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# Study of the isomeric yield ratio in the photoneutron reaction of natural holmium induced by laser-accelerated electron beams

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**Introduction:** An accurate knowledge of the isomeric yield ratio (IR) induced by the photonuclear reaction is crucial to study the nuclear structure and reaction mechanisms. <sup>165</sup>Ho is a good candidate for the investigation of the IR since the Ho target has a natural abundance of 100% and the residual nuclide has a good decay property.

**Methods:** In this study, the photoneutron production of <sup>164m, g</sup>Ho induced by laser-accelerated electron beams is investigated experimentally. The  $\gamma$ -ray spectra of activated Ho foils are off-line detected. Since the direct transitions from the <sup>164m</sup>Ho are not successfully observed, we propose to extract the IRs of the <sup>164m, g</sup>Ho using only the photopeak counts from the ground-state decay.

**Results:** The production yields of <sup>164m, g</sup>Ho are extracted to be  $(0.45 \pm 0.10) \times 10^6$  and  $(1.48 \pm 0.14) \times 10^6$  per laser shot, respectively. The resulting IR is obtained to be  $0.30 \pm 0.08$  at the effective  $\gamma$ -ray energy of 12.65 MeV.

**Discussion:** The present data, available experimental data, and TALYS calculations are then compared to examine the role of the excitation energy. It is found that besides the giant dipole resonance, the excitation energy effect also plays a key role in the determination of the IRs.

## KEYWORDS

isomeric yield ratio, photoneutron reaction, laser-accelerated electron beam, effective  $\gamma$ -ray energy, <sup>164m, g</sup>Ho

## 1 Introduction

Nuclear isomers have been widely studied due to their fascinating applications, including medical imaging (Habs et al., 2011; Pan et al., 2021), nuclear clocks (Peik et al., 2021), and nuclear batteries (Prelas et al., 2014). They still play a crucial role in various aspects of astrophysical nuclear reactions (Hayakawa et al., 2008; Zilges et al., 2022). In many nuclear reactions, the residual nuclei have isomeric states with narrow energy levels and relatively long half-lives. The isomeric cross-section or yield ratio (IR) of high-spin to low-spin states of the residual nucleus provides valuable information

about nuclear structure and reaction mechanisms, such as the transfer of angular momentum, the spin dependence of nuclear level density, the amelioration in  $\gamma$ -ray transition theory, and tests of different models (Naik et al., 2016; Rahman et al., 2020). In addition, the IR plays a key role in calculating the total production cross-section of the residual products when the production cross-section of one isomer is known in advance.

The excitation energy and angular momentum of incident particles can significantly affect the IR values of the residual products. The IRs have been studied in nuclear reactions induced by different incident particles, such as photon (Rahman et al., 2016), proton (Hilgers et al., 2007), neutron (Luo et al., 2014), and alpha (Kim et al., 2015). Compared to other particles, photons carry a smaller angular momentum of  $1\hbar$  or  $2\hbar$ . Furthermore, intense bremsstrahlung photons can be readily produced using radio-frequency (RF) electron accelerators. As a result, the photonuclear reactions seem to be a good tool to investigate the effect of the excitation energy on the IR. Kolev et al. (1995) deduced the experimental IRs of  $(\gamma, 3n)^{110m, g}\text{In}$ ,  $(\gamma, n)^{164m, g}\text{Ho}$ , and  $(\gamma, 3n)^{162m, g}\text{Ho}$  by a bremsstrahlung source with an end-point energy of 43 MeV. Thiep et al. (2011) determined the IRs of  $^{165}\text{Ho}(\gamma, n)^{164m, g}\text{Ho}$  and  $^{175}\text{Lu}(\gamma, n)^{174m, g}\text{Lu}$  reactions in the bremsstrahlung energy region from 14 to 25 MeV. Do et al. (2013) measured the IRs of  $^{164m, g}\text{Ho}$  and  $^{162m, g}\text{Ho}$  via  $^{165}\text{Ho}(\gamma, n)$  and  $^{165}\text{Ho}(\gamma, 3n)$  reactions in the bremsstrahlung energy region from 45 to 65 MeV. It is noticeable that the available IRs for the  $^{165}\text{Ho}(\gamma, n)^{164m, g}\text{Ho}$  reactions are still scarce. It particularly lacks experimental data in the energy region below 11 MeV. With the rapid development of high-intensity laser technology (Danson et al., 2019), laser-plasma interactions are used to study various nuclear phenomena (Schlenvoigt et al., 2008; Günther et al., 2022; Cao et al., 2023). Recently, the efficient production of nuclear isomers, including  $^{113m, 115m}\text{In}$  and  $^{93m}\text{Mo}$ , has been studied experimentally using the laser-accelerated electron beam ( $e^-$  beam) (Feng et al., 2022; Fan et al., 2023 under review).

In this study, we experimentally investigate the production of  $^{164m, g}\text{Ho}$  by laser-induced photoneutron reactions. The  $\gamma$ -ray spectra of the activated Ho foils are detected by an offline  $\gamma$ -ray spectrometry technique. Since the direct transitions from  $^{164m}\text{Ho}$  were not successfully observed, we propose to extract the ground and isomeric yields of  $^{164}\text{Ho}$  using only the photopeak counts from the ground-state decay. We should note that this approach differs from determining the counts of two photopeaks that directly characterize the isomeric and ground states. The IR value of  $^{165}\text{Ho}(\gamma, n)^{164m, g}\text{Ho}$  is obtained for a given excitation energy. The present and similar literature data on IRs are compared to examine the role of excitation energy. Furthermore, the cross-section and IR curves of the  $^{165}\text{Ho}(\gamma, n)^{164m, g}\text{Ho}$  reaction are calculated by the TALYS software to examine the compatibility of the theoretical model with the experimental data.

## 2 Experimental setup

The  $^{164m, g}\text{Ho}$  production experiment was performed on the XingGuang-III laser facility at the Laser Fusion Research Center in Mianyang. The experimental setup is schematically shown in Figure 1A. An intense laser pulse with a duration of  $\sim 0.8$  ps and energy of  $\sim 100$  J was focused by an  $f/2.6$  off-axis parabola (OAP)

mirror (Robbie et al., 2018) onto a supersonic gas jet with a well-defined uniform density distribution (Feng et al., 2022). In the first stage of the experiment, high-charge multi-MeV  $e^-$  beams were produced during the laser-gas interactions. An image plate (IP) stack with a central hole was used to measure the spatial distribution of the laser-accelerated  $e^-$  beam. It should be noted that the IP stack is composed of seven IPs, with each IP being stuck on a tantalum foil with a thickness of 0.5 mm. Meanwhile, an electron magnetic spectrometer (EMS) was placed downstream of the IP stack to accurately diagnose the energy of the  $e^-$  beam passing through the central hole of the IP stack. In the second stage of the experiment, a metal stack composed of Ta foil and stacked Ho foils was installed, and both the IP stack and EMS were uninstalled. The Ta foil is 2 mm thick, in which energetic bremsstrahlung photons are generated. The stacked Ho foils used for activation have 10 layers in total, with each layer having a thickness of 1 mm and a natural abundance of 99.99% (Inagaki et al., 2020). During the activation, the bremsstrahlung radiations irradiate the Ho foils, successfully triggering photoneutron reactions and then producing a large number of  $^{164m, g}\text{Ho}$ , as shown in Figure 1B. After the activation, the Ho foils are taken out from the target chamber of the XingGuang-III laser facility. The activation spectra are recorded using a high-purity germanium (HPGe) detector. The response of the HPGe detector has been well calibrated by standard  $\gamma$ -ray sources, including  $^{60}\text{Co}$ ,  $^{152}\text{Eu}$ ,  $^{133}\text{Ba}$ ,  $^{226}\text{Ra}$ ,  $^{137}\text{Cs}$ , and  $^{241}\text{Am}$ . In order to reduce the self-absorption effect induced by the stacked Ho foils, the 10 layers are spread out at the surface of the Al window of the HPGe detector.

## 3 Isomeric yield ratio determination

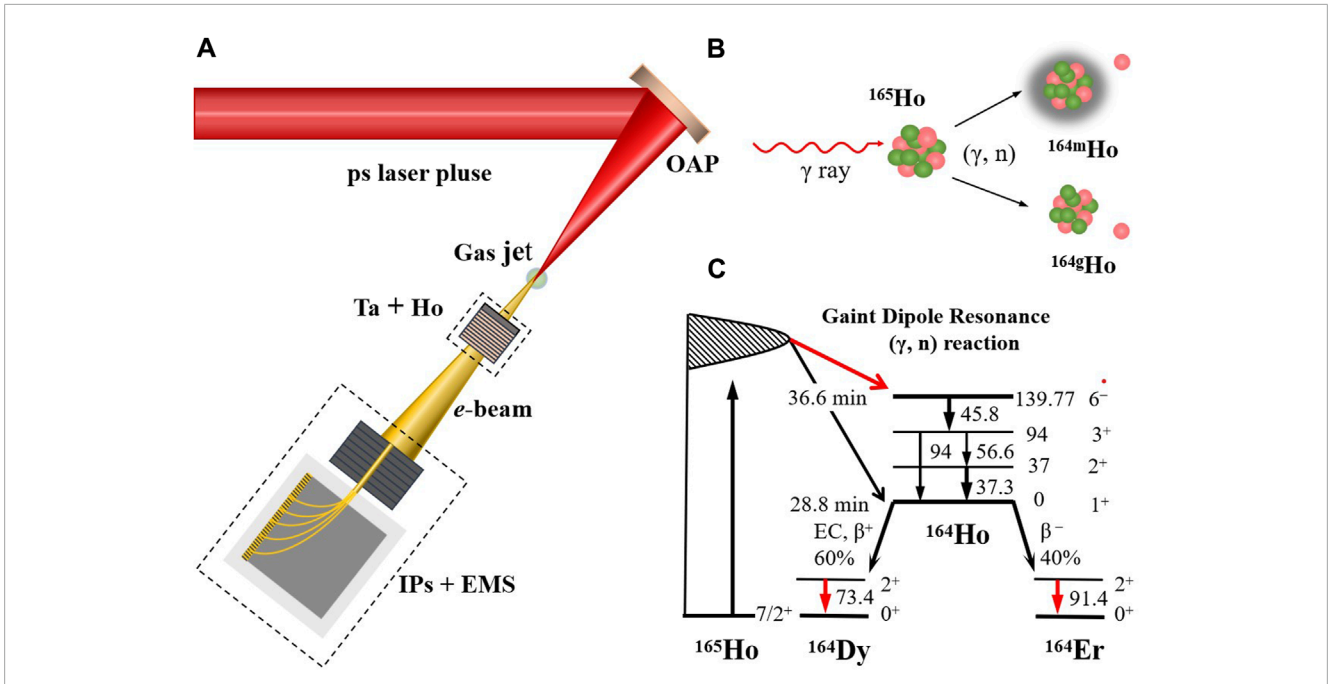
The temporal evolution of the numbers of nuclei that are formed in the isomeric and ground states is described by the following kinetic equations (Thiep et al., 2011):

$$\begin{cases} \frac{dN_m}{dt} = p_m - \lambda_m N_m, \\ \frac{dN_g}{dt} = p_g + \eta \lambda_m N_m - \lambda_g N_g, \end{cases} \quad (1)$$

where the subscripts  $m$  and  $g$  designate the isomeric and ground states of  $^{164}\text{Ho}$ , respectively;  $p_m$  and  $p_g$  are the production rates leading to  $^{164}\text{Ho}$  in the isomeric and ground states;  $N_m$  and  $N_g$  are the numbers of nuclei in the corresponding states;  $\lambda_m$  and  $\lambda_g$  are the constants of nuclear decay; and  $\eta$  is the transition coefficient from the isomeric state to the ground state. These equations describe the processes involved in the direct production of the desired isotopes during the target irradiation and the reduction of the number of nuclei as a result of their radioactive decay. The production rate  $p_x$  with  $x$  being the subscript  $m$  or  $g$  (similarly hereinafter) can be written as (Kolev et al., 1995)

$$p_x = N_0 \int_{E_{th}}^{E_{max}} \varphi(E_\gamma) \sigma_x(E_\gamma) dE_\gamma = N_0 \Phi \langle \sigma_x \rangle, \quad (2)$$

where  $N_0$  is the number of target nuclei,  $\varphi(E_\gamma)$  represents the bremsstrahlung photon flux;  $\sigma_x(E_\gamma)$  is the reaction cross-section leading to the formation of  $^{164}\text{Ho}$  in both the isomeric and ground states;  $E_{th}$  and  $E_{max}$  are the reaction threshold and bremsstrahlung end-point energy, respectively;  $\Phi = \int_{E_{th}}^{E_{max}} \varphi(E_\gamma) dE_\gamma$  is the integrated



**FIGURE 1** Experimental setup for the production of  $^{164m,9}\text{Ho}$  at the XingGuang-III laser facility (not to scale) (A). Schematic view of the photoneutron production of  $^{164m,9}\text{Ho}$  (B) and the partial-level scheme of  $^{164m,9}\text{Ho}$  and the decay property of  $^{164g,9}\text{Ho}$  (not to scale) (C). As the laser-accelerated  $e^-$  beam fires to the metal stack (Ta + Ho), a large number of bremsstrahlung photons are generated, and subsequently, the Ho stacks are activated via photoneutron reactions, producing  $^{164}\text{Ho}$  in both the ground state ( $J^\pi = 1^+$ ) and isomeric state ( $J^\pi = 6^-$ ) (Singh et al., 2018). The  $6^-$  isomer in  $^{164}\text{Ho}$  decays, via only internal decay, to the ground state. The decay from the  $6^-$  isomer to the  $3^+$  excited state is an E3 transition. This  $3^+$  excited state subsequently de-excites to the ground state. The resulting transition energies are 94.0, 56.6, and 37.3 keV. Finally, the ground-state decays to the daughter nucleus  $^{164}\text{Dy}$  or  $^{164}\text{Er}$ , emitting two characteristic  $\gamma$ -rays at 73.4 and 91.4 keV.

photon flux; and  $\langle \sigma_x \rangle = \int_{E_{th}}^{E_{max}} \varphi(E_\gamma) \sigma_x(E_\gamma) dE_\gamma / \int_{E_{th}}^{E_{max}} \varphi(E_\gamma) dE_\gamma$  is the flux-weighted average cross-section leading to the isomeric or ground state.

Since the gamma spectroscopy method is used in the experiment, the photopeak counts ( $C_x$ ) of the characteristic  $\gamma$ -ray of interest can be readily obtained over the detection time  $t_d$ . When taking into account the irradiation time  $t_{irr}$  and the cooling time  $t_c$ , the solution of Eq. 1 in three time intervals ( $t_{irr}$ ,  $t_c$ , and  $t_d$ ) and the consequent integration of the relevant activity over the  $t_d$  lead to

$$C_m = I_m \epsilon_m A p_m, \tag{3a}$$

$$C_g = I_g \epsilon_g (B p_g + D p_m), \tag{3b}$$

where  $I_x$  and  $\epsilon_x$  are the branching intensity and source-peak detection efficiency of the characteristic  $\gamma$ -rays to be detected, respectively. The other variables are listed as follows:  $A = \frac{1}{\lambda_m} (1 - e^{-\lambda_m t_{irr}}) e^{-\lambda_m t_c} (1 - e^{-\lambda_m t_d})$ ,  $B = \frac{1}{\lambda_g} (1 - e^{-\lambda_g t_{irr}}) e^{-\lambda_g t_c} (1 - e^{-\lambda_g t_d})$ , and  $D = \frac{\eta}{\lambda_g - \lambda_m} \left[ \frac{\lambda_g}{\lambda_m} (1 - e^{-\lambda_m t_{irr}}) e^{-\lambda_m t_c} (1 - e^{-\lambda_m t_d}) - \frac{\lambda_m}{\lambda_g} (1 - e^{-\lambda_g t_{irr}}) e^{-\lambda_g t_c} (1 - e^{-\lambda_g t_d}) \right]$ .

In the case of the bremsstrahlung photon, the expression of the IR reads (Jonsson et al., 1977) as follows:

$$IR = \frac{\langle \sigma_m \rangle}{\langle \sigma_g \rangle} = \frac{p_m}{p_g}. \tag{4}$$

Usually, the IR in a nuclear reaction is determined by measuring the counts of photopeaks that characterize the isomeric and ground

states, respectively. When one or more photopeaks induced by the isomeric state are directly detected, the  $p_x$  and the resulting IR values can be readily obtained by solving Eq. 3 and Eq. 4, respectively (Rahman et al., 2020). In the case of the Ho sample, the photopeak at 37.3 keV is popularly used to characterize the isomeric state, while that at 73.4 and 91.4 keV is used to characterize the ground state, as shown in Figure 1C. In our experiment, the 37.3 keV photopeak was not successfully observed. This is because only single-shot irradiation is performed, and both the  $\sigma_m$  and  $\epsilon_m$  values are relatively small. As a result, the abovementioned approach used to extract the IR value becomes invalid. It is shown in Eq. 3b that both the isomeric and ground states contribute to the  $C_g$  value, which varies with the  $t_d$ . It suggests that the  $p_x$  values can also be obtained by solving only Eq. 3b at two different time instants. More specifically, the  $p_x$  values can be deduced by solving the simultaneous equations of Eq. 3b at  $t_d^i$  and  $t_d^j$ , with  $i$  and  $j$  denoting two arbitrary time instants.

$$\begin{cases} p_g = \frac{D_j Y_i - D_i Y_j}{B_i D_j - B_j D_i}, \\ p_m = \frac{B_i Y_j - B_j Y_i}{B_i D_j - B_j D_i}, \end{cases} \tag{5}$$

where  $Y_i = C_g^i / I_g \epsilon_g$ . This indicates that using only the photopeak counts from the ground-state decay, the IR value can be obtained. Furthermore, a group of data on IR can be obtained by reasonably changing the time increments. According to the error propagation, the uncertainties of the  $p_x$  values can be determined by the following

formula:

$$\begin{cases} \sigma(p_g) = \sqrt{\frac{D_j^2 \sigma(Y_i)^2 + D_i^2 \sigma(Y_j)^2}{(B_i D_j - B_j D_i)^2}}, \\ \sigma(p_m) = \sqrt{\frac{B_i^2 \sigma(Y_j)^2 + B_j^2 \sigma(Y_i)^2}{(B_i D_j - B_j D_i)^2}}. \end{cases} \quad (6)$$

As a result, the uncertainty of the IR value can be written as

$$\sigma(IR) = IR \sqrt{\frac{\sigma(p_g)^2}{p_g^2} + \frac{\sigma(p_m)^2}{p_m^2}}. \quad (7)$$

## 4 Results and discussion

### 4.1 Electron spectra

In our experiment, high-energy electrons are mainly produced by the parametrically enhanced direct laser acceleration (Cao et al., 2023). As the electron yield and charge are sensitive to the plasma density, the  $e^-$  beam generation can be optimized by adjusting the backing pressure of the gas jet. Figure 2A shows the energy distributions of truncated  $e^-$  beams recorded by the EMS at two backing pressures of 2.0 and 2.6 MPa. The spectral pattern of the  $e^-$  beam can be described by a Boltzmann distribution  $\frac{dN}{dE} \propto e^{-\frac{E}{T_e}}$ , where the  $T_e$  is the slope temperature (Qi et al., 2019). The fitting results show that the  $T_e$  values are 7.8 MeV and 4.8 MeV for backing pressures of 2.0 MPa and 2.6 MPa, respectively. In addition, the charge of the laser-accelerated electrons higher than 1 MeV is  $Q_e \sim 42$  nC at 2.0 MPa, which is 2.5 times higher than that at 2.6 MPa. The spatial distribution of the  $e^-$  beam is shown in Figure 2B. It is visibly seen that a bright spot is located beneath the central hole. According to the experimental arrangement and the spot size of the  $e^-$  beam, the laser-accelerated  $e^-$  beam has an angular divergence of approximately 200 mrad (FWHM).

Generally, only high-energy electrons can be used to induce isomer production. However, the bright electron spot is located beneath the central hole, as shown in Figure 2B. This suggests that most of the electrons with high energy did not pass through the central hole of the IP stack and were not recorded by the EMS in our experiment. To understand more about the spectral pattern of the laser-accelerated  $e^-$  beam, we utilized the Geant4 toolkit (Agostinelli et al., 2003) to simulate the attenuation of monoenergetic electrons inside the IP stack. For a given energy, when the number of incident electrons reduces by a factor of 0.9, such energy is regarded as the minimum energy recorded by each IP. Then, the spectral distribution of the  $e^-$  beam can be figured out but with a relatively large uncertainty. Similar studies have been conducted by Bonnet et al. (2013) and Nishiuchi et al. (2020). Figure 2C shows the simulated electron spectral distribution, which matches well with the Boltzmann distribution. Note that the uncertainty represents the detectable energy range for each IP. The slope temperature is fitted to be 16.2 MeV, which is two times higher than the one recorded by the EMS. This is because the bright  $e^-$  beam was not centered with the hole on the IP stack so that the EMS only detected the low-energy part of the  $e^-$  beam, as presented earlier.

Since the slope temperature is sufficiently high, such an  $e^-$  beam interacting with a Ta foil can generate a high flux of bremsstrahlung radiation.

### 4.2 Characteristic $\gamma$ -ray spectrum

The characteristic  $\gamma$ -rays emitted from the Ho sample were measured with the HPGe detector, as mentioned earlier. In our case, the cooling time  $t_c$  is 30 min. Figure 3A shows the measured characteristic  $\gamma$ -ray spectra for  $t_d = 240$  min, from which two photopeaks at 73.4 keV ( $I_g = 1.88\%$ ) and 91.4 keV ( $I_g = 2.30\%$ ) are clearly observed, whereas the 37.3 keV  $\gamma$ -ray for  $^{164m}\text{Ho}$  does not appear. This is because the amount of  $^{164m}\text{Ho}$  produced during a single-shot irradiation was not enough to be detectable after the cooling time of 30 min. However, the signal and background counts around the  $\gamma$ -ray energy at 37.3 keV can be used to safely determine an upper limit for the yield of  $^{164m}\text{Ho}$ . By integrating over the energy region of the characteristic  $\gamma$ -ray at 37.3 keV, the signal and background counts are 242, which gives an upper limit of  $0.85 \times 10^6$  for the  $^{164m}\text{Ho}$  yield according to Eq. 3a.

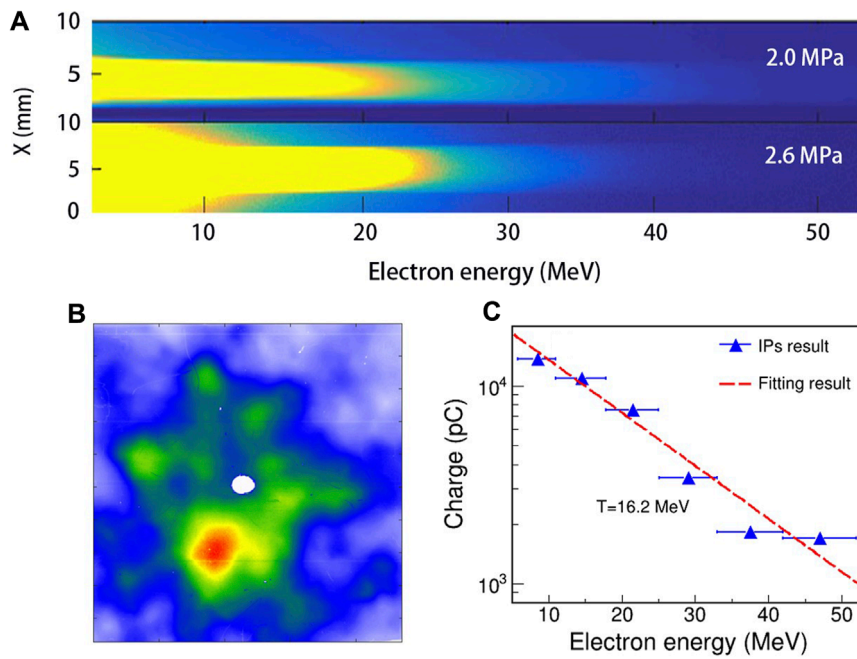
As mentioned previously, reasonably partitioning the  $C_g$  is vital to obtain the  $p_x$  and the resulting IR. The  $C_g$  values for 73.4 and 91.4 keV lines as functions of  $t_d$  are shown in Figure 3B. The temporal variation of  $C_g$  can be fitted well with Eq. 3b. The fitting curve can be re-written as

$$C_g = P_0 e^{-\lambda_g t_d} + P_1 e^{-\lambda_m t_d} + P_2, \quad (8)$$

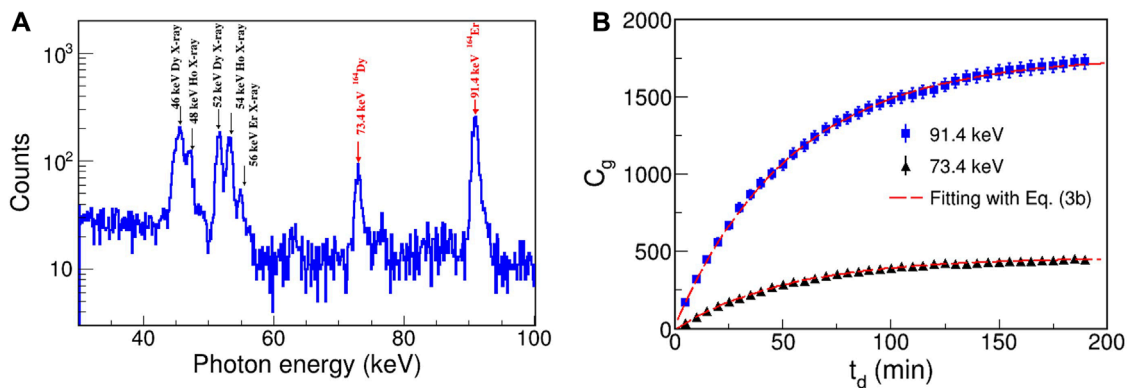
where  $P_0$ ,  $P_1$ , and  $P_2$  are the coefficients dependent on the  $p_x$ . More specifically, the coefficients  $P_0$  and  $P_2$  are associated with both the  $p_m$  and  $p_g$ .  $P_1$  is the function of  $p_m$ . From Eq. 8, one can see that the  $C_g$  value is not only contributed by the ground state of  $^{164}\text{Ho}$  but also induced by its isomeric state. In our case, the  $P_1$  is fitted to be  $-1865 \pm 229$ , and the  $p_m$  value is then obtained to be  $(0.44 \pm 0.05) \times 10^6$ . The resulting confidence level is approximately 9.0  $\sigma$ .

### 4.3 Isomeric ratio calculation

The calculation of the IR relies on the determination of  $p_m$  and  $p_g$ . Since the characteristic  $\gamma$ -ray line at 37.3 keV is not observed in our case, we employ the approach shown in Eq. 5 to extract the  $p_x$  values of  $^{164m,g}\text{Ho}$ . Figure 4A presents 10 groups of  $p_x$  values obtained with the photopeak counts at 91.4 keV. The average  $\overline{p_m}$  and  $\overline{p_g}$  are calculated to be  $0.45 \times 10^6$  and  $1.48 \times 10^6$  per laser shot, respectively. The uncertainty of  $p_x$  is determined by  $\sigma(p_x) = \sqrt{\sum_{i=1}^n \sigma_i^2(p_x)}/n$ , where the  $\sigma_i(p_x)$  is the uncertainty of  $p_x^i$  calculated by Eq. 6. Finally, the  $p_m$  and  $p_g$  of Ho produced in the experiment are obtained to be  $(0.45 \pm 0.10) \times 10^6$  and  $(1.48 \pm 0.14) \times 10^6$  per laser shot, respectively. Accordingly, the confidence level of  $p_m$  is 4.5  $\sigma$ . It should be noted that the  $p_m$  value is in good agreement with the one obtained by fitting the  $C_g$  curve, as discussed earlier. However, its confidence level is smaller than the confidence level of  $P_1$ . This is reasonable since the former reasonably considers the error propagation. In addition, the  $p_m$  value is almost two times lower than the upper limit of  $0.85 \times 10^6$  mentioned earlier, which in turn validates the feasibility of extracting the  $^{164m}\text{Ho}$  yield using only the



**FIGURE 2** Spectral distributions of the laser-accelerated  $e^-$  beam diagnosed by the EMS (A), spatial distribution of the laser-accelerated  $e^-$  beam recorded at the backing pressure of 2.0 MPa (B), and the electron charge in dependence on the electron energy (C).

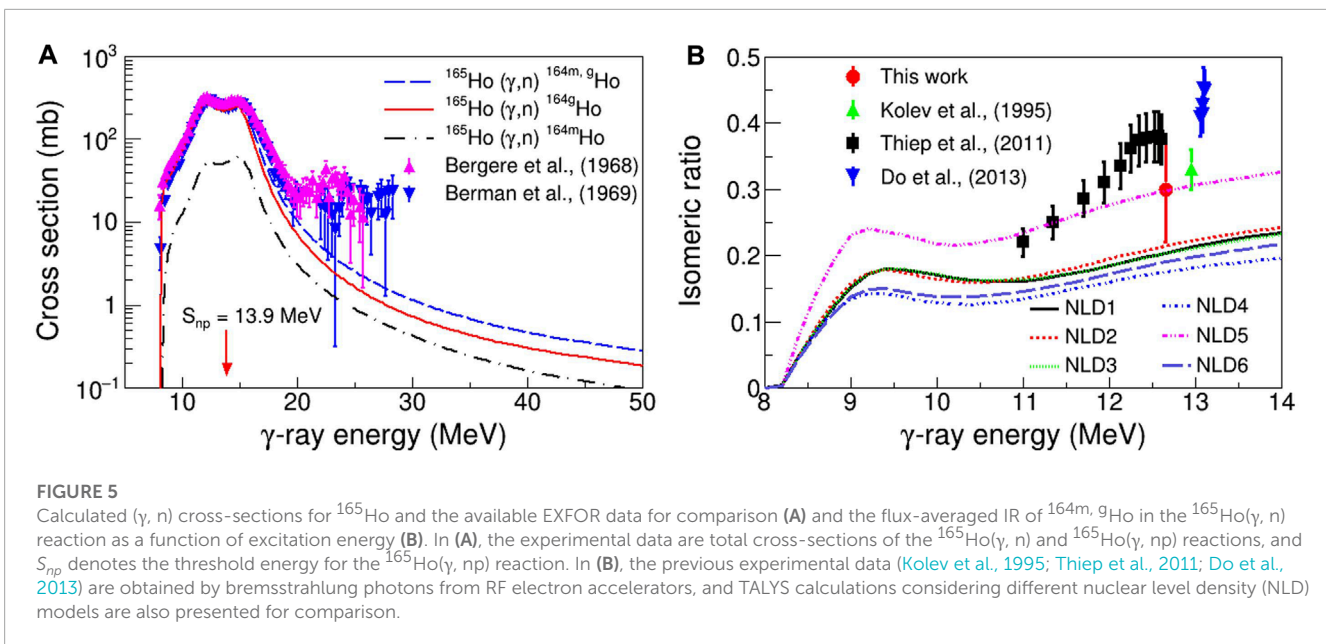
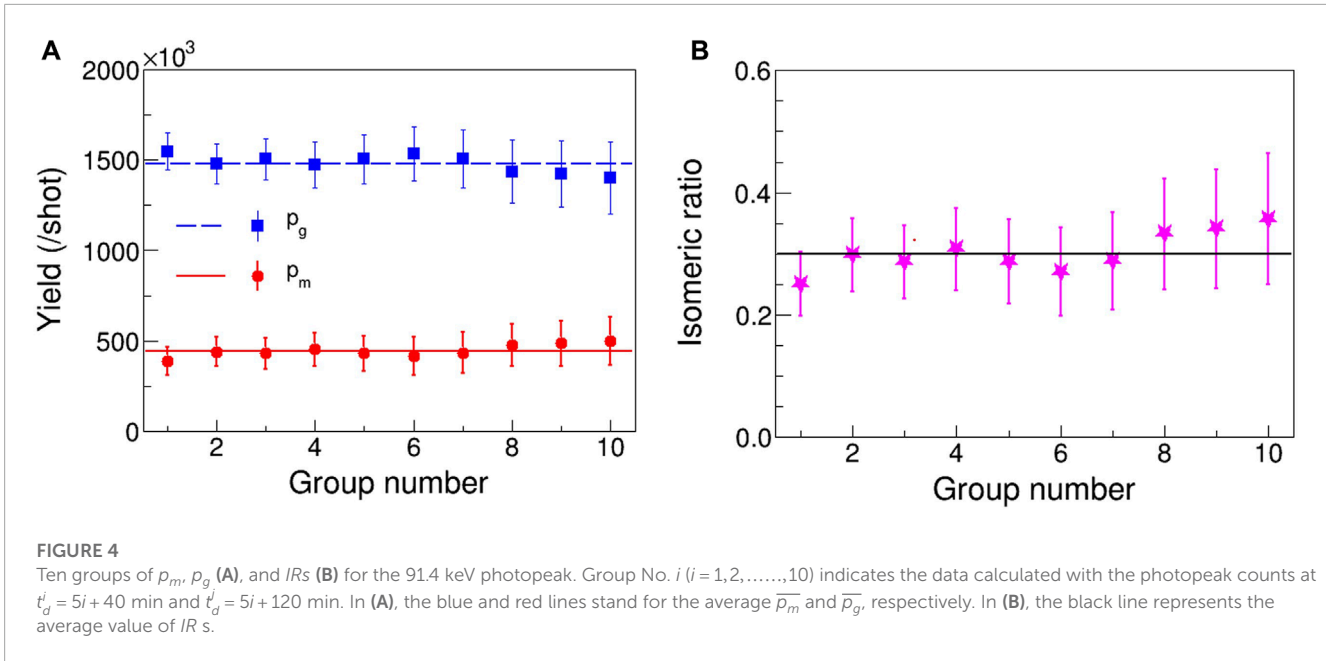


**FIGURE 3** Typical  $\gamma$ -ray spectrum from the activated Ho foils ( $t_c = 30$  min and  $t_d = 240$  min) (A) and accumulated photopeak counts as a function of detection time (B).

peak counts from the ground-state decay. Similarly, the  $IR$  value and its uncertainty  $\sigma(IR)$  are calculated with Eq. 4 and 7, respectively. Figure 4B shows 10 groups of  $IR$ s and their average value. The  $IR$  value of  $^{164m}\text{gHo}$  is  $0.30 \pm 0.08$ , which is less than unity. This is because the spin ( $J = 6$ ) of the isomeric state is visibly higher than the ground state with  $J = 1$ .

Photoneutron reaction cross-section of  $^{165}\text{Ho}$  calculated with TALYS 1.9 (Koning et al., 2019) and the data from the Experimental Nuclear Reaction Database (EXFOR) are compared and shown in Figure 5A. One can see that the  $^{165}\text{Ho}(\gamma, n)^{164}\text{gHo}$  reaction plays a dominant role in the giant dipole resonance (GDR) region. The  $^{165}\text{Ho}(\gamma, n)^{164m}\text{Ho}$  reaction has a similar distribution with the

$^{165}\text{Ho}(\gamma, n)^{164}\text{gHo}$ . However, its maximum cross-section,  $\sim 60$  mb, is visibly lower than that of the latter. As the photon energy continues to increase, the multiple emission reactions take over. The maximum cross-section decreases as the number of emitted particles increases. The TALYS calculations are in overall good agreement with the EXFOR data obtained from previous measurements using photon sources caused by positron annihilation in flight (Bergère et al., 1968; Berman et al., 1969). This indicates the reliability of the TALYS inputs and calculations. In addition, it is noticeable that the available experimental data in terms of isomer production are very rare, which can potentially be measured using state-of-the-art laser-Compton scattering facilities generating high-intensity and



quasi-monoenergetic  $\gamma$ -ray beams (An et al., 2018; Wang et al., 2022).

The IRs of  $^{164m,9}\text{Ho}$  can be examined by using different bremsstrahlung radiations from both the laser-plasma accelerator and the RF accelerator. For this purpose, the effective  $\gamma$ -ray energy  $\langle E_\gamma \rangle$  from the threshold to the end-point energy can be obtained by using the following relation (Jacobs et al., 1979):

$$\langle E_\gamma \rangle = \frac{\int_{E_{th}}^{E_{max}} \varphi(E_\gamma) \sigma_R(E_\gamma) E_\gamma dE_\gamma}{\int_{E_{th}}^{E_{max}} \varphi(E_\gamma) \sigma_R(E_\gamma) dE_\gamma}, \quad (9)$$

where the  $\varphi(E_\gamma)$  is calculated with the Geant4 toolkit considering their realistic target arrangements, and  $\sigma_R(E_\gamma)$  is the cross-section for the  $^{165}\text{Ho}(\gamma, n)^{164m,9}\text{Ho}$  reaction, which is calculated by using the default option in the TALYS software. In order to understand the effect of excitation energy, the measured IR value of  $^{164m,9}\text{Ho}$  from the present work, literature values, and TALYS calculations are plotted in Figure 5B as a function of  $\langle E_\gamma \rangle$ . From the EXFOR data, one can see that when  $\langle E_\gamma \rangle > 11$  MeV, the IR of  $^{164m,9}\text{Ho}$  increases with the  $\langle E_\gamma \rangle$  and then gets saturated. This is because the input angular momentum brought in by photons is very low. Since the experimental data are not available within the energy range  $\langle E_\gamma \rangle < 11$  MeV, the IRs are further calculated with the TALYS software

considering different NLD models. It is found that the  $IR$  clearly depends on the  $\langle E_\gamma \rangle$ . The increasing and decreasing trends of the  $IR$  values appear within the energy range of  $8.5 < \langle E_\gamma \rangle < 11.0$  MeV. Such trends are not only due to the excitation energy effect but also due to the GDR effect. In our experiment, the  $IR$  value of  $^{164m, g}\text{Ho}$  is  $0.30 \pm 0.08$  at  $\langle E_\gamma \rangle = 12.65$  MeV, which is in agreement with both TALYS calculations and the data of Kolev et al. (1995) within the statistical uncertainty. However, the experimental  $IR$ s provided by Thiep et al. (2011) and Do et al. (2013) are higher than the TALYS calculations at  $\langle E_\gamma \rangle > 12$  MeV.

## 5 Conclusion

We carried out the experiment to produce  $^{164m, g}\text{Ho}$  via photon-neutron reaction induced by a laser-accelerated electron beam, in which the  $IR$  value of  $^{164m, g}\text{Ho}$  is determined by using the activation and offline  $\gamma$ -ray spectrometry technique. However, since the characteristic  $\gamma$ -rays from the isomeric decay of  $^{164m}\text{Ho}$  were not successfully observed, we propose to extract the production yields of  $^{164m, g}\text{Ho}$  by partitioning counts of photopeak characterizing the ground-state decay. This is different from the approach by extracting the counts of two photopeaks characterizing directly the isomeric and ground states. The production yields of  $^{164m, g}\text{Ho}$  were successfully extracted to be  $(0.45 \pm 0.10) \times 10^6$  and  $(1.48 \pm 0.14) \times 10^6$  per laser shot. Accordingly, the  $IR$  value is calculated to be  $0.30 \pm 0.08$  at  $\langle E_\gamma \rangle = 12.65$  MeV. The  $IR$  as a function of  $\langle E_\gamma \rangle$  is further calculated with the TALYS software considering different NLD models. It is found that our result is in agreement with both TALYS calculations and the available experimental data within the statistical uncertainty. In addition, the increasing and decreasing trends of the  $IR$  values are observed within the energy range of  $8.5 < \langle E_\gamma \rangle < 11.0$  MeV, suggesting that excitation energy is crucial to determine the  $IR$  value of  $^{164m, g}\text{Ho}$ .

## Data availability statement

The original contributions presented in the study are included in the article/Supplementary material; further inquiries can be directed to the corresponding authors.

## Author contributions

JZ: Data curation, Formal Analysis, Investigation, Software, Visualization, Writing—original draft. WQ: Data curation, Investigation, Resources, Writing—review and editing. WF:

Data curation, Visualization, Writing—review and editing. ZC: Data curation, Software, Writing—review and editing. KL: Data curation, Visualization, Writing—review and editing. CT: Software, Writing—review and editing. XZ: Resources, Writing—review and editing. ZD: Resources, Writing—review and editing. ZZ: Resources, Writing—review and editing. XL: Writing—review and editing. YY: Writing—review and editing. WL: Funding acquisition, Supervision, Writing—review and editing. WZ: Funding acquisition, Supervision, Writing—review and editing.

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## Conflict of interest

The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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## Appendix

The photopeak counts  $C_x$  ( $x = m, g$ ) is the integration of the Activity  $A_x$  for  $x$ -state considering  $I_x$  and  $\epsilon_x$  over a detection time  $t_d$  as follows:

$$C_x = \int_0^{t_d} I_x \epsilon_x A_x dt. \tag{A1}$$

As shown above, the activity  $A_x$  is the key factor in the  $C_x$  solution. According to Eq. 1 in the proof (on line 204), in irradiation interval, both the productions and the decay properties contribute to the activities of the isomeric and ground states. And in the cooling and the detection interval, only the decay properties of two states contribute to the activities. So, we deduce the activities of the isomeric and ground states for two intervals, i.e., the irradiation interval and the natural decay interval (including cooling interval and detection interval).

Firstly, the number of  $x$ -state  $N_x$  at the irradiation time  $t_{irr}$  can be solved out. In irradiation interval, the  $N_x$  changes as a function of  $t_{irr}$  and the formula is like to Eq. 1 in the proof. By solving the Eq. 1 in the proof, the  $N_x$  at the irradiation time  $t_{irr}$  can be obtained as:

$$N_m = \frac{1}{\lambda_m} P_m (1 - e^{-\lambda_m t_{irr}}), \tag{A2}$$

$$N_g = \eta P_m \frac{1}{\lambda_g (\lambda_g - \lambda_m)} (\lambda_g (1 - e^{-\lambda_m t_{irr}}) - \lambda_m (1 - e^{-\lambda_g t_{irr}})) + \frac{1}{\lambda_g} P_g (1 - e^{-\lambda_g t_{irr}}). \tag{A3}$$

And then, in the cooling and the detection intervals, the production doesn't do any contribution to the activities of the isomeric and ground states. Therefore, the Eq. 1 in the proof for the cooling and detection intervals can be written as:

$$\begin{cases} \frac{dN_m}{dt} = -\lambda_m N_m, \\ \frac{dN_g}{dt} = \eta \lambda_m N_m - \lambda_g N_g. \end{cases} \tag{A4}$$

By solving it, the  $N_x$  changes as a function of the cooling  $t_c$  and the detection  $t_d$  times can be obtained as:

$$N_m = \frac{1}{\lambda_m} P_m (1 - e^{-\lambda_m t_{irr}}) e^{-\lambda_m t_c} e^{-\lambda_m t_d}, \tag{A5}$$

$$N_g = \frac{\eta P_m P_m}{\lambda_g (\lambda_g - \lambda_m)} (\lambda_g (1 - e^{-\lambda_m t_{irr}}) e^{-\lambda_m t_c} e^{-\lambda_m t_d} - \lambda_m (1 - e^{-\lambda_g t_{irr}}) \times e^{-\lambda_g t_c} e^{-\lambda_g t_d}) + \frac{1}{\lambda_g} P_g (1 - e^{-\lambda_g t_{irr}}) e^{-\lambda_g t_c} e^{-\lambda_g t_d}. \tag{A6}$$

Due to  $A_x = \lambda_x N_x$ , the  $A_x$  can be obtained as the following:

$$A_m = P_m (1 - e^{-\lambda_m t_{irr}}) e^{-\lambda_m t_c} e^{-\lambda_m t_d}, \tag{A7}$$

$$A_g = \frac{\eta P_m P_m}{(\lambda_g - \lambda_m)} (\lambda_g (1 - e^{-\lambda_m t_{irr}}) e^{-\lambda_m t_c} e^{-\lambda_m t_d} - \lambda_m (1 - e^{-\lambda_g t_{irr}}) \times e^{-\lambda_g t_c} e^{-\lambda_g t_d}) + P_g (1 - e^{-\lambda_g t_{irr}}) e^{-\lambda_g t_c} e^{-\lambda_g t_d}. \tag{A8}$$

Substituting Eq. 7 into Eq. 1 and solving it, the  $C_m$  can be gotten as:

$$C_m = I_m \epsilon_m P_m \frac{(1 - e^{-\lambda_m t_{irr}})}{\lambda_m} e^{-\lambda_m t_c} (1 - e^{-\lambda_m t_d}), \tag{A9}$$

where the Eq. 3a in the proof is deduced out.

And do the same performance to Eq. 8 like Eq. 7. The  $C_g$  can be obtained as:

$$C_g = I_g \epsilon_g \left\{ P_g \frac{1 - e^{-\lambda_g t_{irr}}}{\lambda_g} e^{-\lambda_g t_c} (1 - e^{-\lambda_g t_d}) + P_m \frac{\eta}{\lambda_g - \lambda_m} \left[ \frac{\lambda_g}{\lambda_m} (1 - e^{-\lambda_m t_{irr}}) \times e^{-\lambda_m t_c} (1 - e^{-\lambda_m t_d}) - \frac{\lambda_m}{\lambda_g} (1 - e^{-\lambda_g t_{irr}}) e^{-\lambda_g t_c} (1 - e^{-\lambda_g t_d}) \right] \right\}, \tag{A10}$$

where the Eq. 3b in the proof is deduced out.