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# Analysis of lightweight composite sections with reinforced concrete infill with autoclaved aerated concrete (AAC)

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The development of composite sections is of great importance in structural design, with the aim of reducing weight and deflection while limiting the effect on the composite section's strength and durability. This paper examines the computational analysis of composite sections where reinforced concrete was replaced with autoclaved aerated concrete (AAC) in the compression zone. The first principles of concrete combined with Hook's law were adopted to find a flexure, shear, equivalent modulus of elasticity, effective moment of inertia, and deflection. The results are discussed and investigated using the finite element models developed by ANSYS WORKBENCH software. We found that the proposed analytical model can effectively provide a solution for the composite crosssection. The comparison between the theoretical calculation of the first cracking loads and the finite element percentage ranges from 89 to 110%. The ratio of the computational calculation of the modulus of elasticity to the finite element results ranged from 0.91 to 1.06. The comparison between the theoretical calculation of the effective moment of inertia to the finite element percentage ranged from 92% to 118%. The ratio of the computational calculation deflection to the finite element ranged from 0.87 to 1.15.

#### KEYWORDS

AAC, composite section, ANSYS, equivalent modulus of elasticity, effective moment of inertia

## Introduction

Autoclaved aerated concrete (AAC) is a low-density cementitious product of calcium silicate hydrate as a form of cellular concrete. The low density is obtained by forming microscopic air bubbles, which mainly occurs by chemical reactions during the liquid or plastic phase. These air bubbles are uniformly distributed and retained in the matrix during the setting, hardening, and subsequent curing with high-pressure steam in an autoclave to produce a homogeneous structure with microscopic void cells. AAC was first commercially produced in Sweden in 1923. Since then, its production and use have globally spread to more than 40 countries including North America, Central and South America, Europe, the Middle East, the Far East, and Australia. This has produced many case studies in different climates and under different building codes. In the United States, the modern uses of AAC began in 1990 for residential and commercial projects in the southeastern states (ACI, 2009). Farid et al. (2017) presented a vision of a newly planned autoclaved aerated concrete and concrete sandwich composite. The trials are shown in certain



stages to clarify the testing of the strategic sandwiching system. Three groups of initial sandwich samples were prepared with a changed mixture of autoclaved aerated concrete and concrete. Huang et al. (2019) experimentally studied a great-length multi-ribbed compound slab with filled lightweight blocks of autoclaved aerated concrete. The flexural behavior of four synthetic slabs and one general concrete slab was tested for the bending, buckling, and bearing capacity. Stress-strain curves of the tensile rebars were also analyzed. Wahyuni (2012) offered a novel way to create a lightweight sandwich-reinforced concrete segment using lightweight concrete. For example, concrete structures can use lightweight sandwich-reinforced concrete profiles as beams or slabs. Naji et al. (2015) developed an overall equation for deflecting a braced sandwich panel under a transverse load. The formulated equation contains all of the core mechanical properties. To design the precast concrete sandwich wall panel, methods for estimating flexure and stresses were developed and validated. The anticipated calculations enable geometric sizes, core shear mechanical properties, and parametric evaluations without reinforcements. EzzatFahmy et al. (2014) presented the findings of a study enhancing reinforced concrete beams including precast permanent U-shaped reinforced mortar methods filled with modified core materials as a substitute for traditional reinforced concrete beams.

## **Research significance**

The proposed solution could efficiently provide a better approach for structural designers to calculate flexure, shear, the equivalent modulus of elasticity, the effective moment of inertia, and deflection for composite sections. Additionally, the proposed analytical solution can provide a better approach for engineers to analyze and design composite sections without resorting to 3D finite element analysis, which is time-consuming.

## Methods

#### Definition of the problem and formulation

The composite section comprises reinforced concrete with autoclaved aerated concrete (AAC) block infill. It was found that



the strain of reinforced concrete equals the strain of autoclave aerated concrete at ACI 523.4R-09 [6]. The theoretical approach to the computation used in the research of the equilibrium equations determines the location of the neutral axis of the composite section, which is divided into two parts as follows. The first part is when the depth of the equivalent compression zone (*a*) is less than the depth of the concrete above the autoclave aerated concrete ( $t_c$ ), as shown in Figure 1. Figure 1 also shows the strain and stress distribution over the entire section. The internal forces in the reinforced concrete and reinforcing bars are shown in Figure 2 for the equilibrium equation. The second part is when the depth of the compression zone (*a*) is bigger than the depth of the concrete above the autoclave aerated concrete ( $t_c$ ), as in Figure 3. In Figure 4, for the equilibrium equation, the internal forces in the reinforced concrete, reinforcing bars, and AAC are depicted.

# The computational analysis of flexure

The equilibrium of the forces should be applied to analyze each section. The internal forces in the section are the compression concrete force and compression steel force equal to the tension steel force in Eq. 4. Once the location of the neutral axis is determined and the internal forces are determined, the ultimate moment on the composite section  $(M_u)$  can be calculated by





examining a moment when the point of application of the tension force occurs as follows:

T

$$C = T, (1)$$

$$C = C_s + C_c, \tag{2}$$

$$C = 0.85 f'_{cu} b a + A'_{s} f'_{y}, \qquad (3)$$

$$=A_{s}f_{y}, \qquad (4)$$

$$M_{u} = 0.85 f'_{cu} b a \left( d - \frac{a}{2} \right) + f'_{y} A_{s}' \left( d - d' \right).$$
 (5)

Another part is when the depth of the compression zone (*a*) is bigger than the depth of the concrete above the autoclave aerated concrete ( $t_c$ ), as in Figure 3. The internal forces in the reinforced concrete, reinforcing bars, and AAC are shown in Figure 4 for the equilibrium equation.

when  $t_c < a$ , the neutral axis is inside the AAC. It was determined that the strain of concrete equals the strain of the autoclaved aerated concrete at ACI 523.4R-09 [6]. The equilibrium equations can be derived as follows:

The equilibrium of forces should be applied to analyze the section. The internal forces in the section are the compression concrete force, the compression AAC force, and the compression steel force that is equal to the tension steel force in Eq. 14. Once the location of the neutral axis is determined and the internal forces are determined by Eq. 14, the stress block distance *a* is calculated as the equilibrium of the forces by Eq. 15, and the ultimate moment on the composite section  $(M_u)$  can be calculated by considering the application point of the tension force by Eq. 17 as follows:

$$C = T,$$
 (6)

$$C = C_1 + C_2 + C_4 + C_3 + C_s, (7)$$

$$T = A_s f_y, \tag{8}$$

$$C_{1} = (t_{c} + t_{1}) 0.85 f_{cu \ concrete} b_{web}, \tag{9}$$

$$C_{2} = (l_{c} + l_{1}) 0.85 f_{cu \ concrete} b_{web}, \tag{10}$$

$$C_{i} = 0.85 f'_{cu_{concret}} t_{AAC} t_{c}, \qquad (11)$$

$$C_4 = 0.00 \int c_{UAAC} c_1 O_{AAC}, \qquad (12)$$

$$C_{S} = A_{s} f_{y}, \tag{13}$$

$$t_{C} + t_{1}) 0.85 f_{cuconcrete} b_{web} + (t_{C} + t_{1}) 0.85 f_{cuconcrete} b_{web} + 0.85 f_{cuconcret} b_{AAC} t_{C} + 0.85 f_{cu_{AAC}} t_{1} b_{AAC} + A_{s} f_{y} = A_{s} f_{y},$$
(14)

where *C* represents the compression force above the neutral axis, *T* represents the tension force beneath the neutral axis, *A<sub>S</sub>* is the cross-sectional area of the tension reinforcement,  $f_y$  is the yield strength of the reinforcing steel,  $t_c$  is measured at the top fiber R.C. above AAC,  $t_1$  is the depth top of AAC above the neutral axis,  $f_{ci}$  is the compression strength of R.C.,  $f_{cu_{AAC}}$  is the compression strength of AAC,  $b_{AAC}$  is the width of the cross section AAC,  $A'_S$  is the cross-sectional area of the compression reinforcement, and  $f'_y$  is the yield strength of the steel. Furthermore, when assuming the dimensions of the composite section, the value of  $t_1$  is obtained from the previous equations.

$$a = t_c + t_1, \tag{15}$$

$$c = 1.25 a,$$
 (16)





where (a) is the depth of the stress block, and (c) is the depth of the neutral axis at the maximum compression

$$M_{u} = C_{1}\left(d - \frac{a}{2}\right) + C_{2}\left(d - \frac{a}{2}\right) + C_{3}\left(d - \frac{t_{c}}{2}\right) + C_{4}\left(d - t_{c} - \frac{t_{1}}{2}\right) + C_{s}\left(d - d'\right).$$
(17)

Design of the shear in the composite section

Calculating the shear of the composite section was conducted in three parts as follows: the first part is the design of the shear of a solid beam. The ACI 318 requires that the allowable shear stress resisted by concrete only is given by Eq. 18, and the calculation of the shear stress carried by the steel stirrup is given in Eq. 19. Hence, the ultimate shear strength in Eq. 20 is as follows:

$$q_{cu_{cracked}} = \frac{1}{6} \sqrt[2]{f'_{cu}}$$
(18)

$$q_{su} = q_u - q_{cu_{cracked}},\tag{19}$$

$$Q_1 = (q_{cu} + q_{su}) b d.$$
 (20)

The second part determines the shear strength of the section with void chambers, as in Eq. 21.

$$Q_2 = q_{cu} [(bd) - (b_{AAC} d_{AAC})].$$
(21)

The third part determines the shear stress of the autoclaved aerated concrete (AAC) section according to ACI 523.4R-09 ACI (2009) by Eq. 22 and the shear strength of the AAC section by Eq. 23.

$$q_{AAC} = 0.75 \ 0.85 \ \sqrt[2]{f_{AAC}},$$
 (22)

$$Q_3 = q_{AAC} \, b_{AAC} \, d_{AAC}. \tag{23}$$

Based on the three parts mentioned previously, the shear strength of the composite section is calculated using Eq. 24, as determined by the author, considering the ratio between the length of the concrete gaps between blocks AAC and the length of the blocks AAC at the longitudinal section.

$$Q_{composite} = Q_1 \frac{L_{cu}}{L_{AAC}} + Q_2 + Q_3, \qquad (24)$$

Model	Type of core material	Reinforcing steel bars			Depth of compression concrete $(t_c)$	Weight reduction
		Tens	Comp	Stirrups		
1	Solid concrete	2 Ø 20	2 Ø 6	5 Ø 6/m		
2	Solid concrete	2 Ø 20	2 Ø 6	5 Ø 10/m		
3	Infill AAC	2 Ø 20	2 Ø 6	5 Ø 6/m	60 mm	22.4%
4	Infill AAC	2 Ø 20	2 Ø 6	5 Ø 10/m 1,010/m	60 mm	22.4%
5	Infill AAC	2 Ø 20	2Ø6	5 Ø 6/m	0	29.8%
6	Infill AAC	2 Ø 20	2 Ø 6	5 Ø 10/m	0	29.8%
7	Infill AAC	2 Ø 20	2Ø6	5 Ø 10/m	30 mm	26.1%
8	Infill AAC	2 Ø 20	2 Ø 6	5 Ø 10/m	40 mm	24.8%
9	Infill AAC	2 Ø 20	2 Ø 6	5 Ø 10/m	50 mm	23.6%
10	Infill AAC	2 Ø 20	2 Ø 6	5 Ø 6/m	70 mm	21.15%
11	Infill AAC	2 Ø 20	2 Ø 6	5 Ø 6/m	80 mm	19.4%
12	Infill AAC	2 Ø 20	2Ø6	5 Ø 6/m	90 mm	18.6%
13	Infill AAC	2 Ø 20	2 Ø 6	5 Ø 6/m	100 mm	17.4%
14	Infill AAC	2 Ø 20	2 Ø 6	5 Ø 6/m	110 mm	16.18%

#### TABLE 1 Details of all the beams.

#### TABLE 2 Properties of the materials (Wahyuni, 2012).

Property	Concrete	Steel reinforcement	AAC
Compressive strength $f_{cu}$ Mpa	43		3.5
Modulus of elasticity $(E_{cu})$ Mpa	32,000	200,000	8,000
Poisson's ratio	0.2	0.3	0.2
Density kN/m3	25	75.5	5.3

where  $L_{cu}$  is the length of the concrete gaps between the AAC blocks, and the  $L_{AAC}$  is the length of the AAC blocks.

#### Deflection of the composite section

The calculation of the deflection of the composite section is divided into two parts as follows: the first part calculates the equivalent modulus of elasticity of the composite section, and the second part calculates the effective moment of inertia of the composite section.

# The first part: Computational calculation of the equivalent modulus of elasticity

It was determined that the strain of reinforced concrete equals the strain of autoclave aerated concrete at ACI 523.4R-09 [6]. Based on Hook's law mentioned as follows, the equivalent modulus of elasticity of the composite section was computed using Eq. 31 and determined by the author.  $E = \frac{\sigma}{s},$  (25)

$$E_{composite} \neq E_{cu} + E_{AAC}, \tag{26}$$

$$\varepsilon_{composite} = \varepsilon_{cu} = \varepsilon_{AAC},$$
 (27)

$$\sigma = \frac{P}{4},\tag{28}$$

$$P_{composite} = P_{cu} + P_{AAC},$$
(29)

$$\sigma_{composite} A_{composite} = \sigma_{cu} A_{cu} + \sigma_{AAC} A_{AAC}, \qquad (30)$$

$$E_{composite} = E_{cu} \frac{A_{cu}}{A_{composite}} + E_{AAC} \frac{A_{AAC}}{A_{composite}} + E_{cu} \frac{L_{cu}}{L_{AAC}},$$
 (31)

where *E* is the modulus of elasticity,  $A_{composite}$  is the area of the composite section,  $A_{cu}$  is the area of the concrete section,  $A_{AAC}$  is the area of the AAC section,  $L_{AAC}$  is the length of a block, and  $L_{cu}$  is the length of gaps between the blocks and concrete.

# The second part: Calculating the effective moment of inertia of the composite section

This model can also be used at the linear stage to evaluate the amount of composite behavior provided by the cross section, as





shown in Figure 5. The stress distribution across the composite section can be used to assess the effective moment of inertia  $I_e$  Concerning the computational calculation of the effective moment of inertia, the following equations are explained in the tension stress on the composite section and are divided into two tension stresses as follows: reinforced steel and tension stress by concrete. As for 1.5% fy and 2.5% fy, the tension stresses were obtained from ANSYS results, which showed a nearly linear relationship between tension stress and yield stress. The tension stress of steel equals 1.5%  $f_y$  when the compression strength of concrete is 30 Mpa, and the tension stress equals 2.5%  $f_y$  when the compression strength of strength of concrete is 50 Mpa. The effective moment of inertia in the composite section was computed using Eq. 32, as determined by the author.

$$I_e = M_{cr} \frac{(t-c)}{f_{ctr} + 0.025 f_y}.$$
 (32)

According to ECP 2018, the cracking moment is determined using the following formula:

$$M_{cr} = \frac{f_{ctr Ig}}{y},\tag{33}$$

where y is the distance from the neutral axis to the extreme fiber regarding the tension for the uncracked section,  $f_{ctr}$  is the concrete tensile strength (N/mm2), and  $I_g$  is the gross moment of inertia omitting the influence of reinforcement (mm4) and (mm). The concrete tensile strength  $f_{ctr}$  in the ECP 2018 is provided by

Model	Stirrup	Distance to the neutral axis from the top	is from P first crack Failure load							%	
		Of the beam (mm)									
		c mm	Exp kN [4]	ANSYS kN	Theo kN	Exp kN [4]	ANSYS kN	Theo moment kN	Theo shear kN	Failure load theo	ANSYS/ theo
(1)	5 Ø 6/m	57.3	20.5	17.5	14.33	78.9	77.5	84.4	81	81	95.68
(2)	5 Ø 10/m	57.3	0	17.5	14.33	0	81.85	84.4	122.5	84	97.44
(3)	5 Ø 6/m	57.3	0	15.5	12.6	0	67.6	84.5	65	65	104.00
(4)	5 Ø 10/m	57.3	23.3	15.5	12.6	78.6	78	84.5	90.3	84.5	92.31
(5)	5 Ø 6/m	184	0	11	10.25	0	27	70.9	31.3	31.3	86.26
(6)	5 Ø 10/m	184	0	11	10.25	0	27.163	70.9	33.5	33.5	81.08
(7)	5 Ø 10/m	80.83	0	13.5	11.6	0	53.3	88.2	59.3	59.3	89.88
(8)	5 Ø 10/m	58.6	0	13.5	11.97	0	60.5	83.3	55.7	55.7	108.62
(9)	5 Ø 10/m	72.15	0	13.5	12.3	0	64	84	57.2	57.2	111.89
(10)	5 Ø 6/m	57.3	0	15.5	12.88	0	69.5	84.5	63	63	110.32
(11)	5 Ø 6/m	57.3	0	15.5	13.125	0	70.5	84.5	65	65	108.46
(12)	5 Ø 6/m	57.3	0	15.5	13.33	0	71.5	84.5	67	67	106.72
(13)	5 Ø 6/m	57.3	0	15.5	13.5	0	73.25	84.5	69	69	106.16
(14)	5 Ø 6/m	57.3	0	15.5	13.68	0	73.5	84.5	71	71	103.52

TABLE 3 Comparison between the experimental [4], finite elements, and computational analysis at the first crack and failure load.

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Model	Stirrup	Modulus of elasticity				le			
		Exp [4]	ANSYS	Theo	Ansys/Theo	Exp [4]	ANSYS	Theo	Ansys/Theo
(1)	5 Ø 6/m	32,000	31,960.8	30,819.9	103.70	1.66 E+08	1.56 E+08	1.71 E+08	91.43
(2)	5 Ø 10/m		31,960.8	30,819.9	103.70		1.58 E+08	1.71 E+08	92.61
(3)	5 Ø 6/m		29,125.6	28,255.9	103.08		1.52 E+08	1.5 E+08	100.79
(4)	5 Ø 10/m	32,000	29,125.6	28,255.9	103.08	1.6 E+08	1.73 E+08	1.5 E+08	115.00
(5)	5 Ø 6/m		24,818.2	24,832.9	99.94		1.07 E+08	1.22 E+08	87.31
(6)	5 Ø 10/m		24,818.2	24,832.9	99.94		1.17 E+08	1.22 E+08	95.46
(7)	5 Ø 10/m		28,225.8	26,544.4	106.33		1.61 E+08	1.38 E+08	116.26
(8)	5 Ø 10/m		28,323.6	27,114.9	104.46		1.69 E+08	1.43 E+08	118.07
(9)	5 Ø 10/m		28,225.8	27,685.4	101.95		1.66 E+08	1.47 E+08	113.37
(10)	5 Ø 6/m		28,225.8	28,826.4	97.92		1.59 E+08	1.54 E+08	103.67
(11)	5 Ø 6/m		28,225.8	29,396.9	96.02		1.6 E+08	1.57 E+08	101.89
(12)	5 Ø 6/m		28,225.8	29,967.4	94.19		1.59 E+08	1.59 E+08	100.24
(13)	5 Ø 6/m		28,225.8	30,537.9	92.43		1.62 E+08	1.61 E+08	100.37
(14)	5 Ø 6/m		28,225.8	31,108.4	90.73		1.61 E+08	1.63 E+08	98.90

TABLE 4 Comparison results between the experimental, finite elements, and computational analysis at the modulus of elasticity and effective moment of inertia for all models.

TABLE 5 Results for the comparison between experimental, finite elements, and computational analysis at the deflection of all of the different models.

Model		%		
	Exp [4] mm	ANSYS mm	Theo mm	ANSYS/ Theo
(1)	15.4	12	11.9	100.8
(2)		12.5	13.5	92.6
(3)	17.6	11.9	11.8	100.8
(4)		12	13.6	88.2
(5)		8.2	8.0	102.5
(6)		7.5	8.6	87.2
(7)		9.17	9.5	96.5
(8)		9.9	11.1	89.2
(9)		10.6	10.9	97.2
(10)		12	11.0	109.1
(11)		12.15	10.9	111.5
(12)		12.33	10.9	113.1
(13)		12.45	10.9	114.2
(14)		12.51	10.8	115.8

$$f_{ctr} = 0.6\sqrt{fcu} N/mm^2, \tag{34}$$

$$I_g = \frac{bt^3}{12} + (n-1)\frac{b_{AAC}t^3_{AAC}}{12},$$
(35)

where n is the modular ratio and is given by

$$n = \frac{E_{AAC}}{E_{cu}},\tag{36}$$

$$y = \frac{t_{composite}}{2}.$$
 (37)

Figure 5 (Naji et al., 2015) shows the cracking of the concrete section under applied loads.

## Rustle

#### Validation of the proposed methods

Computational analysis of the composite sections explains the composite section of the beam and compares it with the finite element results conducted using ANSYS software. All beams had a rectangular cross section with a constant width and depth of 200 mm by 300 mm, respectively, with top and bottom longitudinal bars. The bottom bars were 20 mm, while the top bars were 6 mm, and the stirrup reinforcement was 6 mm and 10 mm. The bottom bars recorded a tensile yield strength of 560 Mpa. Top steel and stirrups recorded a tensile yield strength of 300 Mpa. The beam length was 3,000 mm with a 2,800 mm clear span, as shown in Figure 6. To consider the ability and capability of the concrete beam and infill beam modeling by applying the said techniques, an experimental test by Ade Sri Wahyuni [4] was modeled as the micro-sample. These authors have 12 models using AAC infill R.C., and the cross section of AAC blocks was  $180 \times 150$  mm, the gap between the AAC blocks and the concrete was 43 mm, and the reinforcement stirrups were 6 mm and 10 mm, as shown in Table 1.



# Schematic diagram of the study methodology

A scheme to explain the research methodology of the experimental, the finite elements, and the computational analysis and comparison between experimental, finite elements, and computational analysis as shown in Scheme 1.

#### Modeling the beams using ANSYS

The author used the ANSYS program to study the models. The ANSYS APDL program provides simulations of solid concrete elements with eight-node (solid65) at the command file at ANSYS APDL to connect ANSYS WORKBENCH as the solution, steel elements (180 link elements), and AAC solid elements with eight-node (solid65). The properties of the materials are shown in Table 2.

### The results of the ANSYS beams

Finite element analysis models were plotted to compare the failure load and deflection to the results, as shown in Figure 7.

### ANSYS WORKBENCH graphical output

The output of the ANSYS analysis model is obtained, as shown in Figure 8.

#### Results and discussion

The author determined the equations of the first crack, failure loads, flexure, and the dimensions of the compression zone from the first principles. The author also determined the equation of failed shear from the ECP 2018. Moreover, the comparison of the computational and finite element results is shown in Table 3. The table shows that the predicted results of the failure load were similar to the finite element for all models. The ratio of the computational calculation of failure loads shown by finite elements ranged from 0.89 to 1.1. The results show that the failure loads of the experimental and finite elements by ANSYS and computational calculation are slightly different from two other models (Farid et al., 2017, Al-Sherrawi, 2018). The experimental model (Farid et al., 2017) and the other model (Al-Sherrawi, 2018) failed at 78.9 kN and 78.6 kN, whereas the finite elements failed at 81.85 kN and 78 kN, and the computational calculation failed at 84 kN and 84 kN, respectively.

The author concluded that the equation of the equivalent modulus of elasticity from Hooke's law could be calculated. Moreover, the comparison of the computational and finite element results is shown in Table 4. The ratio of the computational calculation of the modulus of elasticity to the finite element ones ranged from 0.91 to 1.06.

An equation is presented for the effective moment of inertia and to calculate it in all sections. Moreover, a comparison of the computational and finite element results is shown in Table 4. The table demonstrates that the predicted outcomes of the effective moment of inertia are close to the finite element for all models. The ratio of the computational calculation of the effective moment of inertia to the finite element results ranged from 0.914 to 1.18.

The equation of the equivalent modulus of elasticity and the equation of effective moment of inertia were used to calculate the deflection of all models. Moreover, a comparison of the computational and finite element results is shown in Table 5. The ratio of the computational calculation deflection to the finite element results ranged from 0.87 to 1.15.

# Conclusion

In this study, an analysis of a composite section was proposed. Conceptual presumptions from the fundamental principles and Hook's law serve as the foundation for the solution. The findings were compared with the finite element using ANSYS results and conducted using ANSYS software to verify the suggested analytical approach, and excellent agreements were found. The suggested and precise solution offers a better method for structural designers to determine flexure, shear, the equivalent elastic modulus, the effective moment of inertia, and deflection for the composite section. Additionally, the suggested analytical solution has the benefit of offering designers a better method for analyzing and designing a failed at 81 kN and 84 kN.

composite section without conducting a time-consuming 3D finite element analysis. The equation is based on the first principle to calculate failure loads, flexure, and the depth of the compression zone. The computational, experimental, and finite elements based on ANSYS results were compared. The failure loads of the experimental and finite elements by ANSYS and theoretical calculations were obtained from the solid beam model (Farid et al., 2017) and R.C. beam infill AAC model (Wahyuni, 2012). It was determined that the experimental model (Farid et al., 2017) and other model (Wahyuni, 2012) failed at 78.9 kN and 78.5 kN, whereas the finite elements failed

- The ratio of the theoretical calculation of the first cracking loads compared to the finite element results ranged from 0.89 to 1.1.

at 77.5 kN and 78.5 kN; in contrast, the theoretical calculations

- The author concluded that the equation of the equivalent modulus of elasticity from Hooke's law was calculated. The ratio of the computational calculation of the modulus of elasticity to the finite element results ranged from 0.91 to 1.06.
- The equation with the author's effective moment of inertia was used to calculate all of the models' respective effective moments of inertia. The ratio of the theoretical calculation of the effective moment of inertia to the finite element results ranged from 0.92 to 1.18.
- The equation of equivalent modulus of elasticity and the equation of effective moment of inertia were used to calculate all models' respective deflections. The ratio of the computational calculation deflection to the finite element results ranged from 0.87 to 1.15.

#### Recommendations for further research

- A study should be conducted on the dimension between concrete and AAC blocks ratio in the LCSRC section.

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- A study should be conducted on the dimension between the  $L_{AAC}$  length of a block and the  $L_{cu}$  length of gaps between blocks and concrete at beams in the longitudinal direction.

## Data availability statement

The original contributions presented in the study are included in the article/supplementary material, and further inquiries can be directed to the corresponding author.

## Author contributions

MO conducted the analysis of the composite section that was proposed. Conceptual presumptions from the fundamental principles and Hook's law serve as the foundation for the solution. MA and HE-E used ANSYS software SA to study the portion of the study related to mathematics.

## **Conflict of interest**

The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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# Nomenclature

- a depth of a compression zone  $t_c$  depth of the concrete above the autoclave aerated concrete  $M_u$  ultimate moment on the composite section C compression force T tension force  $A_S$  cross-sectional area of tension reinforcement  $f_y$  yield strength of reinforcing steel  $t_c$  measured at top fiber R.C. above AAC  $t_1$  depth top AAC above the neutral axis  $f'_{cu}$  compression strength of R.C.  $f_{cu_{AAC}}$  compression strength of AAC  $b_{AAC}$  width of the cross section AAC  $A'_S$  cross-sectional area of compression reinforcement
- $f'_y$  yield strength of steel  $q_{cu_{cncked}}$  allowable shear stress resisted by concrete  $q_{su}$  shear stress carried by steel stirrup Q ultimate shear strength  $q_{AAC}$  shear stress of autoclaved aerated concrete E modulus of elasticity  $A_{composite}$  area of the composite section  $A_{cu}$  area of the concrete section  $A_{AAC}$  area of the AAC section  $L_{AAC}$  length of a block  $L_{cu}$  length of gaps between blocks and concrete  $I_e$  effective moment of inertia  $f_{ctr}$  concrete tensile strength  $I_g$  gross moment of inertia