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# Snow surface properties derived from PRISMA satellite data over the Nansen Ice Shelf (East Antarctica)

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In this paper, we made use of PRISMA imaging spectroscopy data for retrieving surface snow properties in the Nansen Ice Shelf (East Antarctica). PRISMA satellite mission has been launched in 2019 and it features 239 spectral bands covering the 400–2500 nm interval. These data are promising for cryospheric applications, since several snow and ice parameters can be derived from reflectance in the Visible Near InfraRed - Short Wave InfraRed (VNIR-SWIR) wavelength interval. Here we analyze, for the first time, PRISMA data collected in Antarctica. Our scene was acquired on December 2020 over the Nansen Ice Shelf (NIS). Using PRISMA data we estimated various snow parameters (effective grain diameter, snow specific surface area, snow spectral and broadband albedo, bottom of atmosphere snow reflectance, type of impurities in snow and their concentration), and we compared them with data presented in the scientific literature.

## KEYWORDS

remote sensing, albedo, pollution, snow, grain size

## Introduction

Satellite observations of visible and near infrared reflectance represent crucial information for estimating different surface properties of snow and ice, such as snow albedo, snow grain effective diameter, concentration of impurities and liquid water content (Negi and Kokhanovsky 2011; Di Mauro et al., 2017, Haq et al., 2021). In particular, imaging spectroscopy is a powerful tool for mapping surface properties of the cryosphere from space (König et al., 2001; Guanter et al., 2019; Kokhanovsky et al., 2021a; Bohn et al., 2022). With the launch of the PRISMA (PRecursore IperSpettrale della Missione Applicativa) space imaging spectroscopy mission in March 2019, new opportunities for cryosphere monitoring were opened (Di Mauro et al., 2020; Bohn et al., 2022). This mission is promoted by the Italian Space Agency (ASI) (Loizzo et al., 2018; Coppo et al., 2020) and it features a nominal spatial resolution of 30 m in the VNIR-SWIR (Visible Near InfraRed - Short Wave InfraRed) spectral channels. The

measurements are performed in 239 spectral bands covering the 400–2500 nm interval with two instruments. The VNIR spectrometer operates in the 400–1010 nm range with a nominal spectral sampling interval lower than 11 nm and a bandwidth lower than 15 nm, while the SWIR spectrometer operates between 920 and 2500 nm. The two spectrometers share the same entrance telescope. PRISMA radiance data proved to be consistent with field data for agricultural, water and snow surfaces (Giardino et al., 2020; Di Mauro et al., 2020; Cogliati et al., 2021) and already successfully exploited for monitoring water (O’Shea et al., 2021), vegetation (Verrelst et al., 2021) and soils characteristics (Mzid et al., 2022).

The acquisition of optical data in polar areas is challenging. PRISMA, for example, covers areas slightly above  $\pm 70^\circ$  of latitude with relook capability of 7 days, so the observations are not routinely conducted and large areas are missed. Moreover, large solar zenith angles and polar night make the continuous remote observation of snow properties more difficult in these areas (Warren et al., 1998; Pirazzini 2004). Furthermore, few field observations are available (Zibordi and Maracci, 1993; Zibordi et al., 1996; Casacchia et al., 2002; Casacchia et al., 2011; Picard et al., 2016a; Picard et al., 2016b; Di Franco et al., 2022), and mainly used for comparison with satellite estimates (Lupi et al., 2001; Pirazzini 2009).

While most of the surface snow in the interior of the Antarctic Ice Sheet is uncontaminated, on the margins of the continent several processes occur and they can deposit or resurface light-absorbing particles, as observed in different studies (Dadic et al., 2013; Casey et al., 2017; Warren, 2019a; 2019b; Kavan et al., 2020; Di Mauro et al., 2021; Gray et al., 2021; Cordero et al., 2022). Recent observation from the Antarctic Peninsula showed that surface snow may contain cryospheric algae (Gray et al., 2020, 2021) and black carbon (Cordero et al., 2022). Also mineral debris and volcanic tephra can be present on the surface and can produce an overall decrease of spectral albedo of the snow - covered area (Casacchia et al., 2001; Dadic et al., 2013).

The monitoring of the Antarctic Ice Sheet by using hyperspectral data is a Frontier in remote sensing, since potentially it allows to infer snow parameters (e.g. surface impurities) that are not fully investigated until now and can exert a strong role in the future dynamics of the Ice Sheet.

In this context, the objective of this study is to derive, for the first time, snow properties over Nansen Ice Sheet (East Antarctica) using space imaging spectroscopy data. In particular, we exploit PRISMA data with the aim at estimating the effective grain diameter, snow specific surface area, snow spectral and broadband albedo, and bottom of atmosphere snow reflectance. Also we estimate the type of impurities in snow and also their concentration. The spatial resolution of spectral PRISMA measurements is 30 m (the swath width is 30 km). This makes it possible to evaluate snow properties with a spatial detail not accessible for most of modern optical instrumentation

orbiting our planet. In particular, the Ocean and Land Colour Instrument (OLCI) on board Sentinel—3 has 10 times coarser resolution (100 PRISMA pixels within one OLCI pixel). This makes it possible to study the intra-pixel snow property variation for the OLCI and other moderate spatial resolution sensors using PRISMA measurements. Also small scale scene inhomogeneities (say, separate patches of snow containing impurities) can not be detected by the instruments with moderate spatial resolution (e.g., MODIS, S-GLI, OLCI). However, they are clearly observed with the use of high spatial resolution observations such as performed by PRISMA.

## Methods and data

### Retrieval of clean snow properties

In this section we introduce the spectral behavior of clean snow reflectance, with the aim of providing the theoretical basis for the retrieval of snow properties using satellite data. The proposed theory is then applied to PRISMA data and a comparison with the L2d bottom-of-atmosphere reflectance (BOAR) standard product, which includes atmospheric correction, geolocation, and orthorectification (Vangi et al., 2021), performed to evaluate the robustness of the proposed approach.

The snow spectral reflectance  $R$  in the VNIR can be presented in the framework of the asymptotic radiative transfer theory as follows (Zege et al., 1991; Kokhanovsky et al., 2019):

$$R(\mu, \mu_0, \psi) = R_0(\mu, \mu_0, \psi)r^\xi \quad (1)$$

where  $R_0$  is the reflectance of non-absorbing snow layer with the same phase function as an absorbing one,  $r$  is the spherical (white sky) albedo,  $\mu_0$  is the cosine of the solar zenith angle,  $\mu$  is the cosine of the viewing zenith angle,  $\psi$  is the relative azimuthal angle, and

$$\xi(\mu, \mu_0, \psi) = \frac{u(\mu)u(\mu_0)}{R_0(\mu, \mu_0, \psi)} \quad (2)$$

is the directional function, which is determined by the function  $R_0(\mu, \mu_0, \psi)$ . In particular, it follows for the escape function (Sobolev, 1975):

$$u(\mu_0) = \left( \frac{3}{4}\mu_0 + 2 \int_0^1 \overline{R_0}(\mu_0, \mu) \mu^2 d\mu \right), \quad (3)$$

where

$$\overline{R_0}(\mu_0, \mu) = \frac{1}{2\pi} \int_0^{2\pi} R_0(\mu_0, \mu, \psi) d\psi. \quad (4)$$

One can derive for the absolutely white Lambertian surfaces:  $R_0 = 1$  and, therefore (see Eqs 3 and 4,  $u(\mu_0) = a + b\mu_0$ , where  $a = 2/3$  and  $b = 3/4$ . Kokhanovsky et al. (2019) has proposed to

use the constants  $a = 3/7$  and  $b = 6/7$  for the snow albedo retrieval technique, which accounts for the fact that snow is a non-Lambertian surface. In this work, we made use of the following expression (Kokhanovsky et al., 2021a):

$$u(\mu_0) = \frac{3}{5}\mu_0 + \frac{1 + \sqrt{\mu_0}}{3}, \quad (5)$$

which is a valid approximation also at small values of  $\mu_0$  (low Sun typical at polar regions). Equation 1 makes it possible to derive the spherical albedo from the reflection function at a single view analytically:

$$r = \left(\frac{R}{R_0}\right)^{1/\xi} \quad (6)$$

Eqs. 1, 6 are valid for the bottom-of-atmosphere snow reflectance. The reflectance  $R$  as measured on a satellite is influenced also by atmospheric scattering and absorption effects, which must be accounted for. To avoid the necessity of account for generally unknown atmospheric effects, the simplified retrieval approach as discussed below is proposed.

Let us take into account that the snow spherical albedo of clean snow can be presented for weakly absorbing snowpack as (Kokhanovsky et al., 2019):

$$r = \exp(-\sqrt{\alpha L}) \quad (7)$$

where  $\alpha = \frac{4\pi\chi}{\lambda}$  is the bulk ice absorption coefficient,  $\chi$  is the imaginary part of ice refractive index,  $\lambda$  is the wavelength and  $L$  is the Effective Absorption Length (EAL).

Therefore, we can write for the measured reflectance at the pair of near infrared PRISMA channels only weakly affected by the atmospheric scattering and absorption effects in clean polar atmospheres:

$$R_{meas,1} = R_0 \exp(-\xi\sqrt{\alpha_1 L}), R_{meas,2} = R_0 \exp(-\xi\sqrt{\alpha_2 L}), \quad (8)$$

where indices signify the wavelengths used. In this work, we used the PRISMA channels located at  $\lambda_1 = 855nm$  and  $\lambda_2 = 1029nm$  almost free of gaseous absorption. Six et al. (2005) have found that the aerosol optical thickness is smaller than 0.01 at 870 nm at Dome C in Antarctica. Tomasi and Petkov (2005) have found that the molecular optical thickness is smaller than 0.01 in polar regions at wavelength larger than 850 nm. Therefore, aerosol and molecular scattering effects only weakly influence top-of-atmosphere reflectance over snow at wavelengths larger than 850 nm in most of cases. Also atmospheric absorption effects are weak at these channels.

It follows from Eq. 8 neglecting light scattering and absorption effects in clean polar air at selected wavelengths (Kokhanovsky et al., 2019):

$$R_0 = R_{meas,1}^\epsilon R_{meas,2}^{1-\epsilon}, L = W\xi^{-2} \ln^2\left(\frac{R_{meas,2}}{R_0}\right) \quad (9)$$

where  $\epsilon = \frac{1}{1-b}$ ,  $b = \sqrt{\frac{\alpha_1}{\alpha_2}}$ ,  $W = 1/\alpha_2$ . Taking into account the data for the spectral ice refractive index at 865 and 1029 nm (Warren and Brandt, 2008) one derives:  $\epsilon = 1.47$ ,  $W = 35.29mm$ .

One can see that PRISMA measurements at two near infrared channels make it possible to determine the parameters  $R_0$  and  $L$  and, therefore, we can also estimate spectral spherical albedo of clean snow at any wavelength using Eq. 7. Simultaneously, it is possible to determine the bottom of-atmosphere (BOA) snow surface reflectance (see Eqs 1, 7)

$$R = R_0 \exp(-\xi\sqrt{\alpha L}) \quad (10)$$

and plane (black sky) snow albedo (Kokhanovsky et al., 2019)

$$r_p = \exp(-u(\mu)\sqrt{\alpha L}) \quad (11)$$

or

$$r_p = r^u(\mu_0) \quad (12)$$

at any wavelength in the visible and near infrared. An important point is that atmospheric scattering and absorption (say, by water vapor, oxygen, and ozone molecules) effects, which are of importance in the visible, are accounted for automatically in our atmospheric correction scheme. Also multi-view remote sensing instruments and observations generally used to determine albedo are not required. The technique described above has been already applied to MSI/S-2 and OLCI/S-3 measurements and close correspondence to ground measurements have been found for clean snow cases common for remote polar areas (Kokhanovsky et al., 2019, 2020; 2021b).

The value of EAL can be used to estimate other snow parameters such as the effective grain diameter (EGD, mm)  $d$ , the snow specific surface area (SSA)  $\sigma$ , and snow broadband albedo (BBA)  $r_b$  (see Table 1).

## Retrieval of snow properties: Accounting for impurities

In the case of snow containing light-absorbing impurities, the technique described above must be modified. In particular, we assume that the spectral snow reflectance can be presented in the following form (Kokhanovsky et al., 2018; Kokhanovsky et al., 2021a):

$$R = R_0 \exp\left(-\xi\sqrt{(\alpha + cf\tilde{\lambda}^{-m})L}\right) \quad (13)$$

where

$$f = Qk(\lambda_0), \quad (14)$$

where  $\tilde{\lambda} = \lambda/\lambda_0$ ,  $c = \frac{c_p}{c_i}$  is the relative volumetric concentration of snow impurities,  $c_p$  is the volumetric concentration of snow impurities,  $c_i$  is the volumetric concentration of ice grains,  $Q$  is the inverse absorption enhancement factor assumed equal to 0.6 in this work, which is close to the average value of this

TABLE 1 The relationships of various snow parameters with the value of the effective absorption length L for the case of clean snow (case 1 snow).

Quantity	Symbol, dimension	Equation	Parameters	Source
Effective Grain diameter (EGD)	$d, mm$	$pL$	$p = 0.0625$	Kokhanovsky et al. (2019)
Specific Surface Area (SSA)	$\sigma, m^2/kg$	$q/L$	$q = 0.1047 m^3/kg$	Kokhanovsky et al. (2019)
Broadband Albedo (BBA) (400–2500 nm)	$r_b$	$a+bexp(-u(\mu_0)\sqrt{cL})$	$a = 0.5271, b = 0.3612, c = 0.2350cm^{-1}$	Kokhanovsky (2021c)

TABLE 2 Values of the constants used in Eq. 18.

$i$	0	1	2
$b_i$	10.916	-2.0831	0.5441

parameter for various snowpacks measured by Libois et al. (2014),  $k(\lambda_0)$  is the volumetric absorption coefficient of impurities at the wavelength  $\lambda_0$  defined as the ratio of average absorption cross section of particles to their average volume (Kokhanovsky, 2021c). The external mixture of ice grains and impurities is assumed. The parameters  $L$  and  $R_0$  can be derived as discussed above assuming that the concentration of impurities is relatively weak and does not influence snow reflectance at channels above 850 nm. This is generally the case in Antarctica (Kokhanovsky et al., 2021). It follows from Eq. 13 that the snow reflectance is determined by the size of ice grains, the relative volumetric concentration of impurities, the volumetric absorption coefficient of impurities at the wavelength  $\lambda_0$  (say, 500 nm), and the absorption Angström parameter  $m$ .

The absorption of light by ice grains is weak (term  $\alpha L < 1$ ) in the visible and it follows at two wavelengths in the visible (e.g., PRISMA 411 and 508 nm channels):

$$R_1 = R_0 \exp\left(-\xi\sqrt{cL}f\tilde{\lambda}_1^{-m}\right), R_2 = R_0 \exp\left(-\xi\sqrt{cL}f\tilde{\lambda}_2^{-m}\right) \tag{15}$$

Therefore, we can derive from Eq. 15:

$$m = \frac{\ln z}{\ln s} \tag{16}$$

$$c = \frac{\tilde{\lambda}_1^m \ln^2 \tilde{R}_1}{fL\xi^2} \tag{17}$$

where  $z = (\ln \tilde{R}_2 / \ln \tilde{R}_1)^2$ ,  $s = \lambda_1 / \lambda_2$ ,  $\tilde{R}_j = R_j / R_0$ . Eqs. 16, 17 make it possible to determine both  $m$  and  $c$  from dual-wavelength PRISMA measurements in the visible. The retrieved value of  $m$  indicates the type of a impurities being close to one for black carbon and taking larger values for dust (Kokhanovsky, 2021c).

Kokhanovsky et al. (2021b) has proposed the following equation for the value of  $k(\lambda_0)$  (1/mm) in terms of  $m$  (see Table 2):

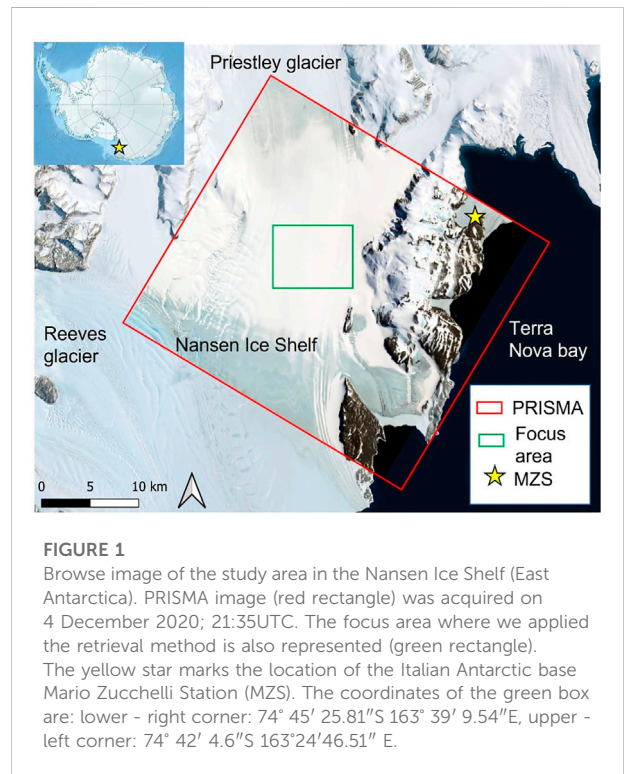


FIGURE 1 Browse image of the study area in the Nansen Ice Shelf (East Antarctica). PRISMA image (red rectangle) was acquired on 4 December 2020; 21:35UTC. The focus area where we applied the retrieval method is also represented (green rectangle). The yellow star marks the location of the Italian Antarctic base Mario Zucchelli Station (MZS). The coordinates of the green box are: lower - right corner: 74° 45' 25.81" S 163° 39' 9.54" E, upper - left corner: 74° 42' 4.6" S 163° 24' 46.51" E.

$$k(\lambda_0) = \sum_{i=0}^2 b_i m^i. \tag{18}$$

The retrieved values of  $m, L, c, R_0$  can be used to determine the snow spectral reflectance at any wavelength using Eq. 13. Also the spherical albedo can be derived:

$$r = exp\left(-\sqrt{(\alpha + cf\tilde{\lambda}^{-m})L}\right) \tag{19}$$

Equation 7 follows from Eq. 19 at  $c = 0$ . The plane albedo is derived using Eqs 12, 19. The values of EGD and SSA are derived as specified in Table 2. The broadband albedo (0.4–2.5  $\mu$ m spectral range) of snow at the cosine of the solar zenith angle  $\mu_0$  can be derived using the following analytical parameterization (Kokhanovsky et al., 2021b):

$$BBA = \frac{\exp\{-u(\mu_0)\sqrt{p_{vis}L + wcfLe^m}\} + Q(\alpha_{0}^{nir} + \alpha_1^{nir} \exp(-u(\mu_0)\sqrt{p_{nir}L}))}{1 + Q} \tag{20}$$

TABLE 3 Retrieved parameters for the selected cases.

N	EGD, mm	SSA, $m^2/kg$	RMC, ppm	BBA	$m$	$R_0$	EAL, mm
1	0.66	9.85	0.16	0.78	8.47	0.97	10.63
2	0.78	13.74	0.84	0.80	7.17	0.99	7.62
3	0.61	10.72	0.33	0.78	7.93	1.00	9.78
4	0.35	18.44	0.08	0.82	8.97	0.95	5.68
5	0.59	11.08	0.02	0.79	10.17	0.93	9.45
6	0.60	10.85	0.25	0.78	8.23	1.01	9.65
7	0.59	11.10	0.61	0.78	7.49	1.01	9.43
8	0.53	12.40	0.88	0.79	7.13	1.01	8.44

where  $p_{vis} = 0.08m^{-1}$ ,  $w = 0.8475$ ,  $\gamma = 0.7426$ ,  $\alpha_0^{nir} = 0.2335$ ,  $\alpha_1^{nir} = 0.56$ ,  $p_{nir} = 32.7 m^{-1}$ ,  $Q = 1.08$ . The spherical (white sky) BBA follows from Eq. 20 at  $u = 1$  (Kokhanovsky et al., 2021b).

## The application of the snow retrieval technique to the PRISMA data over Nansen Ice Shelf

We have applied the theory described above to the PRISMA atmospherically corrected and orthorectified BOAR (L2d product) for the Nansen Ice Shelf (NIS) region in Antarctica (Figure 1) (Frezzotti, 1993) and only snow-covered areas under clear sky conditions have been processed (green rectangle). PRISMA acquisition occurred on 4 December 2020 (21:35 UTC) during the austral summer. The solar zenith angle was  $58^\circ$  and the observation has been performed in the direction close to nadir. The cloud screening has been performed using visual inspection of PRISMA imagery.

The results of retrievals for the randomly selected eight PRISMA pixels over snow are given in Table 3. The relative mass concentration (RMC) given in Table 3 is calculated as follows:  $c_m = c \frac{\rho_p}{\rho_i}$ , where  $\rho_p$  is the bulk impurity density and  $\rho_i$  is the bulk ice density. It has been assumed that  $\rho_p = 2.65g/cm^3$  (as for dust),  $\rho_i = 0.917g/cm^3$ .

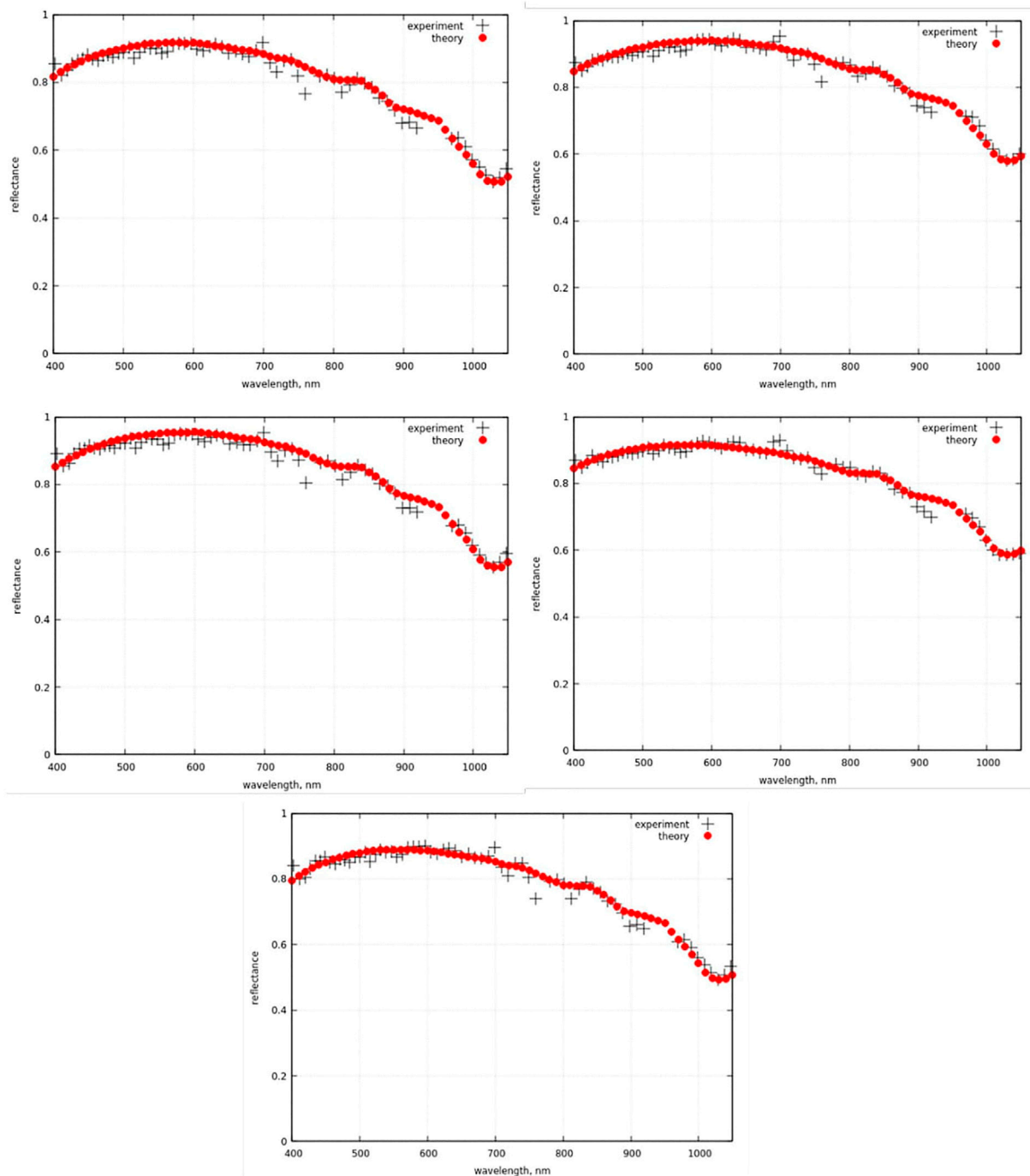
The comparison of PRISMA L2d BOAR product with the spectral reflectance computed using Eq. 13 and parameters presented in Table 3 in the spectral range 400–1030 nm (used in the retrievals) is given in Figure 2. The spectral ice refractive index tabulated by Picard et al. (2016a) (at the wavelengths <600 nm) and Warren and Brand, (2008) (for the longer wavelengths) has been used. It follows from Figure 2 that Eq. 13 describes spectral PRISMA reflectance over snow in Antarctica for the spectral region 400–1030 nm in correct way. The decrease of measured spectral reflectance towards UV seen in Figure 2 is a clear indication of the snow containing light-absorbing impurities (under assumption that the atmospheric correction of PRISMA data used by us (L2d product) has been performed in correct way).

We show the spectral vertical optical density (VOD) of water vapor at the assumption that the vertical water vapor column is  $1.301 \times 10^{22} molecules/cm^2$  in Figure 3. It follows that the deviations of theory and experiment occur mostly in the region of the water vapor absorption, which points out on uncertainties of gaseous absorption correction of PRISMA imagery. This also means that Eq. 13 can be used in atmospheric correction procedures for PRISMA imagery over snow.

The comparison of the model and measurements for the case 1 in Table 3 at the whole PRISMA spectral range is given in Figure 4. The general decrease of reflectance with the wavelength is well captured by the theory, and resembles field spectroscopy observation collected in this area (Zibordi et al., 1996; Casacchia et al., 2001). However, there are deviations of the theory and experiment around 1080 nm and 1250nm, which could be due to snow vertical inhomogeneity not captured by the model or by surface heterogeneity included in PRISMA pixels. The discrepancy around 1150 nm is related to the strong absorption by water vapor. The discrepancy above 1500 nm are due to limitations of the model, which is valid only for weakly absorbing bulk ice absorption bands for vertically homogeneous snow and also due to different light penetration depths in vertically inhomogeneous snow by radiation with different wavelengths (Zhou et al., 2003). These discrepancies deserve further investigation, such as the direct comparison of PRISMA products with synchronous field spectroscopy data.

We also show the theoretical spectral reflectance for pure snow (case -1 snow) in absence of impurities in Figure 4. One can see that impurities play a role for the wavelengths smaller than approximately 550nm, where the maximum of the incident solar radiation is located. The intercomparison of the theory and experiment for the last three cases shown in Table 3 is shown in Figure 5. We can see that the spectral differences of theory and experiment in Figures 4, 5 are similar. It follows from Figure 6 that the difference between theory and experiment in the vicinity of ice absorption band around 2250nm, where water vapor absorption can be neglected, is reduced if the effective grain diameter equal to 0.24 mm is used. This is generally true also for



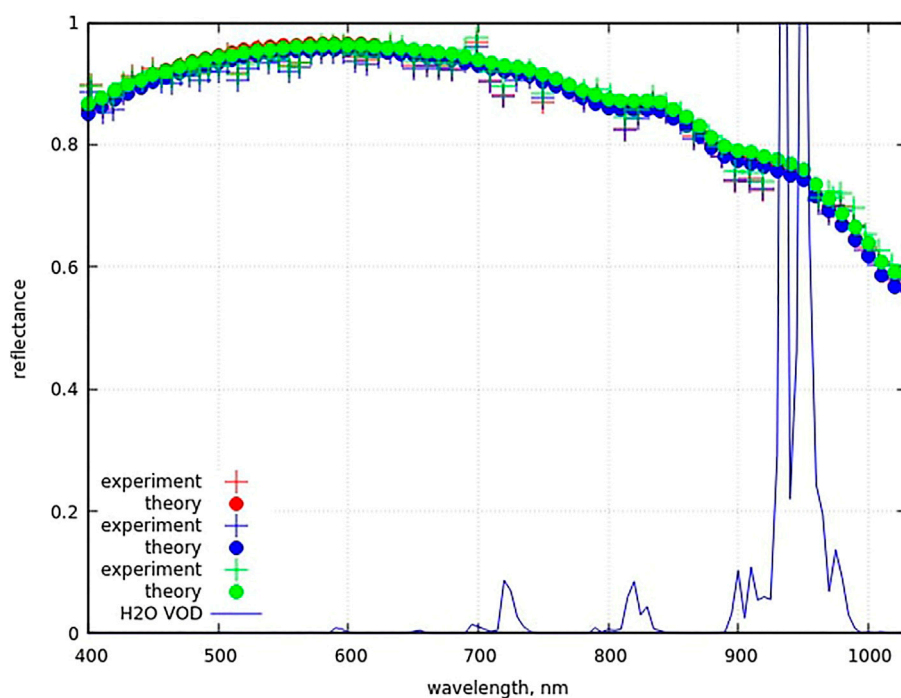


**FIGURE 2**

Comparison of simulated reflectance with satellite measurements for the first five cases shown in Table 4. The sequence of plots coincides with the sequence of lines in Table 3.

all wavelengths larger than 1500 nm as illustrated in Figure 6. The discrepancy around 1800 nm is due to strong absorption by water vapor, probably not well captured by the PRISMA atmospheric correction scheme during the generation of the

BOAR L2d product. The same is true for the region close to 1400 nm. The discrepancy around 1250 nm can be removed, if the effective grain diameter equal to 0.38 mm is used (see Figure 7). However, in this case the differences between



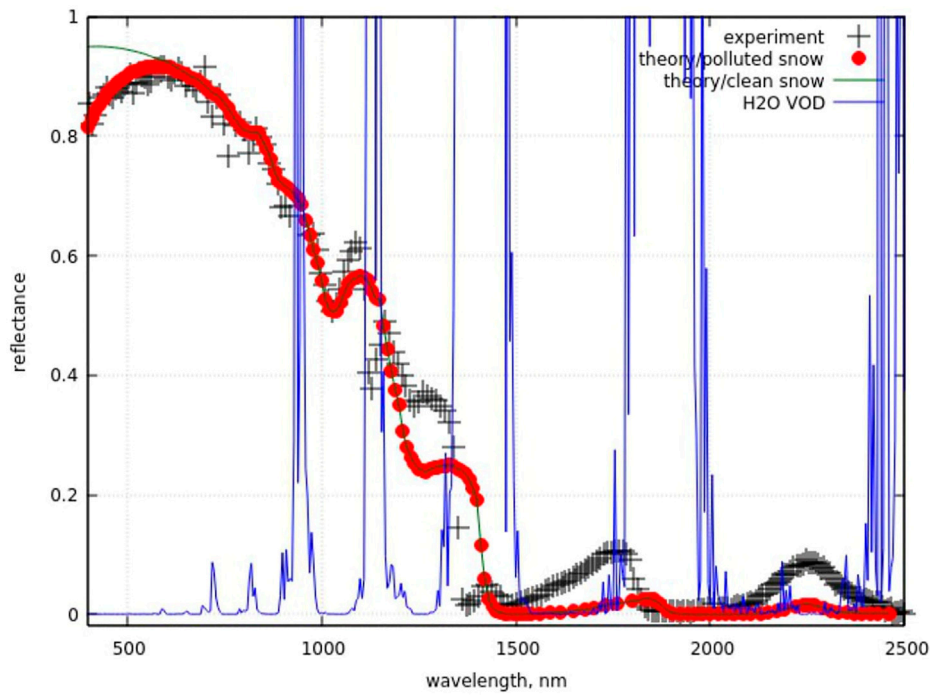
**FIGURE 3**

Comparison of theory and satellite measurements for the last cases shown in Table 3. The sequence of data coincides with the sequence of lines in Table 3. We also show the vertical optical density of water vapor at the assumption that the vertical water vapor column is  $1.301 \times 10^{22} \frac{\text{molecules}}{\text{cm}^2}$  (courtesy of L. Lelli).

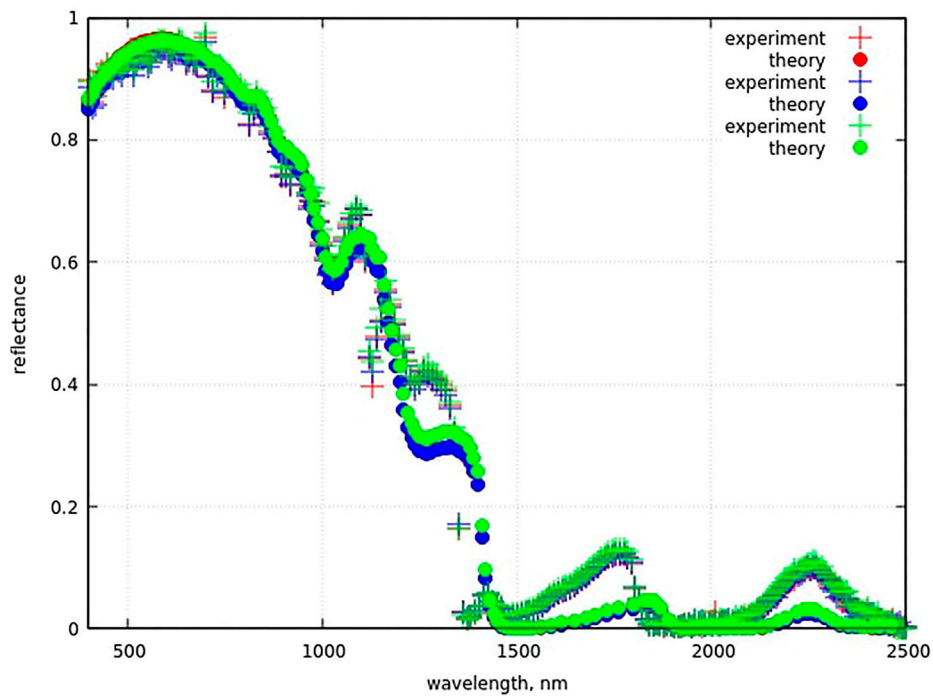
model and PRISMA data in the spectral ranges around 1030 and 2250 nm (almost free of gaseous absorption) increase. This points out to the fact that the Nansen Ice Sheet is characterized by the vertical inhomogeneity of snow properties and the PRISMA channels are sensitive to the vertical structure of snow layers. Our model has been developed specifically for the case of vertically homogeneous snow layers. Therefore, it cannot capture the spectral effects, which are due to different penetration depths of radiation in snowpack (Kokhanovsky, 2022). As a matter of fact the effective grain diameter derived from 1030 nm measurements correspond to the averaging over the larger snow volume in comparison with the measurements at 2250 nm, which give the effective grain diameter close to the surface. We may conclude that the effective grain diameter (for the case 7 shown in Table 3) is 2.5 times smaller at the surface as compared to that retrieved from measurements at 1030 nm corresponding to the larger penetration depth. This means that the size of crystals increases with the depth in the Nansen Ice Sheet. This feature has already been reported (Grenfell et al., 1994) for the central Antarctica and can be explained by the snow metamorphism processes. In particular, Grenfell et al. (1994) has assumed in their two-layer snow model that the top EGD is about 3.3 times smaller as compared to that in deeper layers sensed by the

wavelength around 1030 nm. Also Grenfell et al. (1994) has measured snow grain vertical diameter as function of snow depth. They have found that the effective grain size can change in three times at the depth 0.5–5 cm as compared to the size of grains at the very top of snow layer. This is close to the estimations derived by us (2.5) and also that (3.3) proposed by Grenfell et al. (1994).

After testing the robustness of the proposed method, we have applied the technique to the central part of the Nansen Ice Sheet covered by snow on the green box depicted in Figure 1. The reflectance at 411 and 1029 nm for the studied area are given in Figure 8, as example. One can see that the spatial distribution of reflectance at 1029 nm is quite smooth. This is not the case for the measurements at 411 nm, where some stripes can be seen. These stripes propagate also to the retrieved parameters (see Figure 8), and they can be due to the presence of sastrugi (Warren et al., 1998) or other horizontal inhomogeneities of Nansen Ice Shelf. Various structures on snow surfaces are in fact well known for their impact on snow and ice albedo (Lhermitte et al., 2014). The average values of the retrieved parameters and coefficients of variations of various parameters for the 6 kmx6 km scene studied are given in Table 4. Unfortunately, the validation data for the site at the moment of measurements are not available.

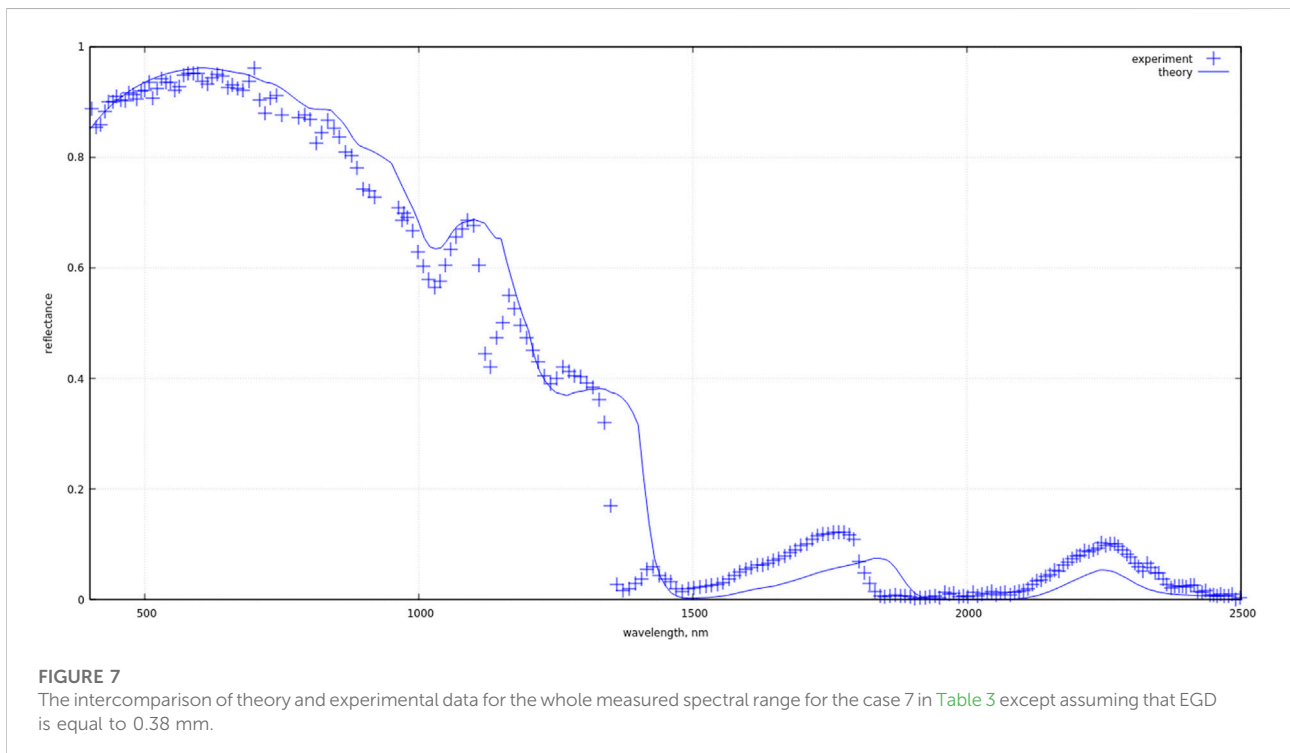
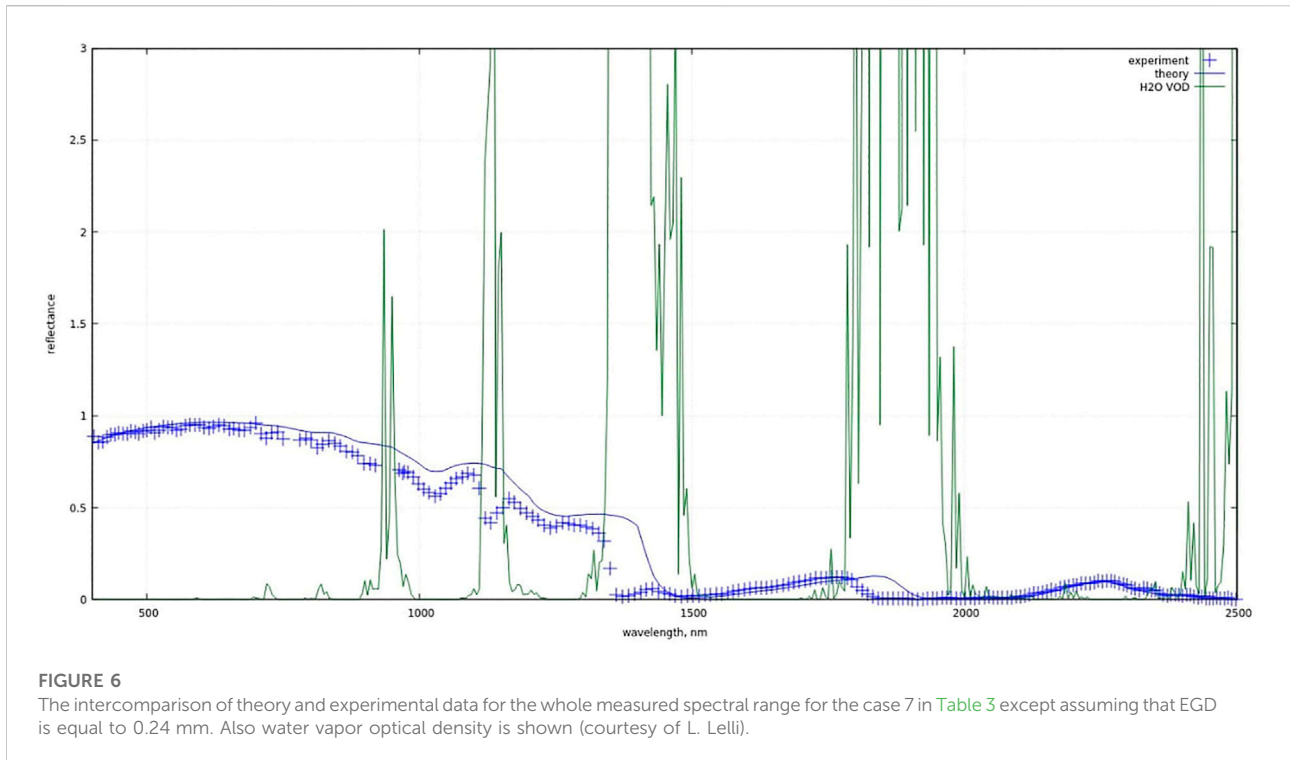


**FIGURE 4**  
 Comparison of theory and experimental data for the whole measured spectral range (for the case 1 in Table 3). We also show the vertical optical depth of water vapor (courtesy of L. Lelli). The solid line corresponds to the calculation in the absence of snow impurities (pure snow).



**FIGURE 5**  
 The intercomparison of theory and experimental data for the whole measured spectral range (for the cases 6–8 in Table 3).





One can see that the average grain diameter is close to 0.51 mm. The results obtained from the 42 sites in Antarctica show that near the surface the mean convex diameter is spatially homogeneous and

on the order 0.2–0.4 mm (Gay et al., 2002). However, the cases with diameters in the range 0.4–1 mm have been found as well. Therefore, our estimation is plausible. The specific snow surface

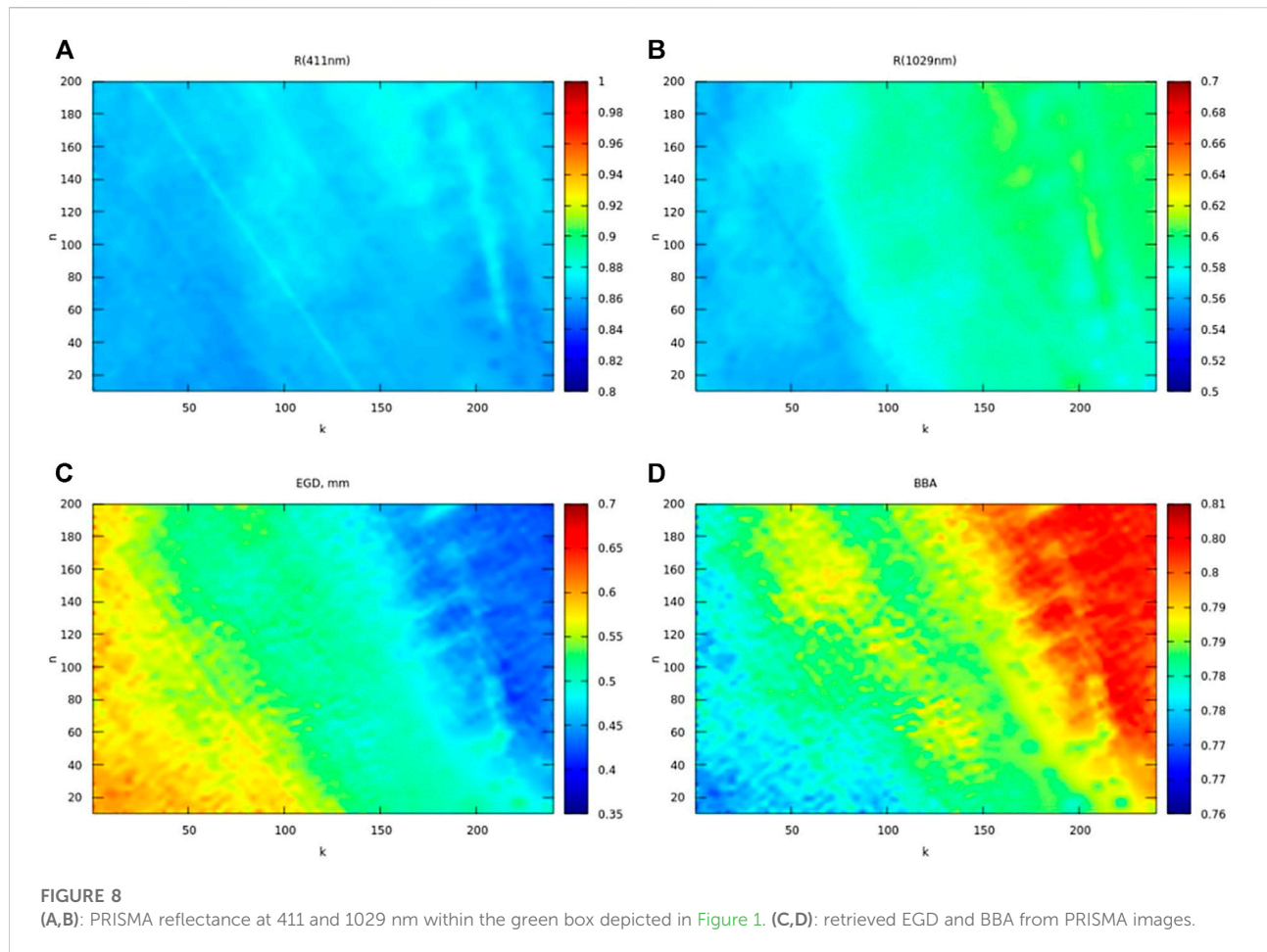


TABLE 4 Average values of retrieved parameters and reflectance at R (411 nm) and R (1029 nm) for the focus area.

	EGD [mm]	SSA [ $m^2/kg$ ]	$c_m$ [ppm]	BBA	m	$R_0$	R (411 nm)	R (1029 nm)
average value	0.52	12.9	0.51	0.79	7.6	1.0	0.86	0.58
coefficient of variation, %	10.6	28.4	40.3	1.0	4.9	0.8	0.6	2.8

area found by us is  $12 m^2/kg$ , which is 2–3 times smaller than that measured at Dome C (Libois et al., 2015). This can be explained by the proximity of ocean and also by generally larger grain sizes. BBA values (average = 0.78) showed in Figure 8 are in agreement with recent remote sensing observations of snow albedo in the Antarctic transition zone (Traversa et al., 2019).

We also have found that snow in the area may contain dust particles due to weathering of nearby rocks (see Figure 1). The average concentration of dust particles as derived from satellite imagery is 0.5ppm. Unfortunately, we have no information on the measurements of dust load in snow of Nansen Ice Shelf.

However, Lim et al. (2014) has reported the values of dust concentration in the range 0.1–10 ppm (0.23–2.3 ppm for Himalaya) in remote mountainous regions around the globe. Our results are closer to the lower boundary of this variability. Also atmospheric correction can induce uncertainties in wavelengths lower than 550 nm, where the impact of dust is marked. Furthermore, dust concentration <1 ppm are often considered as “clean snow” in alpine and remote areas (Di Mauro et al., 2015). Nevertheless, we cannot exclude that mineral dust has been deposited from the erosion of the surrounding moraines and nunataks (Casacchia et al., 2002).

Zege et al. (2011) have suggested that the accuracy of snow impurity retrieval decreases with decrease of impurity load being about 10% for their algorithm at 1ppm of soot. It should be pointed out that impurity content is usually in the range 0.003–0.03ppm in Arctic and subarctic snow (Warren, 2013) and even lower in Antarctic snow (Warren and Clarke, 1990). Such low impurities load values can not be detected using spaceborne observations (Zege et al., 2011; Warren, 2013).

## Conclusion

In this study, we have optimized a snow retrieval approach to PRISMA data and we provide satellite estimates of different snow properties in the Nansen Ice Sheet. The proposed approach made it possible both to derive snow properties and to model PRISMA spectral reflectance over snow covered areas. We have found some discrepancies between the standard L2d PRISMA BOAR product and the reflectance at selected spectral bands simulated with the proposed model. Further investigations are still needed to better understand these differences and we believe that the atmospheric correction of PRISMA imagery over snow should be improved in future (in particular, regarding the complex scattering processes that may occur over snow-covered complex terrains).

The derived average effective snow grain radius for the selected area is close to 0.25 mm, which is similar to the average grain sizes commonly measured *in situ* in Antarctica area (Gay et al. 2002). Also the average specific snow surface area was close to 13  $m^2/kg$ , is in the range reported by Linow et al. (2012) for firn in Antarctica. The average broadband albedo is 0.79, which is close to the values reported for Antarctica by Traversa et al. (2019, 2021) in same snow conditions.

The average value of impurities load is around 0.5ppm. Due to the relatively high absorption Angström parameter  $m$  (see Table 4), this value can be attributed to dust from neighbouring rocks and not to soot. It is expected that the contamination of snow by soot is very low in Antarctica (below 0.0003 ppm (Warren and Clarke, 1990)) and cannot be detected using spaceborne observations. In this context, it should be pointed out that inaccuracy in atmospheric correction, presence of mixed pixels, surface melting water, and blue ice can lead to the wrong detection of dust load in pristine snow on the surface of the Nansen Ice Shelf. Therefore, our retrievals of dust load shall be treated with some precaution. Future field campaigns are needed in order to perform ground measurements of impurities load and type at the site. In summary, this study demonstrates the potential of PRISMA imaging spectroscopy for detecting snow surface properties in the Antarctic Ice Sheet. The method presented in this paper can be directly applied to determine the spatial and

temporal evolution of snow surface properties using PRISMA standard products in remote areas.

## Data availability statement

The raw data supporting the conclusions of this article will be made available by the authors, without undue reservation.

## Author contributions

AK: theory, conceptualization. BM and RC: experimental measurements. AK, BM, and RC: writing of the paper. All authors reviewed and approved the final version.

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## Conflict of interest

Author AK was employed by company Brockmann Consult GmbH.

The remaining authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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