



# Self-Calibrated Measurement of Frequency Response for Broadband Photodetectors Based on Two-Tone Photonic Sampling

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Wang M, Xu Y, He Y, Liu Z, Zhang Y, Zhang Z, Li H, Zhang S and Liu Y (2021) Self-Calibrated Measurement of Frequency Response for Broadband Photodetectors Based on Two-Tone Photonic Sampling. Front. Phys. 9:678777. doi: 10.3389/fphy.2021.678777 A self-calibrated method to measuring the frequency responses of broadband photodetectors (PDs) is proposed based on photonic pulse sampling of two-tone microwave signal, with the help of a mode-locked laser diode (MLLD) and a Mach-Zehnder modulator (MZM). Firstly, the repetition frequency of the optical comb from the MLLD divides the whole measuring frequency range into several segments. Then, a close-spaced two-tone signal modulates every comb tooth through the MZM and generates the sum- and difference-frequency products, working as the probing signal to extract the frequency response of the PD in every segment. Hyper-fine frequency response of the PD at any frequency point can be obtained in every segment by subtly varying the center frequency of the two-tone signal while keeping the difference frequency fixed. Finally, the whole frequency response of the PD in ultra-wide frequency range is obtained by seamlessly stitching the segmental frequency responses. In our experiment, measurement of a commercial PD is demonstrated up to 49.765 GHz with an optical comb at the repetition frequency of 9.953 GHz and a two-tone modulation up to 4.9765 GHz. The measured results are compared with those by using the traditional methods to check accuracy. Moreover, the uneven responses of the MLLD and the MZM are fully subtracted, verifying the ultra-wideband, hyperfine and self-calibrated measurement of PDs based on the two-tone photonic sampling.

Keywords: frequency response, photodetectors, photonic sampling, optical fiber communication, microwave photonics

# INTRODUCTION

Broadband photodetectors (PDs) are essential optical receiver components in optical fiber communication systems and microwave photonic links [1-3], and the frequency response measurement with high-resolution and high-accuracy is very critical to supporting the device characterization and link evaluation for high-spectral-efficiency optical communication systems and hyper-fine microwave photonic links [4-6].

There are numerous methods reported for characterizing frequency responses of PDs by employing all-optical or electro-optical stimulus. The all-optical methods can achieve ultrawideband measurements of PDs based on the ultra-wideband optical stimulus. However, the

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optical wavelength-beating method requires to control the optical wavelength drifting and power fluctuation with extremely high accuracy [7-10], and the optical noise-beating method is subject to the poor signal-to-noise ratio and insufficient frequency resolution [11-14]. By contrast, the electro-optical methods make the best use of electro-optical modulation to improve the frequency resolution. However, the widely used electro-optical swept frequency method needs intense calibration to subtract the effect of the assisted modulator [15-17]. In order to alleviate the electro-optical calibration, the improved swept frequency method was proposed with the help of an electro-absorption modulator used as a modulator and a PD, provided that the frequency responses of the modulator and the PD are identical [18, 19]. The twice modulation method requires active bias control of two intensity modulators [20]. For the calibration-free and bias-drifting-free measurement, we proposed a frequencyshifted heterodyne scheme for extracting frequency responses of PDs [21-24]. Recently, we also presented a low-speed photonic sampling method for the frequency response measurement within ultra-wide frequency range based on a mode-locked laser diode (MLLD), which is also free of the uneven frequency responses of other components in the setup [25]. Nevertheless, the major difficulty of this method lies in that hyper-fine measurement of PD at any frequency point cannot be obtained, since the frequency resolution is limited to be tens of MHz by the repetition frequency of the MLLD.

In this work, we demonstrate a two-tone photonic sampling method, featuring hyper-fine frequency resolution and ultrawide frequency range, for self-calibrated frequency response measurement of broadband PDs. As is shown in Figure 1, the optical pulses from a MLLD are sent to a Mach-Zehnder modulator (MZM) for two-tone modulation, and then are detected by the PD under test. Firstly, the whole frequency range is equally divided into several segments by the repetition frequency of the optical comb from the MLLD. The comb tooth in every segment mixes with the two-tone signal and generates the sum- and difference-frequency products, working as the probing signal to measure the frequency response of the PD, and then the hyper-fine frequency response of the PD at any frequency point is obtained in every segment by subtly varying the center frequency of the two-tone signal. Finally, the whole frequency response of the PD in ultra-wide frequency range can be obtained by stitching the multiple segments. It is noteworthy that the uneven response of the MLLD and the MZM are subtracted by carefully setting the two-tone photonic sampling. Theoretical basis and experimental results are elaborated in detail, where the experimental results agree well-with those obtained by employing the low-speed photonic sampling method.

## **Theoretical Basis**

The schematic diagram of the proposed two-tone photonic sampling is shown in **Figure 1**. The ultrashort pulses with a repetition frequency of  $f_r$  from the MLLD is modulated by the two-tone signal at the frequencies of  $f_1$  and  $f_2$  via the MZM. After two-tone electro-optical modulation, upper- and lower-optical sidebands will be generated at both sides of the optical

comb teeth of the MLLD. The two-tone sampling optical signals are then detected by the PD under test, and analyzed by an electrical spectrum analyzer (ESA). After photodetection, the two-tone upper- and lower-optical sidebands will mix with each other and generate sum- and difference-frequency products at the offset frequency of  $f_1 \pm f_2$  ( $f_1 > f_2$ ) of the comb tooth at the frequency of nfr. As we know, each pair of optical upperand lower-sidebands will keep equalized in the optical domain, and their amplitude difference in the electrical domain only depends on the frequency response of PD. In our method, the two-tone frequencies  $f_1$  and  $f_2$  are carefully chosen so that the lower frequency of  $\Delta f$  (=  $f_1$ - $f_2$ ) is fixed and close to DC, and the frequency response of the PD at the frequency of  $nf_r + f_1 + f_2$  with respect to the frequency of  $nf_r + \Delta f$  can be calculated through the amplitude ratio between these two frequency components, which is shown in Figure 1(I). Then, through subtly varying  $f_1 + f_2$  from 0 to  $f_r$  while keeping  $f_1$  $f_2$  constant, the relative frequency response of the PD at any frequency point between  $nf_r + \Delta f \ (\approx nf_r)$  and  $nf_r + f_1 + f_2$  $(\approx (n+1)f_r)$  can be extracted in the *n*-th segment. As is presented in Figure 1(II), the frequency response at the frequency of  $nf_r + f_1 + f_2$  is normalized to that at the frequency of  $nf_r + \Delta f$  in every segment. In order to obtain the whole frequency response of PD in ultra-wide frequency range, in our case, a specific two-tone frequency is carefully chosen to be  $f_1' = f_r/4$  and  $f_2' = f_r/4-\Delta f$  to ensure all the frequency responses at the frequencies of  $nf_r + \Delta f$  are referenced to the same fixed lowfrequency of  $\Delta f$  as illustrated in **Figure 1(III)**. Therefore, the segmental frequency responses are seamlessly stitched, as shown in Figure 1(IV), allowing for the self-calibrated measurement of frequency response of PDs within ultra-wide frequency range of  $(n+1)f_r$ .

Mathematically, the ultrashort optical pulses from the MLLD can be expressed in the optical domain as

$$E_{MLLD}(t) = \sum_{l=-N}^{N} q_l e^{j2\pi (f_0 + lf_r)t}$$
(1)

Thereinto,  $f_0$  and  $q_l$  are the central frequency of the amplitude of the optical comb from the MLLD, respectively. *N* represents the effective order of the optical comb tooth. The ultrashort optical pulses are injected into the MZM onto which two closely spaced tones  $v_1(t) = v_1 \sin 2\pi f_1 t$  and  $v_2(t) = v_2 \sin 2\pi f_2 t$  ( $f_1 > f_2, f_1 \approx f_2$ , and  $0 < f_1, f_2 \le f_r/2$ ) are applied. The output optical field from the MZM can be written by [26].

$$E_{MZM}(t) = E_{MLLD}(t) \cdot \left[1 + \gamma e^{jm_1 \sin 2\pi f_1 t + jm_2 \sin 2\pi f_2 t + j\varphi_b}\right]$$
(2)

with the asymmetric factor  $\gamma$  and the phase bias  $\varphi_b$  of the MZM.  $m_1$  and  $m_2$  are the modulation indices at the modulation frequencies of  $f_1$  and  $f_2$ , respectively. Then, the photonic sampling signal is sent into the PD under test, and is then



converted into electrical domain, which can be written as

$$i_{PD}(t) = R \cdot |E_{MZM}(t)|^2 = R \Big\{ 2 \left( 1 + \gamma^2 \right) \sum_{n=0}^{2N} p_n \cos \left( 2\pi n f_r t \right) - p_0 \left( 1 + \gamma^2 \right) - 2\gamma p_0 \sum_{n=0}^{+\infty} \sum_{r=0}^{+\infty} J_p(m_1) J_q(m_2)$$
(3)

$$-p_{0}(1+\gamma) - 2\gamma p_{0} \sum_{p=-\infty} \sum_{q=-\infty} j_{p}(m_{1})j_{q}(m_{2})$$
(3)  
$$p_{0}[2\pi (p_{1}+q_{1})t+q_{2}] + 2\gamma \sum_{p=-\infty} p_{1} \sum_{m=0}^{+\infty} \sum_{m=0}^{+\infty} L(m_{1})$$

$$\cdot \cos\left[2\pi \left(pf_1 + qf_2\right)t + \varphi_b\right] + 2\gamma \sum_{n=0} p_n \sum_{p=-\infty} \sum_{q=-\infty} J_p(m_1)$$
$$J_q(m_2) \cos\left[2\pi \left(nf_r \pm pf_1 \pm qf_2\right)t \pm \varphi_b\right] \right\}$$

where *R* is the responsivity of PD,  $J_p(\cdot)$  and  $J_q(\cdot)$  are the *p*th and *q*th-order Bessel function of the first kind, respectively. The coefficient  $p_n$  represents the intensity of the comb tooth from the MLLD, expressed by

$$\sum_{l=-N}^{N-n} q_l q_{l+n} = p_n, (n = 0, 1, ..., 2N)$$

The two-tone signal will mix with each comb tooth and generate frequency up- and down-conversion components quantified as

$$A (nf_r + f_1 - f_2) = 4\gamma p_n R (nf_r + f_1 - f_2) J_1 (m_1) J_1 (m_2) \cos \varphi_b$$
(4a)  

$$A [nf_r \pm (f_1 + f_2)] = 4\gamma p_n R [nf_r \pm (f_1 + f_2)] J_1 (m_1) J_1 (m_2) \cos \varphi_b$$
(4b)

where the bias status of the MZM is the same for these desired frequency components.

In our method, the whole measuring frequency range are divided into several segments by the repetition frequency  $f_r$  of the MLLD. The frequency component at  $nf_r + f_1 + f_2$  is served as the probe signal to extract the high frequency response of PD under test, meanwhile the frequency component at  $nf_r + \Delta f$  ( $\Delta f = f_1 - f_2$ ) is taken as the reference signal. Therefore, the frequency response of PD at the frequency of  $nf_r + f_1 + f_2$  relative to the frequency of  $nf_r + \Delta f$  can be obtained in the *n*-th intra-segment measurement by

$$\frac{R\left(nf_r + f_1 + f_2\right)}{R\left(nf_r + \Delta f\right)} = \frac{A\left(nf_r + f_1 + f_2\right)}{A\left(nf_r + \Delta f\right)}$$
(5)



It is easily seen from Eqs. (4) and (5) that phase bias and the uneven response of the MZM is totally canceled out through the amplitude ratios of these frequency components, indicating the intra-segment measurement can be self-calibrated.

To characterize the PD in the whole frequency range, the frequency responses of PD at the frequency of  $nf_r + \Delta f$  are required to be referenced to that at the same low-frequency of  $\Delta f$  (n = 0) so that all the segmental frequency responses can be seamlessly stitched. According to Eq. (4a), the frequency response of PD at the frequency of  $nf_r + \Delta f$  ( $= nf_r + f_1 - f_2$ ) relative to the frequency of  $\Delta f$  ( $= f_1 - f_2$ ) is written by

$$\frac{R\left(nf_r + \Delta f\right)}{R\left(\Delta f\right)} = \frac{A\left(nf_r + \Delta f\right)}{A\left(\Delta f\right)} \cdot \frac{p_0}{p_n} \tag{6}$$

where the term  $p_0/p_n$  represents the uneven comb intensity of the MLLD. For the inter-segment stitching, the two-tone frequencies are carefully set to be  $f_1 = f_r/4$  and  $f_2 = f_r/4$ - $\Delta f_r$ , to have the assumptions of  $if_r + f_1 + f_2 \approx (i+1)f_r - f_1 - f_2$  and  $R(if_r + f_1 + f_2) \approx R[(i+1)f_r - f_1 - f_2]$  ( $i = 0 \sim n-1$ ) stand. In this case, the uneven comb intensity of the MLLD can be obtained by comparing these two frequencies, given by

$$\frac{p_0}{p_n} = \prod_{i=0}^{n-1} \frac{p_i}{p_{i+1}} = \prod_{i=0}^{n-1} \frac{A\left(if_r + f_1' + f_2'\right)}{A\left[(i+1)f_r - f_1' - f_2'\right]}$$
(7)

Through substituting Eq. (7) into Eq. (6), any frequency response of PD at the frequency of  $nf_r + \Delta f$  can be uniformly referenced to the same low-frequency of  $\Delta f$ . It is easily seen from Eqs. (4–6) that the uneven comb intensity of the MLLD is totally subtracted, indicating the inter-segment stitching can be selfreferenced. Moreover, through slightly sweeping the two-tone frequencies from 0 to  $f_r/2$ , the relative frequency response of PD at any frequency can be extracted within the measuring frequency range of  $(n + 1)f_r$ .

## **RESULTS AND ANALYSIS**

In our experiment, the ultrashort optical pulses come from a MLLD with the repetition frequency of 9.953 GHz ( $f_r$ ) and the output power of 0.58 dBm. The two-tone signal provided by two microwave sources (MSs, R&S SMB100A) is loaded onto a MZM (EOSPACE AX-0MSS-10) through a microwave combiner. The optical sampling signal after the MZM is detected by the PD under test (DSC 10H), and the output electrical spectrum is acquired and analyzed by an ESA (R&S FSU50). In the measurement, the whole measuring frequency range of 49.765 GHz is divided into five segments (=  $5 \times f_r$ ,  $n = 0 \sim 4$ ) by the repetition frequency of 9.953 GHz  $(f_r)$ . The two-tone frequency is chosen to be  $f_1$ - $f_2 = 1$  MHz ( $\Delta f = 1$  MHz), where  $\Delta f$  can be taken other smaller values as long as the desired frequency component can be distinguished by the employed ESA, and it will not affect the measurement results. In this case, the frequency response of PD at the frequency of  $nf_r + f_1 + f_2$  with respect to the frequency of  $nf_r + \Delta f$  can be calculated in the intra-segment measurement. Figure 2 shows typical electrical spectra around  $nf_r + f_1 + f_2$  and  $nf_r + \Delta f$  in the initial (n = 0), first (n =1), second (n = 2) and third (n = 3) segment under different two-tone modulations, where the resolution bandwidth (RBW) of the ESA is set as 500 Hz. For example, when the two-tone frequencies of  $f_1$  and  $f_2$  are set to be 4.97 GHz and 4.969 GHz, the electrical powers at the frequencies of 1 MHz ( $\Delta f$ ) and 9.939 GHz ( $f_1 + f_2$ ) are measured to be -59.07 dBm and -60.63 dBm in the initial segment (n = 0). According to Eq. (5), the frequency response of PD at the frequency of 9.939 GHz  $(f_1 + f_2)$  with respect to the frequency of 1 MHz ( $\Delta f$ ) is calculated as-1.56 dB (= -60.63+59.07). Under the same condition, the electrical powers at the frequencies of 9.954 GHz ( $f_r + \Delta f$ ) and 19.892 GHz  $(f_r + f_1 + f_2)$  are measured to be -62.99 dBm and -60.65 dBm in the first segment (n = 1). Thus, the frequency response of PD at the frequency of 19.892 GHz  $(f_r + f_1 + f_2)$  with respect to the frequency of 9.954 GHz ( $f_r + \Delta f$ ) is solved to be 2.34 dB



(= -60.65+62.99) in the first segment (n = 1). Similarly, the frequency response of PD at the frequency of  $nf_r + f_1 + f_2$  with respect to the frequency of  $nf_r + \Delta f$  can be obtained for other segments (n = 2, 3, 4). In addition, through slightly sweeping the two-tone frequencies from 0 to 4.9765 GHz ( $f_r/2$ ), the frequency response of PD at any frequency with respect to the reference frequency in each segment can be obtained, as displayed in **Figure 4**.

To stitch the five segments, the two-tone frequencies are carefully set to be  $f_1' = 2.48825$  GHz ( $f_r/4$ ) and  $f_2' = 2.48725$ GHz ( $f_r/4-\Delta f$ ), and the measured electrical spectra around  $nf_r + \Delta f_i$ ,  $if_r + f_1' + f_2'$  and  $(i + 1)f_r - f_1' - f_2'$  are illustrated in Figure 3 for different segments. For example, the desired frequency components are measured to be -56.70 dBm at 1 MHz  $(\Delta f)$ , -59.21 dBm at 9.954 GHz  $(f_r + \Delta f)$ , -58.79 dBm at 4.9755 GHz  $(f_1' + f_2')$  and -59.82 dBm at 4.9775 GHz  $(f_r-f_1'-f_2')$ , respectively. According to Eqs. (6) and (7), the uneven comb intensity  $p_0/p_1$  of the MLLD can be determined to be 1.03 dB, and then the frequency response of PD at the frequency of 9.954 GHz ( $f_r + \Delta f$ ) relative to the low-frequency of 1 MHz ( $\Delta f$ ) can be solved to be -1.48 dB in the initial segment (n = 0). Therefore, the frequency response of PD at the frequency of 19.892 GHz  $(f_r + f_1 + f_2)$  in the first segment (n = 1) can be referenced to that at the low-frequency of 1 MHz ( $\Delta f$ ) in the initial segment (n = 0), and is calculated as 0.86 dB (2.34–1.48). Similarly, the uneven comb intensity  $p_0/p_2$  of the MLLD can be solved to be 2.85 dB, and the frequency response of PD at the frequency of 19.907 GHz  $(2f_r + \Delta f)$  in the second segment (n = 2) relative to the frequency of 1 MHz ( $\Delta f$ ) in the initial segment (n = 0) can be determined to be 0.46 dB. In this case, the frequency response of PD at any frequency of  $nf_r + f_1 + f_2$  relative to the same lowfrequency of  $\Delta f$  can be extracted, and the frequency responses of all five segments can be stitched together, as shown in Figure 4.

Figure 5 shows the measured results with the proposed method and the method in [23] as well as the manufacturer data. The good consistency between these results verifies the



**FIGURE 4** | Measured frequency response of PD before and after inter-segment stitching.



effectiveness of the proposed method. To further demonstrate hyperfine measurement, the frequency response of PD has been finely measured at around 32.51 GHz, as shown in the Figure 5. It can be seen that there are only four data points in the frequency range of 300 MHz based on the method in [23], which is limited by the repetition frequency of 96.9 MHz of the employed MLLD. In contrast, our method enables hyperfine measurement with different frequency steps, such as 300 kHz, 10 kHz and 10 Hz, which is mainly limited by the coherence characteristics of the ultrashort optical pulses, the tuning step of the MS and the RBW of the ESA. As displayed in Figure 2, the output electrical spectra from PD show extremely narrow spectral lines, indicating the inherent coherence of the ultrashort optical pulse source. The tuning step of the MS is 1 Hz, and the minimum RBW of the ESA is 10 Hz. Therefore, our method can be qualified by the hyperfine measurement of 10 Hz level.

## **Measurement Uncertainty**

For the accuracy, the measurement uncertainty of the proposed method is investigated. In the intra-segment measurement, the uncertainty of the relative frequency response of PD in the *n*-th segment can be derived by the total derivative of Eq. (5)

$$\frac{\delta R \left(nf_r + f_1 + f_2\right)}{R \left(nf_r + f_1 + f_2\right)} = \frac{\delta A \left(nf_r + f_1 + f_2\right)}{A \left(nf_r + f_1 + f_2\right)} + \frac{\delta A \left(nf_r + \Delta f\right)}{A \left(nf_r + \Delta f\right)}$$
(8)

According to the specification of ESA, the measurement uncertainty of amplitude is 0.05 dB when the range of RBW is from 10 Hz to 100 kHz. Therefore, the relative frequency response of PD in the *n*-th segment would have an uncertainty of <0.1 dB (= 0.05 × 2). It means that the uncertainty of the relative frequency response of PD in the initial segment (n = 0) is 0.1 dB, corresponding to a relative error of 1.16% [=  $(10^{0.1/20}-1) \times 100\%$ ].

In the inter-segment stitching, the uncertainty of the frequency response of PD at the frequency of  $nf_r + \Delta f$  relative to the frequency of  $\Delta f$  can also be obtained by the total derivative of Eq. (6)

$$\frac{\delta R \left( nf_r + \Delta f \right)}{R \left( nf_r + \Delta f \right)} = \frac{\delta A \left( nf_r + \Delta f \right)}{A \left( nf_r + \Delta f \right)} + \frac{\delta A \left( \Delta f \right)}{A \left( \Delta f \right)} + \frac{\delta \left( p_0/p_n \right)}{p_0/p_n}$$
(9)

Thereinto, the uncertainty of the uneven response  $p_0/p_n$  induced by the MLLD is mainly determined by the assumption of PD responsivity, that is  $R(if_r + f_1' + f_2') \approx R[(i + 1)f_r - f_1' - f_2']$  ( $i = 0 \sim n-1$ ). In the experiment, the frequency difference of these two components is set to be 2 MHz (=  $2 \times \Delta f$ ), and an uncertainty of the PD responsivity fluctuation introduced by the frequency difference is 0.05 dB based on the PD's specification. Thus, the uncertainty of the uneven response  $p_0/p_n$  from the MLLD would be 0.05  $\times n$  dB. This uncertainty can be reduced by further reducing the frequency difference. Meanwhile, the measurement amplitude uncertainty of ESA is 0.05 dB. Therefore, the frequency response of PD at the frequency of  $nf_r + \Delta f$  relative to the frequency of  $\Delta f$  will have an uncertainty of <0.05  $\times (n + 2)$  dB based on Eq. (9).

Finally, the frequency response of PD at the frequency of  $nf_r + f_1 + f_2$  relative to the fixed low frequency of  $\Delta f$  has a total uncertainty of no more than  $0.05 \times (n + 4)$  dB (n = 1, 2, 3, 4), which is directly related to the number of the frequency segments. t means that the maximum uncertainty in the experiment is 0.4 dB  $(= 0.05 \times 8)$ , and the corresponding relative error is 4.71%  $[= (10^{0.4/20}-1) \times 100\%]$ .

# **DISCUSSION AND CONCLUSIONS**

In the proposed method, the measuring frequency range of PD is related to the repetition frequency and the effective tooth number of the ultrashort optical pulses from the MLLD, which can be theoretically extended up to  $(2n + 1)f_r$ . In the proof-of-concept experiment, the measurement of PD is only performed up to 49.765 GHz (=  $5 \times f_r$ ,  $f_r = 9.953$  GHz), which is mainly limited by the operation bandwidth of the ESA (20 Hz~50 GHz). In addition, the method is also applicable for the MLLD

with low or higher repetition frequency. If a MLLD with lower repetition frequency is used as the ultrashort optical pulse source, the sweeping frequency range of the two-tone signal can be further reduced, which is only half of the repetition frequency. However, a lower repetition frequency of MLLD will result in more frequency segments and larger measurement uncertainty, so in practical applications, the repetition frequency of MLLD should be compromised in terms of the sweeping frequency range of MS and the measurement uncertainty. If the measurement uncertainty is to be reduced and a higher sweeping frequency range of the two-tone signal can be acceptable, a higher repetition frequency MLLD is better for measurement. In addition, the influence introduced by the phase bias of the MZM can be canceled out by the relative amplitudes of the desired frequency components. However, for a better signal-to-noise ratio (SNR), it is recommended to adjust the phase bias  $\varphi_b$  of MZM to make  $|\cos\varphi_h|$  as large as possible.

In conclusion, we have demonstrated a self-calibrated method for measuring frequency response of broadband PDs through two-tone photonic sampling. The two-tone microwave signal mixes with the optical comb of MLLD, and generates the sum- and difference-frequency products, working as the probing signal to extract the frequency response of PDs. Hyper-fine frequency response of PDs at any frequency point in intra-segment measurement is obtained by subtly varying the center frequency of the twotone signal. Moreover, the frequency response of the PD can be obtained in ultra-wide frequency range by intersegment stitching. In our method, the uneven responses of the MLLD and the MZM are completely eliminated through carefully setting the two-tone photonic sampling, enabling ultrawideband, hyperfine and self-calibrated measurement for highspeed PDs.

# DATA AVAILABILITY STATEMENT

The raw data supporting the conclusions of this article will be made available by the authors, without undue reservation.

# **AUTHOR CONTRIBUTIONS**

MW discussed with YZ, ZZ, HL, and YL, and drafted the content of the manuscript. MW and YX completed the experiment. YH and ZL participated in the analysis and discussion of the experimental results. SZ guided and revised the manuscript. All authors contributed to the article and approved the submitted version.

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**Conflict of Interest:** The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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