

## How Gaps in Time-Series Data Affect Asteroseismic Interpretation

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Most pulsating white dwarf stars pulsate with many periods, each of which is a probe of their interior, which has made asteroseismolgy of these stars an active field. However, disentangling the multiple periodicities requires long, uninterrupted strings of data. We briefly describe the history of multi-site observing campaigns that culminated in the development of the Whole Earth Telescope in the late 1980s that still functions today. Through examples from the May 1990 campaign on GD 358, we show how critical it is to eliminate periodic gaps in data to greatly reduce aliasing in Fourier Transforms normally used to analyze the frequency content of pulsating white dwarfs. We close with a brief description of space satellite-based data, along with the advantages and disadvantages of these data compared to ground-based data.

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## INTRODUCTION

White dwarf stars are the most common endpoint of stellar evolution and are the ultimate fate of all stars with masses less than about 8-10 Mo (Woosley and Heger, 2015). Because their luminosity comes from radiating away the thermal energy in their cores, they are relatively simple to model as complicated thermonuclear reaction networks are not needed (Wood, 1992; Althaus et al., 2010). The typical structure of a white dwarf is a carbon/oxygen core (the ashes of core helium burning), with a helium mantle comprising about 1% of the star's mass. About 80% of these stars also have an outermost hydrogen layer that is 0.01% (or less) of the stellar mass (Bradley, 1996; Bradley, 1998; Giammichele et al., 2016). As these stars cool, the outer layers pass through temperature and density conditions where the opacity reaches a maximum, and this can modulate the outward heat flow, leading to pulsations (Winget et al., 1982a; Winget et al., 1982b). Nature has been kind enough to provide several classes of pulsating white dwarfs, including (but not limited to) the hot PG 1159 stars, DBV, and ZZ Ceti stars. The DBV and ZZ Ceti stars in particular appear to be phases that all helium atmosphere (DBV) and hydrogen atmosphere (ZZ Ceti) stars go through, so that what we learn about the structure of the pulsating white dwarfs should apply to white dwarfs more generally. Good recent reviews of pulsating white dwarfs include: Winget and Kepler (2008), Fontaine and Brassard (2008), Kepler and Romero (2017), and Corsico et al. (2019). Numerous white dwarfs pulsate with many different periods at once. While white dwarfs with multiple periods offer great potential for asteroseismology, with each mode offering a different probe of the interior, they also make data collection and analysis a challenge. The best way to analyze these data is to assume the periods are stable over the course of an observing run, as it can be impossible to disentangle real periods from noise and additional peaks resulting from gaps due to single-site data and bad weather. The most common additional peaks arise from daily sunrise and sunset, and this creates a pattern of side lobes usually separated by multiples of 1 cycle/day or 11.57 µHz surrounding the main peak. Examples of such patterns may be found in Figure 1, (Winget et al., 1985; Nather et al., 1990).



# THE WHOLE EARTH TELESCOPE AND THE MAY 1990 OBSERVING RUN

The problems of single-site data analysis became especially acute with the discovery of PG 1159–035 (McGraw et al. 1979), which was found to have a number of equally spaced (in period) modes. Theoretical models suggested that the star should be cooling rapidly enough that changes in the pulsation period should be observable; the time of maximum brightness (phase) is an even more sensitive indicator of cooling than the length of the period. A change in the phase of the dominant 516 s period should be visible within a few years (McGraw et al. 1979). Observers in Texas and South Africa obtained telescope time near the same calendar dates and the longer daily data strings reduced the aliasing enough to allow a detection of the cooling rate as measured by the 516 s mode (Winget et al. 1985). While these multi-site observations showed promise, the alias pattern was still an issue. Clearly, something better was needed.

The Whole Earth Telescope (aka WET; Nather, 1989; Nather et al., 1990) was created in the late 1980s by the white dwarf community to address the need for continuous photometric data sets to reduce aliasing noise to low levels and realize the potential for asteroseismology of white dwarf stars. The paper on PG 1159-035 (Winget et al., 1991) demonstrated that the Whole Earth Telescope could eliminate aliasing; the alias peaks were only 5% of the power of the main peak. By contrast, the alias peaks could be 70–90% of the power of the main peak for single-site data (Nather, 1989, **Figure 1**). In May 1990, the primary target of the WET was the prototype pulsating DB (DBV) star GD 358. The results of the observing run were published by Winget et al. (1994) as well as Bradley and Winget (1994) and we refer the reader to those papers for details. Here, we summarize the observations and show how adding sites reduces the aliasing peaks in the Fourier Transform (FT). Our aim is to show which longitude distribution is optimal for reducing the alias peaks (if a gap must exist) and the dramatic reduction in the alias peaks once the longitude gaps are filled, even once. We will not be describing the seismological results for GD 358, but refer the reader to Bischoff-Kim et al. (2018) and Corsico et al. (2021) for the latest results.

GD 358 is a northern hemisphere target with an RA of  $16^{h} 47^{m}$  and declination of  $+32^{\circ} 28'$ . The observing sites for GD 358 included: McDonald Observatory (Texas, 0.9 m), Kitt Peak Observatory (Arizona, 1.3 m), Mauna Kea (Hawai'i, 0.6 m), Perth (Australia, 0.6 m), Wise Observatory (Israel, 1 m), South African Astrophysical Observatory (SAAO, South Africa, 0.75 m), Itajuba (Brazil, 1.60 m); European Southern Observatory (Chile, 1.0 m). The sites are shown as stars on the world map in **Figure 2**.

There are a couple things worth noting about the observation strategy that are key for GD 358. First is that GD 358 is relatively bright (mag = 13.65) and is a large amplitude pulsator (up to 0.3 mag). As a result, telescopes as small as 0.6 m contributed excellent data. Requiring smaller telescopes means that potentially more sites could participate. The second thing to note is that several longitudes had more than one observing site, which made it more likely that we would observe GD 358 over an entire 24 h cycle (see also O'Donoghue and Provencal, 1992) and less likely that weather would create gaps in the data. **Figure 3** shows the reduced data from all the sites. The first thing to note is that there is not a continuous 24 h span of coverage at any time during the run. However, all of the 24 h of a day have at least some coverage, as we describe. On day 1, there are gaps between 22,000 and 32,000 s as well as 42,000 to 68,000 s. The first gap gets filled



between days 3 and 4 (281,000 to 291,000 s) and days 4 and 5, while the second gap is largely filled by data from Israel and Perth on subsequent days (days 3 and 4 for example). As we will show, just filling all 24 h of longitude even once during the entire observing run is enough to nearly wipe out the 1 cycle per day alias.

## THE FOURIER TRANSFORM AND "WINDOW FUNCTION"

### **Fourier Transform**

To analyze data for pulsating stars, we start by assuming the observed periodicities are constant over the course of an observing run. This allows us to process the data with a Fourier Transform (FT; Blackman and Tukey, 1958) to analyze the frequency content of the pulsations. Problems arise when the data have gaps. If the interval between individual data points is short relative to the periods of interest, then the gaps will not have a significant effect on data interpretation. For this reason, the observers of GD 358 used 10 s integration times, which is short compared to the shortest observed periods of >400 s for the pulsation modes and >200 s for the combination peaks arising from the non-sinusoidal shape of the light curve. Another requirement is that the observing runs are long enough to sample several cycles of the dominant modes; in this case, the runs need to be at least 2-3 h long. The problem arises with the fact that the Sun comes up at every observing site once per day. Thus, while an FT may compute the largest amplitude for a pulsation mode at, say, 1,428 µHz (123.4 cycles/day), the periodic gap implies there is a nonnegligible chance that a mode at 1,439.6 and 1,416.4  $\mu$ Hz (or 1 cycle/day different) can fit the data (with a lower amplitude) as shown in **Figure 1**. If the pulsations are monoperiodic, the "comb" pattern can be recognized and the true period determined. However, almost all white dwarfs are multiperiodic and have modes with similar amplitudes, which can make disentangling single-site data impossible. This impasse, the favorable experience with 2-site data, and a desire to perform asteroseismology of white dwarfs amongst the community led to the development of the WET (Nather, 1989; Nather et al., 1990).

## The "Window Function" for GD 358

With this said, we can turn to the main point of this article, which is to show how minimizing the single-site daylight observing gaps can reduce the alias pattern and make asteroseismology possible. We show the main result in Figure 4. In this example, we take a single sine wave with a period of 700 s (which is the dominant mode of GD 358) that has l = 1, and is the 15th radial overtone (k = 15). We then sample this mode with exactly the same time span as the data selected. This is commonly called the "window function". In Figure 4, we show the results for data from a single site with good weather (7 of 8 nights; dark blue curve for Hawai'i), data from two sites (red, green, and cyan curves), and finally all of the data shown in Figure 3 (black curve). The results from a single site (about 8 h of data per night) exhibit prominent 1 cycle/day and other alias peaks. The red and green curves show the result when two adjacent sites (Hawai'i and Perth) or (Hawai'i and the Americas) are used. The 1 cycle/day alias power is cut in half, and the other peaks virtually disappear. The alias patterns are very similar, because each represents



12–14 h of continuous data each day. When two sites on opposite sides of the Earth are used (Hawai'i and Israel, cyan curve), the 1 cycle/day peak disappears, and the peak at 2 cycles/day (23.14  $\mu$ Hz) is the most prominent. In this case, the roughly 14 h of data have periodic gaps of about 5.5 and 4.5 h each day. Finally, when all the data are used, the alias peaks become negligible (<6% in power). As mentioned earlier, it is not necessary to obtain a continuous 24 h string of data in 1 day; it just needs to be done at least once during an observing run of about 10 days.

The window function suggests that two-site data will have an alias pattern considerably reduced from single-site data, but it will still imprint a pattern that makes discerning individual modes challenging, especially if the mode content is rich. Most of the pulsation power (amplitude squared) in GD358 lies in the range of 1,200–2,500  $\mu$ Hz, with "combination" peaks arising from nonlinear pulse shape modulations showing up outside this range. In **Figure 5**, we show the FT of the main region using data from Hawai'i and Perth. Each of the main modes happens to be a rotationally split l = 1 triplet, but aliasing makes this identification difficult. For example, the k = 15 (15th radial overtone) mode shows 6 large peaks and many smaller peaks nearby, while the k = 13 mode has two large peaks. In this case,

with the benefit of hindsight, we would be able to identify the different overtones, but we would have difficulty picking out the rotationally split sidelobes from the alias pattern, which would compromise our confidence that these are all the same spherical harmonic index modes. If we compare **Figure 5** to **Figure 6**, where we compute an FT for the region from 2000 to 2,500  $\mu$ Hz, the difference in the alias pattern is dramatic. Each of the main modes now shows a clear triplet pattern and the overall "noise" level is greatly reduced. We refer the reader to Winget et al. (1994) for the definitive data analysis (see especially their **Figures 3** and 7); our aim here is to graphically illustrate that the WET achieved the goal of nearly eliminating alias peaks and making asteroseismology of white dwarf stars possible.

## SATELLITE DATA AND THE FUTURE

#### Satellite Data

The recognized need for long time baseline photometric data without being subject to the vagaries of weather, allocations of telescope time, and the circumstances of astronomers at each site on the globe led to the recognition that space-based photometry offered compelling opportunities. An early



FIGURE 4 | A summary of the spectral window for a single mode at 700 s (which happens to be the largest amplitude mode (I = 1, k = 15) seen in May 1990). The dark blue curve shows the results from a single site, with prominent 1 cycle/day and other peaks. The red and green curves show the result when two adjacent sites (Hawai'i and Perth) or (Hawai'i and the Americas) are used. The 1 cycle/day alias power is cut in half, and the other peaks virtually disappear. When two sites on opposite sides of the Earth are used (Hawai'i and Israel, cyan curve), the 1 cycle/day peak disappears, and the peak at 2 cycles/day is the most prominent. Finally, when all the data are used, the alias peaks become negligible (<6% in power).



space probe dedicated to photometric seismology was MOST (Walker et al., 2003), which was a small satellite that could only observe bright (mag <6) stars. However, it demonstrated that satellite photometry could obtain long (~30 days) strings of data of uniform quality, sufficient for asteroseismology of

some bright stars. COROT (Baglin et al., 2002; Baglin et al., 2009; Poretti et al., 2009) was another satellite that was used to obtain roughly 30–60 days timespan data sets for pulsating and rotationally modulated variable stars. The major breakthrough came with the *KEPLER* (Koch et al., 2010; Borucki et al., 2010)



spacecraft, which was designed to look for extrasolar planet transits via photometry, but was also ideally suited for variable star research. *KEPLER* discovered many thousands of new variable stars (with mag <17; Koch et al., 2010) with unprecedented measurement accuracy. In the original field (Borucki et al., 2010), some stars had up to 4 years of nearly continuous data. Currently, the *TESS* satellite (Ricker et al., 2014) is being used for asteroseismology. Based on the results of Bognar et al. (2020), the limiting magnitude of TESS to observe pulsating white dwarfs is ~17). Corsico et al. (2021) have recently analysed *TESS* results for GD 358.

## A Comparison of Ground-Based Versus Space-Based Data Collection

Ground-based and space-based photometry have their advantages and disadvantages for long time baseline precision photometry and should be viewed as complimentary tools.

Ground-based photometry has the singular advantage of being far cheaper to implement than building, launching and running a spacecraft, even a modest one such as MOST. In addition, observing sites can be chosen based on the declination of the target star and all of the sky is potentially available. Also, a ground-based network typically involves far fewer people than a satellite collaboration.

That being said, ground-based photometry has some significant drawbacks. Foremost is the issue of weather. Multiple sites at each longitude can mitigate weather-related data gaps, but not eliminate them. In addition, low frequency (on order of hours) transparency variations are very hard to remove unless careful work is done with the photometric data collection to remove these effects. Another serious issue is dealing with the bureaucracy of different telescope allocation committees and different countries' views of funding asteroseismology, especially when the papers have many coauthors. These constraints affect which sites can participate. Also, resources and observer fatigue make it difficult for runs to last longer than 2 weeks or occur more than twice a year. Another issue is creating a "standard instrument" that mitigates cross-calibration issues. As discussed by Nather et al. (1990), this turned out not to be a major issue, but it cannot be ignored. Finally, the telescopes are of different sizes (and state of repair) and observing sites are of different quality. In addition, it is much easier to obtain time on smaller telescopes (which are frequently controlled by one institution) than large ones. This tended to limit targets to magnitude 15 or brighter in many cases. Small telescopes at premier observing sites are also at risk of being removed in favor of building a larger telescope. This fate befell the two 24 inch telescopes at Mauna Kea; they were removed to allow much larger telescopes to be built.

Ground-based photometry typically has a frequency resolution limit of 0.1 days (~0.5  $\mu Hz$  for a 10 days observing run) and a noise limit of about 0.1 mmag.

Space-based photometry has the enormous advantage of the instrument being above the Earth's atmosphere. This means no atmospheric data artifacts and no sunrise/sunset issues. As a result, the noise limit is typically in the 1  $\mu$ mag range, or up to 100 times better than from the ground. Most satellites were (and are) set up to observe a particular spot in the sky for 1–2 months,

although *KEPLER* observed some targets for up to 4 years. The frequency resolution is therefore 0.1 to 0.005  $\mu$ Hz. Observations with extremely long time baselines (>1 year) also showed amplitude variations in pulsation modes and infrequently occurring phenomena (the "*sforzando*" event in GD 358; Provencal et al., 2009) being a case in point. Once funded, satellites tend to have many more resources available for observing, data reduction, and analysis, so that there is a large quantity of data collected and a large number of people available (even the entire astronomical community, once the "exclusive rights" period expires).

The biggest drawback of space-based photometry is the extreme expense of the mission and competition with other space missions. This means only a few missions have been flown and almost all of these missions were multi-purpose, in that the photometry was used for extrasolar planet transits, pulsations, and other sources of light variations in stars. Competition to observe stars, especially with rapid cadence, can be intense. The observing pattern for some satellites has resulted in some parts of the sky being relatively poorly sampled. The expense of launching large amounts of mass means that the telescope size is typically rather modest, with *KEPLER* being a 0.95 m telescope and TESS being four 10.5 cm lenses.

### CONCLUSION

We have shown that multi-site data with 24 h coverage at some point during an observing run can drastically reduce the 1 cycle/ day alias pattern seen in FTs of pulsating white dwarfs, which have enabled asteroseismology of these (and other) stars. In our illustration, we describe how the need to remove these alias peaks motivated the creation of the Whole Earth Telescope and similar networks. Later, this promise led to the development of satellites

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that could "stare" continuously at a target for 1–2 months with photometric precisions not possible from the ground. Each method has advantages and disadvantages, and hopefully people and funding agencies will continue to have an interest in asteroseismology in general and white dwarf asteroseismology in particular.

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PB conceived the idea for this article, performed the Fourier Transforms and wrote the article.

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