measuring the pF curves, also called soil water retention curves, in a large soil moisture range from saturation to a dry state corresponding to an applied pressure of near 1500 kPa. However, the pressure plate can only provide discrete water retention curves represented by a dozen measured points. In contrast, the measurement of the soil water retention curves by tensiometer is direct and continuous, but limited to the range of the tensiometer reading: from saturation to near 70–80 kPa. The two methods stem from two very different concepts of measurement and the compatibility of both methods has never been demonstrated. The recently established thermodynamic formulation of the pedostructure water retention curve, will allow the compatibility of the two curves to be studied, both theoretically and experimentally. This constitutes the object of the present article. We found that the pressure plate method provides accurate measurement points of the pedostructure water retention curve  $h(W)$ , conceptually the same as that accurately measured by the tensiometer. However, contrarily to what is usually thought,  $h$  is not equal to the applied air pressure on the sample, but rather, is proportional to its logarithm, in agreement with the thermodynamic theory developed in the article. The pF curve and soil water retention curve, as well as their methods of measurement are unified in a same physical theory. It is the theory of the soil medium organization (pedostructure) and its interaction with water. We show also how the hydrostructural parameters of the theoretical curve equation can be estimated from any measured pF curve, whatever the method of measurement. An application example using published pF curves is given.

**Keywords:** pressure plate apparatus, tensiometric measurement, soil moisture characteristic curve, soil water retention curve, pF curves, matric potential, pedostructure, hydrostructural parameters

## INTRODUCTION

There are numerous parametric equations for simulating the soil water retention curve, representing the relationship between the water content and the matric suction of a soil medium. This is usually expressed as a plot of volumetric water content ( $m^3/m^3$ ) vs. suction (kPa) (Leong and Rahardjo, 1997). The proposed equations are empirical or semi-empirical (El-kadi, 1985; Leij et al., 1997), but are of great importance in soil water modeling where a retention function is needed to simulate water transport in the soil medium using the Richards' equation (Tietje and Tapkenhinrichs, 1993). Today, the most commonly used equations are those of van Genuchten (1980), Campbell (1974) and Brooks and Corey (1964), not an exhaustive list, which shows only that the exact physical equation, if it exists, is not known. Moreover, several names and units were given to the retention energy (matric potential, soil water tension, soil water suction, soil water retention, pressure head, and water potential) depending on the point of view of the scientific discipline using

this important state variable in its physical models or experiments. It is generally known that the soil water retention phenomenon (water held in soil by retention forces) is related to the water potential in the soil matric—but how, exactly? How do we define the water potential in a natural medium (biological cell, soil medium) whose water content is changing? To answer such questions, we have to go back to the water thermodynamics in the natural medium.

According to “A Dictionary of Biology” (2004), the definition of the water potential in biological sciences is the following: “Symbol  $\psi$ . The difference between the chemical potential of the water  $\mu_w$  in a biological system and the chemical potential of pure water at the same temperature and pressure,  $\mu_w^0$ . . . . In soils and other extracellular systems, another factor, called matric potential, can contribute significantly to water potential.” This matric potential symbolized by “ $\psi_m$ ” is a component of water potential due to the adhesion of water molecules to non-dissolved structures of the system, i.e., the matrix, such as plasma membranes or

soil particles. It is always negative and it is significant only outside living cells in relatively dry systems, for example soils, where much of the water is tightly bound to soil particles.”

The definition of the *water potential* in soil water thermodynamics is almost the same: “In the soil physics literature, the chemical potential of soil water,  $\mu_w$ , when referenced against the value of  $\mu_w^0$ , is called the water potential and is given the symbol  $\psi_w$ ” (Sposito, 1981, p. 193). The difference between both definitions of water potential lies in the definition of  $\mu_w^0$ , which is the chemical potential of pure water at standard temperature (25°C) and pressure (1 atm).

As for the matric potential  $\psi_m$ , it is defined by Sposito (1981, p. 197) as a component of  $\psi_w$  responding to the equation  $d\psi_m = (\partial\mu_w/\partial W)_{T,P,Pa}dW$  where  $W$  is the gravimetric water content ( $\text{kg}_{\text{water}}\text{kg}_{\text{solids}}^{-1}$ ). “This potential component represents the effect of the changes in the water content, an effect usually attributes to the presence of the solid portion of a soil-water system. This equation also includes the effect of dissolved solid components of the soil water system on  $\mu_w$ .” According to this definition, Braudeau et al. (2014) showed that the *matric potential* ( $\psi_m$ ), measured by the tensiometer on unconfined soil samples at constant  $T$  and  $P$ , is in fact equals the chemical potential of soil water  $\mu_w$ , when referenced against the value of  $\mu_{wsat}$ . This value represents the water chemical potential of the soil medium at saturation, such that:

$$\psi_m = (\mu_w - \mu_{wsat}) \quad (1)$$

For those authors, the matric potential governs the *local* water movement in the soil medium linked to a *local* variation in water content and is due to the thermodynamic interaction between the liquid phase of water and the surface charges of the clay particles. The arrangement of these particles with other soil particles (silt, sand) makes the aggregated structure of the soil medium, namely the pedostructure.

The matric potential ( $\psi_m$ ), as the soil water potential ( $\psi_w$ ) of which it is a component, is always  $\leq 0$  and is expressed in unit of specific energy: Joule per kg of water ( $\text{J kg}^{-1}$ ). “Quite often equivalent units are employed in place of the SI units. For example, the quotient  $\mu_w/M_w$ , where  $M_w$  is the mole weight of water, is called the ‘molar water potential’ (joules per mole); the product  $\rho_w^0\mu_w$  where  $\rho_w^0$  is the mass density of bulk liquid water, is called the ‘soil water pressure’ ( $\text{J m}^{-3} = \text{Nm}^{-2}$ ), and the quotient  $\mu_w/g$ , where  $g$  is the gravitational acceleration, is called the ‘soil water head’ ( $\text{J kg}^{-1} \text{m}^{-1} \text{s}^2 = \text{m}$ )” (Sposito, 1981, p. 194).

Agronomists and hydro-pedologists generally prefer to use units of pressure (Pa, positive) or of water head (m, negative) for the same notion of matric potential, using the symbol  $h$ . In this study,  $h$  will be expressed in terms of retention (or suction) pressure and will be the negative product of  $\psi_m$  and  $\rho_w^0$  in  $\text{kg}\text{w}\text{dm}^{-3}$ , such as:

$$h = -\rho_w^0\psi_m = -\rho_w^0(\mu_w - \mu_{wsat}) \quad (2)$$

$h$  is positive or null and expressed in kPa. The curve  $h(W)$  will be called the “soil water retention curve” or, more precisely, the “pedostructure water retention curve” after Braudeau et al. (2014)

who established its theoretical equation. Its thermodynamic formulation was established as a state equation depending on  $W$  (at  $T$  and  $P$  ambient and constant) and whose parameters are characteristics of the structural organization of the soil medium and its mineralogy. A methodology for measuring accurately these parameters was proposed based on the use of tensiometers (Assi et al., 2014). The advantage of having a unique thermodynamic formulation for the soil water retention curve, rather than a non-physically based equations (El-kadi, 1985; Leij et al., 1997), is that, despite the limited range of measurement of tensiometers (0–80 kPa), this range can be considered as sufficient to determine the parameters which are *theoretically* valuable for the entire curve or, at least, until the micro air entry point (Braudeau et al., 2014), i.e., largely beyond 80 kPa.

The problem stays in the method of measurement of these characteristic curves: the measurement of the soil water retention curves by tensiometer is direct and continuous but it is limited to the range of the tensiometer reading. In contrast, the curves obtained using the pressure plate method (Richards, 1948) are built by a dozen (or more) measured points but can cover a larger soil moisture range, from saturation to a water retention of near 1500 kPa. So, the two different methods are not covering the same range of soil moisture, nor do they have the same accuracy (Schelle et al., 2013). The junction between these ranges remains uncertain; moreover, inconsistent results were also noted comparing pressure plate with dew point method (Cresswell et al., 2008; Bittelli and Flury, 2009; Solone et al., 2012). In fact, not only is the accuracy of the pressure plate apparatus undefined, but its principle of measurement is also questionable as soon as soils are considered non-rigid (Sposito, 1981, p. 200).

The goal of this article is to integrate the soil water retention curve measured using the pressure plate apparatus into the unified theoretical framework proposed by Braudeau and Mohtar (2014) where, in particular, the physical equations of the hydrostructural functioning of the pedostructure are well established. This theoretical framework has to be used for interpreting the different methods of measurement of the soil water properties in order to compare the measured moisture characteristic curves with their theoretical equations. Thus, the pressure plate method (Richards, 1948) will be: (1) reconsidered from the thermodynamic point of view of this theoretical framework in order to theoretically formulate the water retention curve actually measured by this method; and (2) compared with the theoretical equation curve, accurately measured by the tensiometer.

## THEORY

### PHYSICAL EQUATION OF THE PEDOSTRUCTURE WATER RETENTION CURVE $h(W)$

Braudeau and Mohtar (2009) showed that any physical equation of the soil structure and soil water interactions cannot be found without changing the paradigm used for the soil medium characterization and modeling. This shift in paradigm must allow for considering the internal and multi scaled organization of the soil structure in the soil water physics. The concept of pedostructure (Braudeau et al., 2004) is at the basis of the new proposed paradigm. It represents and defines the first level of organization of the soil medium in a soil horizon, as an assembly of primary

ped. These peds are composed of a clayey mixture (S-matrix: Brewer, 1964) and act like saturated clay pastes at high water content.

The Structural Representative Elementary Volume (SREV) concept and the associated terminology for describing the pedostructure state variables (Table 1) were then applied to the thermodynamic theory of water in soil presented by Spósito (1981). The particularity of the SREV variables is that all extensive variables describing the different levels of organization of a given volume of soil structure (SREV) sampled (cut) in the soil medium is reported to the mass  $M_s$  of the structure contained in this volume. Therefore, the thermodynamic functions, which are all extensive variables (U, G, H), were rewritten according to the SREV concept and using the SREV variables, i.e., extensive variables reported to the structural mass  $M_s$  (Braudeau and Mohtar, 2009; Braudeau et al., 2014). Except for the water content, symbol  $W$  or  $w$ , the other SREV variables will be distinguished from the corresponding extensive variable by a single bar above the variable, like  $\bar{U}$ ,  $\bar{G}_w$ ,  $\bar{S}_w$ ,  $\bar{V}_w$ , ..., meaning  $U/M_s$ ,  $G_w/M_s$ ,  $S_w/M_s$ ,  $V_w/M_s$ , ..., and not the derivative  $dx/dm_s$  that the single bar means in many articles. Thus, the Gibbs-Duhem equation applied to the component  $i$  of the phase  $a$ , according to Spósito (1981, p. 15), can be rewritten in the SREV paradigm, such that:

$$\bar{S}_{\alpha i} dT - \bar{V}_{\alpha i} dP + W_{\alpha i} d\mu_{\alpha i} = 0 \quad (3)$$

where  $\bar{S}_{\alpha i}$ ,  $\bar{V}_{\alpha i}$ , and  $W_{\alpha i}$  are the massic entropy, massic volume and water content of component  $i$  of the phase  $a$ , all reported to the pedostructure mass of the sample  $M_s$ .

Using this terminology, it could be shown that the pedostructure water retention  $h$  (in kPa) must be defined as:

$$h = h_{ma} = h_{mi} = -\rho_w^0 (\mu_{ma} - \mu_{masat}) = -\rho_w^0 (\mu_{mi} - \mu_{misat}) \quad (4)$$

where  $\mu_{ma}$  and  $\mu_{mi}$  are the chemical potentials of the water in the pore spaces inter and intra primary peds, corresponding to the water contents  $W_{ma}$  and  $W_{mi}$ ; while  $\mu_{masat}$  and  $\mu_{misat}$  correspond to  $W_{masat}$  and  $W_{misat}$ . We should note that  $\mu_{masat} = \mu_w^0$ , the chemical potential of the free water, at ambient temperature and atmospheric pressure, while  $\mu_{misat} < \mu_{masat} = \mu_w^0$  in all cases.

**Table 1 | Pedostructure state variables.**

Volume of concern	Specific volume [dm <sup>3</sup> /kg]	Specific pore volume [dm <sup>3</sup> /kg]	Specific water content [kg <sub>water</sub> /kg <sub>soil</sub> ]	Suction [kPa]
Pedostructure	$\bar{V}$	$\bar{V}_p$	$W$	$h$
Interpedal porosity		$\bar{V}_{pma}$	$W_{ma}$	$h_{ma}, h_{ip}$
Primary peds	$\bar{V}_{mi}$	$\bar{V}_{pmi}$	$W_{mi}$	$h_{mi}$
Primary particles	$\bar{V}_s$			

Subscripts  $mi$ ,  $ma$  and  $s$ ; refer to micro, macro, and solids; (after Braudeau and Mohtar, 2014).

Showing that the pedostructural Gibbs free energy (accounted negatively) for each water component of the liquid phase:  $\bar{G}_{wmi} = W_{mi}\mu_{mi}$  and  $\bar{G}_{wma} = W_{ma}\mu_{ma}$ , remains constant after any change in water content. Braudeau et al. (2014) established the physical equation of  $h(W)$ , the soil water retention curve, for the general case of the pedostructure (structured soil medium).

$$h^{eq}(W) = \begin{cases} h_{mi}(W_{mi}^{eq}) = \rho_w^0 \bar{E}_{mi} \left( \frac{1}{W_{mi}^{eq}} - \frac{1}{W_{miSat}} \right), & \text{inside the primary peds} \\ h_{ma}(W_{ma}^{eq}) = \rho_w^0 \bar{E}_{ma} \left( \frac{1}{W_{ma}^{eq}} - \frac{1}{W_{maSat}} \right), & \text{outside the primary peds} \end{cases} \quad (5)$$

where,  $h_{mi}$  is the water retention inside the primary peds (kPa),  $h_{ma}$  is the water retention outside the primary peds (kPa);  $\rho_w^0$  is the bulk density of water [1kg<sub>water</sub>dm<sup>-3</sup>],  $\bar{E}_{mi}$  and  $\bar{E}_{ma}$  [Jkg<sub>solid</sub><sup>-1</sup>] are the specific potential energies inside the primary peds and outside of the primary peds. They result from the surface charges of the clay particles and are equal to  $-\bar{G}_{wmi}$  and  $-\bar{G}_{wma}$ , respectively.  $W_{mi}^{eq}$  and  $W_{ma}^{eq}$  are the micro and macropore water contents at equilibrium when  $h_{mi} = h_{ma} = h$ . Their equations, deduced from (4) and (5), are:

$$W_{ma}^{eq}(W) = \frac{1}{2} \left( W + \frac{\bar{E}}{A} \right) + \frac{1}{2} \sqrt{\left[ \left( W + \frac{\bar{E}}{A} \right)^2 - \left( 4 \frac{\bar{E}_{ma}}{A} W \right) \right]} \quad (6a)$$

and

$$W_{mi}^{eq}(W) = W - W_{ma}^{eq} = \frac{1}{2} \left( W - \frac{\bar{E}}{A} \right) - \frac{1}{2} \sqrt{\left[ \left( W + \frac{\bar{E}}{A} \right)^2 - \left( 4 \frac{\bar{E}_{ma}}{A} W \right) \right]} \quad (6b)$$

where,  $A$  is a constant representing the difference of chemical potentials of the two types of water ( $W_{ma}$  and  $W_{mi}$ ) at saturation:

$$A = -(\mu_{maSat} - \mu_{miSat}) = \frac{\bar{E}_{ma}}{W_{maSat}} - \frac{\bar{E}_{mi}}{W_{miSat}} \quad (7)$$

$$\bar{E} = \bar{E}_{mi} + \bar{E}_{ma} \quad (8)$$

and  $W_{miSat}$  and  $W_{maSat}$  are the micro and macro water content at saturation such that:

$$W_{Sat} = W_{miSat} + W_{maSat} \quad (9)$$

## THE pF CURVES

The pressure plate apparatus is widely used in pedology and agronomy to get what is named the pF curve: log of the suction pressure, expressed in cm of water height, vs. the water content  $W$ . Fully saturated soil (or clay paste) samples are put in contact with

a saturated porous plate and the whole is submitted to a given pressure  $P$  of the air introduced in the pressure chamber. The other side of the porous plate is open to the atmospheric pressure. The samples water content decreases under this pressure, the water crossing through the porous plate, until a thermodynamic equilibrium is reached. The pF curve is the air pressure applied on the sample (usually the log of this pressure in cm of water) vs. the corresponding water content (kg/kg) of the sample at equilibrium. The question is the following: is this pressure equivalent to the difference of the water chemical potentials as stated in Equation (2)?

Under the pressure (atmospheric pressure plus applied pressure:  $P_a + \Pi$ ) and when the transfer of water has ceased, the water content in the sample is  $W = \rho_w \bar{V}_w$  (remembering that  $\bar{V}_w = V_{water}/M_s$  and  $W = M_{water}/M_s$ , **Table 1**) and the water chemical potentials ( $\mu_w$ ) of the liquid and gas phases of the pedostructure and the pressure chamber, is equal to the potential of free water,  $\mu_w^0$ , which is the water chemical potential at the other side of the porous plate submitted to the atmospheric pressure. Thus, when the pressure is returned to  $P_a$  and the chamber is opened to the air without any change in water content of the sample ( $W$ ), the pedostructure water potential decreased from  $\mu_w^0$  (under  $P_a + \Pi$ ) to its equilibrium value,  $\mu_w$ , at ambient  $T$  and  $P_a$ . The water retention (or suction)  $h$  defined by Equation (4) passes from the value 0 to  $h = -\rho_w^0 (\mu_{wma} - \mu_w^0)$  under the atmospheric pressure  $P_a$ .

Consider now the Gibbs-Duhem equation Equation (3) is applied to the external layer of the pedostructure liquid phase at the liquid-gas interface (variables with subscript lg). At this interface, the state variables can be defined such that:  $W_{lg} = \Delta W_{ma}$ ,  $\bar{S}_{wlg} = \Delta \bar{S}_{wma}$ , and  $\bar{V}_{wlg} = \Delta \bar{V}_{wma}$ , thus, the equation can be written such that:

$$\bar{S}_{wlg} dT - \bar{V}_{wlg} dP + W_{lg} d\mu_{wma} = 0 \quad (10)$$

Dividing Equation (10) by  $W_{lg}$  gives a relationship between the specific entropy  $\hat{S}_{wlg} = \bar{S}_{wlg}/W_{lg}$  (in  $\text{JK}^{-1}\text{kg}^{-1}$  of water) and the specific volume  $\hat{V}_{wlg} = \bar{V}_{wlg}/W_{lg}$  (in  $\text{dm}^3\text{kg}^{-1}$  of water if  $P$  in kPa) of the liquid interface in contact with air in the pedostructure (soil) sample:

$$\hat{S}_{wlg} dT - \hat{V}_{wlg} dP + d\mu_{wlg} = 0 \quad (11)$$

On the other hand, the Gibbs-Duhem equation related to the water component of the gaseous phase of the pedostructure (variables with subscript g) at equilibrium with the air in the pressure chamber can also be written such that:

$$\bar{S}_{wlg} dT - \bar{V}_{wlg} dP + W_g d\mu_{wg} = 0 \quad (12)$$

where  $\bar{S}_{wlg}$ ,  $\bar{V}_{wlg}$ , and  $W_g$  are the entropy, the partial volume and the mass of the water molecules of all the gaseous phase (in the pedostructure and in the pressure chamber) reported to  $M_s$ . Then, dividing Equation (12) by  $W_g$  gives:

$$\hat{S}_{wlg} dT - \hat{V}_{wlg} dP + d\mu_{wg} = 0 \quad (13)$$

where  $\hat{S}_{wlg} = \bar{S}_{wlg}/W_g$ , the specific entropy of the water vapor, and  $\hat{V}_{wlg} = \bar{V}_{wlg}/W_g$ , the specific partial volume of the water vapor in the air. Assuming that all the components of the gaseous phase have behavior of perfect gas (subscript g) and, according to the state equation of ideal gasses:

$$\hat{V}_{wlg} M_w P = \hat{V}_g M_g P = V_A P = RT \quad (14)$$

where  $R$  ( $\text{Jmole}^{-1}\text{K}^{-1}$ ) is the constant of perfect gasses,  $M_w$  is the molar mass of water,  $M_g$  the molar mass of gas, and  $V_A$  is the volume of 1 mole of ideal gas at pressure  $P$  and temperature  $T$ .

Since  $d\mu_{wma} = d\mu_{wg}$  at equilibrium of the two phases in contact (exchange of molecules of water) subtracting Equation (11) from Equation (13) gives:

$$(\hat{S}_{wlg} - \hat{S}_{wlg}) dT - \hat{V}_{wlg} dP + \hat{V}_{wlg} dP = 0 \quad (15)$$

Thus, in a transformation at  $T$  constant:

$$\hat{V}_{wlg} dP = \hat{V}_{wlg} dP \quad (16)$$

meaning that  $\hat{V}_{wlg}$  stays equal to  $\hat{V}_{wlg}$  in this transformation and, according to Equation (14),

$$\hat{V}_{wlg} P = \hat{V}_{wlg} P = RT/M_w \quad (17)$$

Integrating Equations (11) and (13) from the hydrostructural state of the sample under  $(P_a + \Pi)$  to the state at  $P_a$  in the pressure apparatus, keeping  $T$  and  $W$  constant and replacing  $\hat{V}_{wlg}$  and  $\hat{V}_{wlg}$  by their expression given by Equation (17), provides the same formulation of  $h$  Equation (20):

$$\int_{P_a+\Pi}^{P_a} \hat{V}_{wlg} dP = \int_{P_a+\Pi}^{P_a} \hat{V}_{wlg} dP = RT/M_w \ln((P_a + \Pi)/P_a) \quad (18)$$

$$\int_{\mu_w^0}^{\mu_w} d\mu_{wlg} = \int_{\mu_w^0}^{\mu_w} d\mu_{wg} = (\mu_w^0 - \mu_{wlg}) = (\mu_w^0 - \mu_{wg}) = h^{eq}/\rho_w \quad (19)$$

$$h^{eq} = -\rho_w \Delta \mu_w = \rho_w RT / M_w \ln((P_a + \Pi)/P_a) \quad (20)$$

$\Delta \mu_w$  is numerically equal to  $\psi/m$  since  $\mu_w^0$  and  $\mu_w$  are the values of the chemical water potential at  $T$  and  $P$  constant (laboratory conditions). Thus, a pressure of  $(P_a + \Pi)$  in the pressure plate apparatus leads, at equilibrium, to a water content  $W$  corresponding to the water retention  $h$  given by Equation (20), analog to the water retention measured by the tensiometer under the atmospheric pressure.

Replacing  $h^{eq}$  by its equation in terms of  $W_{ma}^{eq}$  or  $W_{mi}^{eq}$  Equation (5) leads to the relationship between the applied air pressure in the chamber and the two pedostructural water contents  $W_{mi}$  and  $W_{ma}$ , such that:

$$\begin{aligned} (P_a + \Pi)/P_a &= \exp\left(\frac{M_w \bar{E}_{mi}}{RT} \left(\frac{1}{W_{mi}^{eq}} - \frac{1}{W_{miSat}}\right)\right) \\ &= \exp\left(\frac{M_w \bar{E}_{ma}}{RT} \left(\frac{1}{W_{ma}^{eq}} - \frac{1}{W_{maSat}}\right)\right) \quad (21) \end{aligned}$$

where  $W_{mi}^{eq}$  and  $W_{ma}^{eq}$  are calculated using Equations (6a) and (6b).

The difference between the “lg” and “g” phases stays only in the fact that the fraction of water molecules is 1 in the liquid-gas interface while this fraction is  $N_{wg}/N_g = p_w/P$  in the gaseous phase of the sample and the pressure chamber;  $p_w$  is the partial pressure of water vapor,  $N_w$  the number of water molecules and  $N_g$  the total number of gas molecules in the air phase. This means also that  $p_w = P$  in the “lg” interface.

## MATERIALS AND METHODS

To validate the theory above we need to compare the two soil water retention curves obtained by the two methods using: the tensiometer (Braudeau et al., 2014) and the pressure plate apparatus (Richards, 1948). The tensiometric measurements were made on unconfined cylindrical soil samples reconstituted from 2 mm-sieved soil material and using the TypoSoil® apparatus according to the methodology described in Assi et al. (2014). The preparation of the sample, the measurement and the treatment of data to extract parameters of the water retention curve:  $E_{ma}$ ,  $E_{mi}$ ,  $W_{miSat}$  and  $W_{maSat}$ , of Equations (5) and (6) have been detailed in the article.

As for the pressure plate apparatus method, the obtained curves called “pF curves” represent generally the log of the applied air pressure, in hPa, vs. the corresponding water content in kg/kg, at equilibrium under this air pressure. In this classical method, the applied pressure is identified to the water retention  $h$ , contrary to what we have deduced here in the theory where  $h$  is proportional to the logarithm of the applied pressure. The samples put on the porous plate are constituted of 2 mm-thick slices cut from the cylindrical samples prepared for the TypoSoil® analysis (Assi et al., 2014). The slices (three replicates for the water content measurement at a given pressure) were put in a ring on the porous plate and saturated with water.

Two types of soil were tested; they are the same as those used in Braudeau et al. (2014) article: a soil sample of Versailles soil from France, and a soil sample of Rodah soil from Qatar. Their characteristics are given in Table 2.

For each soil, two replicates of a pedostructure sample were prepared in cylinders of 5 cm diameter and height using the

*fine ground* samples (aggregated soil material < 2 mm) stored in the laboratory. The two moisture characteristic curves,  $\bar{V}(W)$  and  $h(W)$ , were then measured using the TypoSoil® apparatus following the methodology mentioned above (Assi et al., 2014).

The pF curves for the two soils were measured using the pressure plate apparatus but at two different places and times, so the set of data making the curve (applied pressure and water content) is different in the two cases: For the Rodah soil, pressures applied (kPa) were: 80, 100, 150, 200, 400, 1000; using only one kind of porous plate: “15 bar,” and for the Versailles soil, pressures applied were: 1, 5, 10, 30, 50, 80, 100, 200 kPa, using a porous plate of “1 bar” for the low values of pressure and 5 bar for 100 and 200 kPa. A beaker of 50 cm<sup>3</sup> of water was put on the 15 bar plate to saturate the air in the chamber and the waiting time to reach equilibrium was no more than 1 week.

These sets of applied pressures are converted into the water retention of the sample  $h$  (in kPa) corresponding to the water content reached at equilibrium under the applied pressure  $\Pi$ , using Equation (20) where  $R = 8.314 \text{ J mole}^{-1} \text{ K}^{-1}$ ,  $T = 294 \text{ K}$  for Rodah and 298 K (for Versailles),  $M_w = 0.018 \text{ kg mole}^{-1}$  and  $\rho_w = 1 \text{ kg dm}^{-3}$ . Practically, the relationships used for the correspondence between the applied pressure,  $\Pi$ , and the water retention at equilibrium is, for  $T = 294 \text{ K}$ :

$$h = 13.772 \ln(\Pi/100 + 1) \quad (22)$$

where  $h$  and  $\Pi$  are expressed in kPa.

Parameters of the pedostructural water retention curve ( $W_{Sat}$ ,  $W_{miSat}$ ,  $\bar{E}_{mi}$ ,  $\bar{E}_{ma}$ ) are then extracted from the measured water retention curve according to the methodology given in Braudeau et al. (2014) and detailed in Assi et al. (2014) by adjustment of the theoretical equation  $h(W)$  to the measured curve. All calculations were done in Excel sheets, using the Excel solver for optimization of adjustments of the measured curve by the theoretical one.

## RESULTS

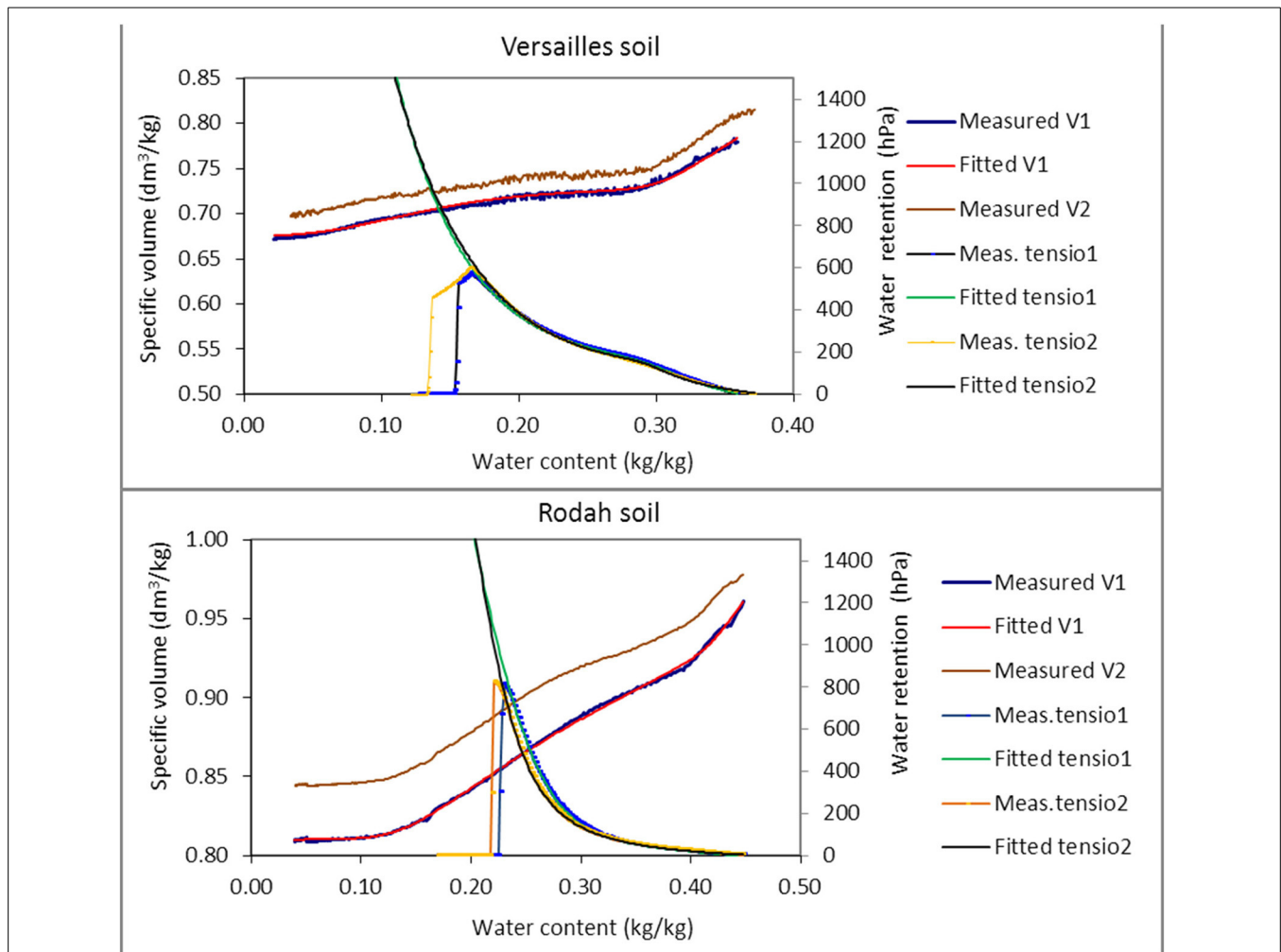
### COMPARISON OF WATER RETENTION CURVES OBTAINED BY THE TWO METHODS

The pedostructural moisture characteristic curves (water retention curve, WRC, and shrinkage curve, ShC) of the two replicates of pedostructure prepared for each soil were measured using TypoSoil®. Then, the curves were fitted by their theoretical equations to obtain the corresponding hydrostructural parameters. The methodology of fitting is explained in Braudeau et al. (2014) for the kind of soil sample analyzed here (Figure 1), presenting

**Table 2 | General description of soil samples.**

Sample ID	Soil core	Sample location	Description of the soil sample	Soil texture		
				% clay	% silt	% sand
V4	Reconstituted pedostructure	France	Sampled from the surface horizon [0–20 cm] of a soil in the Versailles agronomic research center	18.2	60.2	21.6
V5						
R1	Reconstituted pedostructure	Qatar	Samples taken from 0 to 15 cm depth of a soil named locally Rodah	39	52	9
R2						





**FIGURE 1 | Pedostructural moisture characteristic curves of two replicates of a pedostructure sample of two soils.** For each soil, the curves of the two replicates are represented: (i) The measured (blue points) and fitted (red) shrinkage curve (ShC), for replicate 1; (ii) The

measured shrinkage curve (brown points) for replicate 2; (iii) The measured (blue points with line) and fitted (green) water retention curve (WRC); and (iiii) the measured (brown points with line) and fitted (black line) water retention curve for replicate 2.

**Table 3 | Values of parameters of the pedostructural water retention curve for Rodah and Versailles soils.**

Sample ID	Hydro-structural parameters of pedostructure water retention curve						
	$W_{miSat}$ [ $\text{kg}_{\text{water}}\text{kg}_{\text{soil}}^{-1}$ ]	$E_{ma}$ [ $\text{Jkg}_{\text{soil}}^{-1}$ ]	$E_{mi}$ [ $\text{J kg}_{\text{soil}}^{-1}$ ]	$W_{sat}$ [ $\text{kg}_{\text{water}}\text{kg}_{\text{soil}}^{-1}$ ]	$W_{ipo}$ [ $\text{kg}_{\text{water}}\text{kg}_{\text{soil}}^{-1}$ ]	$k_L$ [ $\text{kg}_{\text{soil}}\text{kg}_{\text{water}}^{-1}$ ]	$W_L$ [ $\text{kg}_{\text{water}}\text{kg}_{\text{soil}}^{-1}$ ]
R1	0.265	0.82	116.26	0.442	0.113	112	0.417
R2	0.238	1.30	163.42	0.463	0.174	120	0.394
RpF	0.261	1.09	136.94	0.440	–	–	–
V1	0.163	1.81	33.38	0.362	0.059	83	0.302
V2	0.190	1.22	29.45	0.380	0.051	0.780	0.302
VpF	0.215	1.43	29.31	0.384	–	–	–

R1 and R2, V1 and V2, refer to replicates 1 and 2 of the Rodah soil and the Versailles soil respectively, of which the WRC was measured by tensiometers. RpF and VpF refer to the Rodah soil and the Versailles soil of which the water retention curve were measured with the pressure plate apparatus.

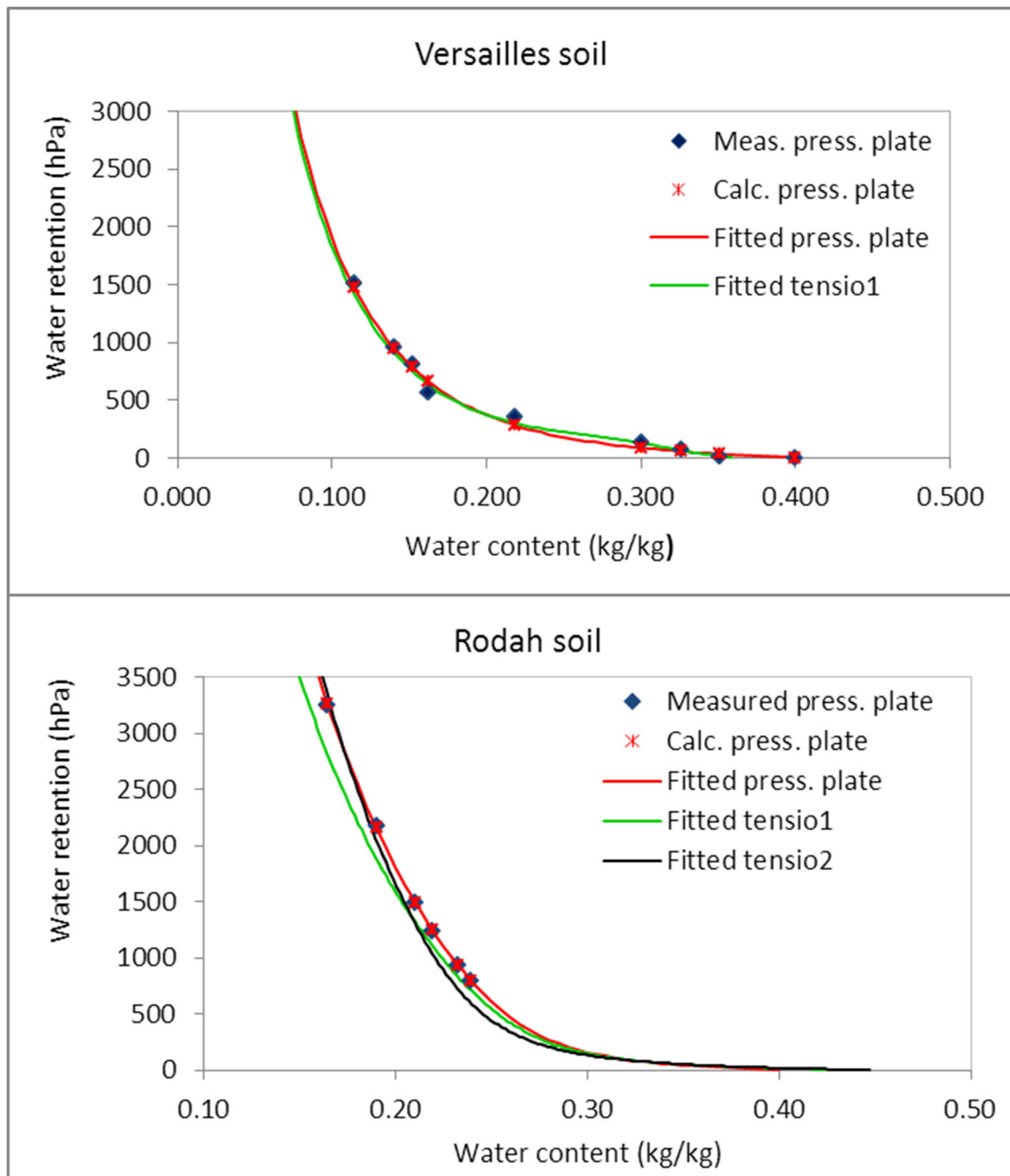
a sigmoidal shape with a shrinkage phase due to the saturating interpedal water  $W_{ip}$  at high value of  $W$ . The hydrostructural parameters of the water retention curve obtained from the optimization of the adjustment are given in **Table 3**.

The measured characteristic curves of the replicates are very close to each other (**Figure 1**), attesting the appropriate preparation procedures of the pedostructure samples and the accuracy of their characterization. The shrinkage curves are shifted only

by a constant value of the specific volume and the water retention curves of the two replicates are almost superimposed in both cases, although the validity of measurement is limited to low values of suction (800 hPa for Rodah soil and 600 Pa for Versailles soil on **Figure 1**). As their physical equation is known (Equation 5) and assumed to be valid for the whole curve (at least up to air entry point in primary peds), and because parameters can be determined on the range measured by the tensiometer, the

modeled water retention curves cover the whole range of water contents and can be compared to the results given by the pressure plate apparatus.

This comparison is presented in **Figure 2** which shows for each soil the water retention curves: (i) measured with the pressure plate apparatus, (ii) modeled by fitting on the measured points of the pF curve, and (iii) modeled using parameters extracted from the tensiometric curve measured by TypoSoil®. The pressure plate



**FIGURE 2 | Three water retention curves for each soil.** (i) Measured (dark-blue points) using the pressure plate apparatus, (ii) Fitted (red line and crosses) on these measured points using the

theoretical equation of the curve and (iii) (green line and black line) fitted on the measured water retention curve using a tensiometer.

**Table 4 | Data of the pressure plate apparatus experiment for the measurement of the water retention curve (pF curve) of two soils.**

Versailles soil			Rodah soil		
Air pressure applied [hPa]	Water retention pressure [hPa]	Water content at equilibrium [ $\text{kg}_{\text{water}}\text{kg}_{\text{soil}}^{-1}$ ]	Air pressure applied [hPa]	Water retention pressure [hPa]	Water content at equilibrium [ $\text{kg}_{\text{water}}\text{kg}_{\text{soil}}^{-1}$ ]
0	3	0.400	0	3	0.44
10	14	0.351	–	–	–
50	67	0.326	–	–	–
100	131	0.300	800	796	0.239
300	361	0.218	1000	939	0.232
500	558	0.162	1500	1241	0.219
800	809	0.152	2000	1488	0.210
1000	955	0.140	4000	2179	0.190
2000	1513	0.114	10,000	3247	0.164

Calculation of the water retention corresponding to the applied air pressure is explained in the text.

**Table 5 | Chimney Meadow (Church Field) soil water retention measurements (pF curves) data.**

Given pF	Applied pressure [hPa]	Measur. method	Corresponding water retention [hPa]	Depth levels of (cm)								
				0–10 cm	10–20 cm	30–40 cm	40–50 cm	50–60 cm	60–70 cm	70–80 cm	80–90 cm	90–100 cm
Water content [ $\text{kg}_{\text{water}}\text{kg}_{\text{soil}}^{-1}$ ]												
Saturation	–1	(1)	1	0.363	0.352	0.293	0.327	0.329	0.370	0.396	0.330	0.304
pF1.0	–10	(1)	10	0.351	0.337	0.286	0.318	0.319	0.352	0.393	0.317	0.291
pF 1.5	–32	(1)	32	0.348	0.337	0.284	0.303	0.317	0.344	0.386	0.313	0.290
pF 1.8	–63	(1)	63	0.340	0.329	0.275	0.291	0.310	0.336	0.372	0.309	0.288
pF 2.0	–100	(1)	100	0.339	0.326	0.273	0.289	0.309	0.333	0.369	0.306	0.286
pF 2.3	–200	(2)	200	0.332	0.318	0.270	0.285	0.305	0.328	0.362	0.303	0.282
pF 2.7	–500	(2)	500	0.293	0.284	0.252	0.266	0.290	0.313	0.339	0.286	0.266
pF 3.48	3000	(3)	1877	0.262	0.266	0.233	0.243	0.267	0.287	0.304	0.261	0.246
pF 3.71	5000	(3)	2426	0.239	0.247	0.224	0.230	0.254	0.272	0.289	0.251	0.231
pF 4.18	15000	(3)	3754	0.195	0.203	0.198	0.200	0.224	0.234	0.247	0.214	0.201

The third column indicates the experimental conditions (in the text) and the 4th column gives the theoretical water retention (or suction) pressure  $h$  corresponding to the given pF in the first column.

measurement data are given in **Table 4**. We can see from **Figure 2**, the very good concordance of the curves coming from the two kinds of measurement. This confirms the validity of the relationship Equations (20) and (22) between the applied pressure  $\Pi$  and the corresponding matric (or pedostructural) water retention  $h$ .

Moreover, as it can be seen in **Table 3**, the fitting using the physical equation of the water retention curve on the points measured with the pressure plate apparatus, provides parameters (lines RpF and Vpf of **Table 3**) that are very close to those of the modeled curve coming from the tensiometer (lines R1, R2, V1, V2).

We can conclude from these results that the water retention curve can be accurately measured using the tensiometer as well as the pressure plate apparatus, provided that, in this last case,  $h$  has been calculated from  $\Pi$  using Equation (20). Accordingly, the four hydrostructural parameters of the water retention curve, namely:  $W_{Sat}$ ,  $W_{miSat}$ ,  $\bar{E}_{mi}$ , and  $\bar{E}_{ma}$ , characterizing the pedostructure, can be obtained from the one or the other method. However, the tensiometer method is faster and very accurate at low retention pressure (0–500 hPa). It should be preferred, in particular for the kind of soil like those selected

here which presents an interpedal shrinkage phase parallel to the saturated line, at the beginning of the shrinkage curve, and for which two parameters more are needed:  $W_L$  and  $k_L$  (Braudeau et al., 2014). The shape of the retention curve in this part, near saturation, looks like the traditional curves with an air entry near saturation (at  $\theta_w$ , similar to  $W_L$ ). These parameters make part of the set of soil characteristics required by the multiscale soil water model Kamel® (Braudeau and Mohtar, 2014) built in respect to the new paradigm of the hydrostructural Pedology. An example of treatment of pF curves according this new paradigm is given here after.

#### APPLICATION TO pF CURVES FOUND IN SOIL DATA BASES

As an example of application, we used the data of water retention curves published on the web by the Center of Ecology and Hydrology (Blyth, 2011). The water retention curves (pF curves) were constructed as follows: “At each depth, two samples were collected. The samples were stood in a water bath until they reached an equilibrium (saturated) weight. The samples were then placed in (1) a sand bath, (2) a sand/kaolin bath, (3) pressure vessels set at a range of suctions in order to progressively dry



**Table 6 | Pedostructural water retention curve parameters obtained by fitting the corrected Chimney Meadow soil water retention curves with the theoretical equation.**

Depth level	$W_{sat}$ [kg <sub>water</sub> kg <sub>soil</sub> <sup>-1</sup> ]	$W_{miSat}$ [kg <sub>water</sub> kg <sub>soil</sub> <sup>-1</sup> ]	$E_{ma}$ [J kg <sub>soil</sub> <sup>-1</sup> ]	$E_{mi}$ [J kg <sub>soil</sub> <sup>-1</sup> ]	$E_{mi}/E_{ma}$
CM 0–10	0.363	0.344	0.015	181	8.20E-05
CM 10–20	0.352	0.329	0.015	217	6.78E-05
CM 30–40	0.293	0.273	0.032	282	1.14E-04
CM 40–50	0.327	0.290	0.030	256	1.17E-04
CM 50–60	0.329	0.310	0.016	322	5.09E-05
CM 60–70	0.370	0.334	0.028	322	8.65E-05
CM 70–80	0.396	0.369	0.062	299	2.08E-04
CM 80–90	0.330	0.309	0.015	287	5.37E-05
CM 90–100	0.304	0.287	0.012	264	4.72E-05

out the samples. Water-release curves were constructed for each soil level.” **Table 5** presents the water retention data re-arranged such that: (i) the set of the different pF values (1st column) given by the authors; these pF values are the currently assumed ones corresponding to the log of the water suction expressed in hPa or cm of water (2nd column); (ii) the method used for equilibrium of the sample under suction (methods 1 and 2) or under air pressure in the pressure plate apparatus (method 3); and (iii) the corresponding value of the water retention pressure  $h$  in hPa, equal to the suction pressure for the measurement methods (1) and (2) and calculated using Equation (20) for the pressure plate method (3).

Four selected pedostructural water retention curves, among the nine listed in **Table 5**, are shown in **Figure 3**; the measured points are presented with their fitted theoretical curve. The corresponding parameters obtained from the fitting of the measured points are presented in **Table 6** for the 9 samples. The high values of  $W_{miSat}$  relative to  $W_{sat}$  and of  $E_{mi}$  relative to  $E_{ma}$  indicate that the soil is clayey and has a small macro porosity (interpedal porosity).

The sets of four parameters characterizing each layer are not very different from each other. This is consistent with the description of the soil given in the report: “Church Field lies on a clay lens which overlies surrounding sand and gravel soils. Apart from the A and B horizons, the clay was found to be fairly homogenous down to the maximum depth of 1.1 m of the access pit.”

## DISCUSSION

### COMPARISON WITH THE MEMBRANE PRESS RESULTS OF LOW (1979) ON CLAY PASTES

Results show clearly that the relationship between the applied air pressure in the pressure plate apparatus and the pedostructure water retention pressure  $h(W)$ , as it is measured by the tensiometer in the laboratory, is described by Equation (20). This leads to Equation (21) between the air pressure and the pedostructural macro and micro water contents at equilibrium  $W_{mi}^{eq}$  and  $W_{ma}^{eq}$ . This equation is similar to the empirical equation found by Low and Margheim (1979) between the applied pressure  $\Pi$  and the water content of the clay pastes in the membrane press apparatus and that Low (1979) expressed such as:

$$\Pi + 1 = \exp(\alpha (m_c/m_w - m_c/m_w^0)) \quad (23)$$

in which  $m_c/m_w$  is the mass ratio of water to montmorillonite,  $\Pi$  is the applied pressure, in units of atmosphere, “and  $\alpha$  is a linear function of the specific surface area and cation exchange capacity.” This equation was obtained for clay pastes which has no structure, so we can identify  $m_c/m_w$  with  $1/W_{mi}$ , so Equation (23) can be written as:

$$(P_a + \Pi)/P_a = \exp(\alpha (1/W_{mi} - 1/W_{mi}^0)) \quad (24)$$

Comparing this equation to Equation (21), gives:

$\alpha = M_w \bar{E}_{mi}/RT$  and  $W_{mi}^0 = W_{miSat}$ , the maximum of absorbed water by the clay paste.

The water content  $W_{ma}$  is negligible and concerns the layer of water at the surface of the clay paste in contact with the air. Therefore, Low’s equation expresses, in fact, the following relationship between the applied pressure and the matric potential  $\psi_m$  of the clay paste:

$$(P_a + \Pi)/P_a = \exp(-\psi_m M_w/RT) \quad (25)$$

where  $\psi_m = \Delta\mu_w = -h/\rho_w^0 = -\bar{E}_{mi}(1/W_{mi} - 1/W_{miSat})$ , contrary to what Low (1979) was thinking, namely that  $\Pi$  could be identified to the swelling pressure ( $-\rho_w \Delta\mu_w$ ).

### WATER VAPOR PRESSURE $p_w$ AT THE SURFACE OF THE PEDOSTRUCTURAL WATER

Equation (25) can be written as:

$$\mu_w - \mu_w^0 = RT/M_w \ln(P_a/(P_a + \Pi)) \quad (26)$$

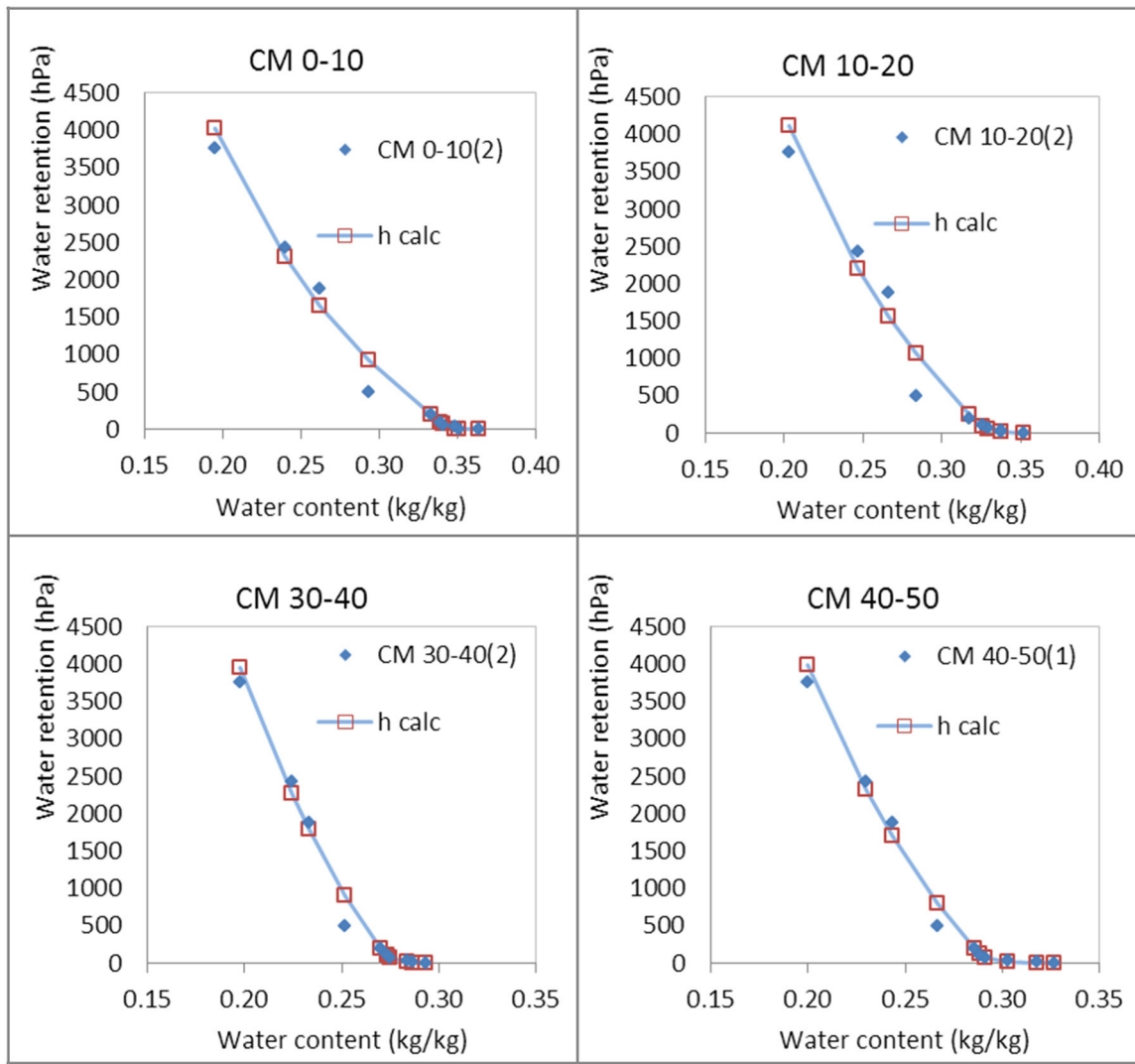
This means that, assuming the well-known relationship between  $\mu_w - \mu_w^0$  and the water vapor pressure  $p_w$  at the surface of water in the pedostructure, Equation (25) can also be written such that:

$$\mu_w - \mu_w^0 = RT/M_w \ln(p_w/p_w^0) \quad (27)$$

this relationship compared to Equation (26) leads to:

$$P_a/(P_a + \Pi) = p_w/p_w^0 \quad (28)$$

where  $p_w^0$  is the water vapor pressure over pure water at ambient  $T$  and  $P$ .



**FIGURE 3 |** Pedostructural water retention curves of the four first depth levels of the Chimney Meadow (Church Field) soil, measured (blue points) and fitted with the theoretical equation (blue line and red squares).

On the other hand, considering the external layer of the interface liquid-gas “lg,” where the partial pressure of water is  $p_w = P$  (the pressure in the chamber), and taking into account Equation (17), we have the following equalities:

$$p_w^0/p_w = (P_a + \Pi)/P_a = \hat{V}_{wlg}/\hat{V}_{wlg}^0 = \exp(-M_w\psi_m/RT) \tag{29}$$

These equalities (29) could explain the assertion of Low (1980) who said that “Our evidence shows that every property of the interlayer water obeys the following general equation:

$$J/J^0 = \exp(\beta m_c/m_w) \tag{30}$$

in which  $J$  represents any given property of the interlayer water,  $J^0$  represents the value of this property for pure bulk water and  $b$  is

a constant.” In fact, according to our results, we should have:

$$\ln(J/J^0) = \beta (m_c/m_w - m_c/m_{wSat}) = -(\beta/\alpha) \psi_m M_w/RT \tag{31}$$

which, according to (29), leads to:

$$(J/J^0)^{\alpha/\beta} = \hat{V}_{wlg}/\hat{V}_{wlg}^0 = \exp(\alpha (1/W_{mi} - 1/W_{miSat})) \tag{32}$$

Thus, Equation (30) of Low (1980) could be explained by the direct relationship of any thermodynamic property  $J$  of the water at the surface of clays with the specific volume  $\hat{V}_{wlg}$  of the water layer at the interface liquid-vapor which depends on the water content of the clay paste according to Equation (32).

## FUNDAMENTALS OF THE PEDOSTRUCTURAL WATER THERMODYNAMICS

The definition of the matric potential by Sposito (1981) as representing “the effect of changes in the water content” at  $T$  and  $P$  constant, is in total agreement with our results obtained here. The thermodynamic equation of the pedostructural water retention curve, which was validated only on the little validity range of tensiometers, is validated now on the larger range covered by the pressure plate method. It is obvious that the “matric potential” defined above and which is the potential of a mixture of soil particles, water and air, corresponds to the “pedostructural water potential,” the potential of the water contained in the pedostructure which is defined in the SREV paradigm as a thermodynamic system representing the soil medium at its first levels of organization: those of the primary peds and their assembly. It’s why we could define two phases in the water phase of the soil matric: one ( $W_{mi}$ ) embedded in the other ( $W_{ma}$ ), corresponding to the intra and inter- primary peds. Primary peds correspond to the first level of aggregation of clay particles. The thermodynamic law that we evidenced in our experiments and which is at the basis of the pedostructural water retention equation, is that the pedostructural Gibbs free energies (accounted negatively in  $\text{Jkg}^{-1}$  of solids) for each water component of the liquid phase,  $\bar{G}_{wmi}$  and  $\bar{G}_{wma}$ , defined as the products:

$$\bar{G}_{wmi} = W_{mi}\mu_{mi} \text{ and } \bar{G}_{wma} = W_{ma}\mu_{ma}, \quad (33)$$

remain constant (equal respectively to  $-\bar{E}_{mi}$  and  $-\bar{E}_{ma}$ ) against any change in water content.

This law is, for the pedostructural water liquid phase, of the same nature as the perfect gasses law for the gaseous phase. Any change in water content provokes a change in  $W_{mi}$  and  $W_{ma}$  and simultaneously a change in  $\mu_{mi}$  and  $\mu_{ma}$  such that their products stay constant according to Equation (34):

$$d\bar{G}_w = d\bar{G}_{wmi} = d\bar{G}_{wma} = 0 \quad (34)$$

From this phenomenon ( $\bar{G}_{wmi}$  and  $\bar{G}_{wma}$  constant), we can deduce immediately the following fundamental equation:

$$d\bar{G}_w = -\bar{S}_w dT + \bar{V}_w dP + \mu_{mi} dW_{mi} + \mu_{ma} dW_{ma} = 0 \quad (35)$$

leading to the Gibbs-Duhem equation for both phases, like Equation (3) for  $W_{ma}$  above.

In conclusion, we can say that the matric potential as defined by Sposito (1981) is exactly the pedostructural water potential as defined by:

$$\psi_m = (\mu_{ma} - \mu_{maSat}) = (\mu_{mi} - \mu_{miSat}) \text{ in } \text{Jkg}^{-1} \text{ of water} \quad (36)$$

Divided by the negative value of the bulk water density ( $-\rho_w^0$ ), it has unit of pressure and can be called: water retention pressure (or matric suction pressure)  $h$ ,

$$h = -\rho_w^0 \psi_m \text{ (in kPa with } \rho_w^0 = 1\text{kgdm}^{-3}\text{)} \quad (37)$$

The pedostructural water potential  $\psi_m$  can also be expressed in water head (m) by dividing by the gravitational acceleration  $g$ .

$$h = \psi_m/g \text{ (in m, negative)} \quad (38)$$

The conversion between the different units is as follows: 1019 cm of water head = 1 bar = 1000 hPa = 100 kPa

## CORRECTIONS TO MAKE ON THE RETENTION CURVES GIVEN BY PTFs

Pedotransfer functions (PTFs) are widely used in soil water modeling to estimate the hydraulic characteristics of soils from simple soil characteristics, such as texture, organic matter content, etc. Tietje and Tapkenhinrichs (1993) “grouped PTFs into three categories: (i) estimate the water content at certain matric potentials; (ii) estimate soil water retention relation with a physical conceptual modeling approach, and (iii) estimate parameters of an algebraic retention function.” Corrections that should be done are only those concerning the retention pressures above 60 kPa that are yielded by PTFs of the first and third group. It would consist to calculate the corrected values of  $h$  using Equation (20) or (22) replacing  $\Pi$  by the value of  $h$  given by the PTF. For example, the retention function estimated by Saxton and Rawls (2006) between 1500 and 33 kPa, namely:  $\psi_{(1500-33)} = A\theta^{-B}$ , where  $A$  and  $B$  are estimated such as:  $A = \exp(\ln(33) + B\ln(\theta_{33}))$  and  $B = [\ln(1500) - \ln(\theta_{33})]/[\ln(\theta_{1500}) - \ln(\theta_{33})]$ . We can just correct the parameter  $B$  by using  $\ln(382)$  instead of  $\ln(1500)$  in the formula and calculate  $\psi_{(1500-33)}$  using the corrected parameters, or we can also let the parameters as they are and correct the retention pressure  $\psi_{(1500-33)}$  by using Equation (22) such as (in kPa):

$$h = 13.772 \ln(A(\theta)^{-B}/100 + 1) \quad (39)$$

The proposed correction would be valuable in principle for all retention functions falling in the third category and currently used in soil-water models, like the very popular equation of van Genuchten (1980). In contrast, retention functions of the second category like the one proposed by Rieu and Sposito (1991) do not need this kind of correction above and are well working but only if parameters of the curve are accurately measured (Braudeau and Mohtar, 2004).

The correction brought to  $\psi_{(1500)}$  seems enormous: passing from 1500 to 382 kPa. In fact, looking at **Table 4**, we can see that the corrections for the suction pressures generated by the pressure plate are negligible in the range 0–100 kPa, but then they are exponentially increased after 100 kPa. This corresponds to the results of Solone et al. (2012), Bittelli and Flury (2009) and Cresswell et al. (2008) who worked on the adequacy of the pressure plate for determining the water retention curve: the measured total water potential using a thermocouple psychrometer was consistently less negative (wetter) than the expected matric potential of the sample (identified to the applied air pressure) after equilibrium in the pressure plate apparatus. The discrepancy between both measurements (dew point and pressure plate) appears at 100 kPa and increases strongly thereafter depending on the texture. However, they observed that the expected matric potential  $-1.5$  MPa can be obtained, in certain conditions, for rigid soils (non-swelling soils,

sandy soils). Our interpretation is that the matric potential sensu stricto is the specific potential energy of the water surrounding the clay particles and so, in contact with their surface charges. The clay particles are never cemented between them: if there is no swelling of the matric, the matric potential that we want to measure does not exist and the sample is like a bundle of capillary tubes on which the air pressure acts like a piston to remove the water from the sample; it is not the thermodynamic equilibrium by which the matric potential is defined.

## CONCLUSION

In order to theoretically formulate and unify the water retention curve measured by pressure plate and tensiometers, we have analyzed the measurement method of pF curves by the pressure plate apparatus based on the thermodynamic theory of the soil medium organization (Pedostructure-SREV concept). The same theoretical paradigm has been applied before only on the tensiometric measurement range (0–80 hPa) for the water retention curve (Braudeau et al., 2014). In this paper, we were able then to compare the results given by both methods (tensiometer and pressure plate) with those given by the theoretical equations. The parameters used in these equations were extracted from the measured WRC by TypoSoil®. It was found that the pressure plate method provides in fact measured points of the characteristic retention curve  $h(W)$  of the soil sample, but after a certain calculation of  $h$  from the applied air pressure  $\Pi$  that has been established according to the theory. Besides the fact that the thermodynamic analysis of the pressure plate method has led to a thermodynamic definition of what quantity is actually measured by this method, explaining old results obtained on clays pastes, this work has several significant practical implications in soil science, as follows:

- What is called matric water potential or matric potential ( $\psi_m$ , negative), as was well defined by Sposito (1981) in the REV paradigm, corresponds quantitatively to the “pedostructure water potential” defined in the SREV paradigm. Other terms can be encountered in soil science and agro environmental modeling, but all refer to this physical quantity ( $\psi_m$ ) which can be expressed in units of pressure ( $-\rho_w^0 \psi_m$ ) (then qualified by the term “pressure,” positively valued) or expressed in units of length and qualified by the term head (i.e., matric pressure head, negative).
- The water retention curve measured in laboratory using tensiometer is very precise but only valid within a limited range of water retention, from 0 at saturation to near 60 kPa; our results showed that it can be extended to high retention pressure (at least 1500 kPa) using the modeled curve of which the hydrostructural characteristic parameters have been obtained from tensiometric curves, using the valid range of measurement. This was confirmed by the points of the water retention curve obtained at high pressure by the pressure plate method on the same soil sample.
- We can now reconsider the “pF curves” stored in soil data bases and transform them into the correct pedostructure water retention curves that are characteristic of the soil horizon which was sampled. We showed how the four hydrostructural

parameters of these curves can be easily extracted by fitting with the thermodynamically-based equation of the curve. These parameters are physically-based and so are universal and valuable for all type of soils, opening the way for building a hydro-functional typology of the pedostructures. They represent the entire soil water retention curve that is needed by all models of soil water dynamics.

## ACKNOWLEDGMENTS

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