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Sliding mode control based on maximum power point tracking for dynamics of wind turbine system

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This article presents a proportional-integral sliding mode control (PI-SMC) approach for a two-mass variable speed wind turbine (VSWT) system. Most studies on wind turbines typically focus mainly on the electromagnetic part of the generators, or even on the high-speed part, considering the shaft stiffness as negligible. However, the generator torque is actually driven by the aerodynamic torque, and a two-mass system like the one studied here plays the role of a transmission element for this power. To address this challenge, the problem of low power generation resulting from wind speed variability is tackled by designing a PI-SMC control law, capable of controlling the mechanical turbine model that optimizes power and torque by tracking the maximum power point (MPPT) for rotational speed and aerodynamic power. To validate the developed theoretical results, an application of the wind turbine system is simulated in Matlab/Simulink, for a particular case. The control used is capable of satisfying the dynamic performance of the systems.

KEYWORDS

variable speed wind turbine, two-mass gear train system, maximum power point tracking, sliding mode control, proportional integral controller

1 Introduction

Renewable energy is essential for creating a sustainable and environmentally friendly future, as it significantly reduces greenhouse gas emissions and dependence on finite fossil fuels. By harnessing natural resources such as sunlight, wind, and water, renewable energy technologies mitigate the adverse effects of climate change, improve air quality, and enhance energy security (Kamal and Ibrahim, 2018). Furthermore, the transition to renewable energy fosters economic growth through the creation of green jobs and the development of new industries. This shift not only ensures a more resilient and diverse energy supply but also promotes innovation and long-term environmental stewardship, essential for the well-being of current and future generations. Wind energy has become increasing interest in recent years as a promising and sustainable renewable energy source. Recent research has highlighted the growing importance of wind energy as a clean and renewable power source, particularly in light of concerns about climate change and natural resource depletion

(Martin et al., 2023). With the rapid evolution of wind turbine technology, it has become crucial to design more powerful and intelligent control systems to improve their performance, reduce costs, and increase reliability (Alsayouf, 2011; Dhanraj et al., 2022a; Abdelrahim and Almakhlis, 2023; Jaikrishna et al., 2023; Sethi et al., 2023). To achieve maximum energy extraction from the wind, variable-speed wind turbines (VSWT) have been developed to operate over a wide range of speeds. However, the significant challenge of controlling the electrical generator in response to wind speed fluctuations remains (Dhanraj et al., 2022b; Chang et al., 2022).

In the field of wind energy conversion technologies, various approaches have been explored in recent years to optimize aerodynamic power. Classical controllers, such as the proportional-integral-derivative control (PID), have been widely used, as evidenced by numerous studies (Yang et al., 2017; Lisitsyn and Zadorozhnaya, 2019; Alqudah, 2020; Frikh et al., 2021). While many control approaches face issues like the runaway phenomenon, research has proposed enhancements to address these challenges. Optimal control methods like Linear Quadratic Regulator (LQR) and Linear Quadratic Gaussian have also been employed (Jeon and Paek, 2021; Zgarni and ElAmraoui, 2021; El Beshbichi et al., 2022). However, recent studies have indicated that these methods do not show improved performance compared to other controllers. On the other hand, Sliding Mode Control (SMC), a crucial transient mode for Variable Structure Control, has been utilized to improve robustness (Lu and Spurgeon, 1999; Utkin, 2004; Sira-Ramírez, 2015; Levant and Livne, 2016). The original work on SMC was primarily conducted by Soviet control experts (Petrov et al., 1964; Itkis, 1976; Zinober, 1994).

Modern wind turbines incorporate sophisticated power electronics to ensure efficient generator control and operation compatible with the electrical system (Ko et al., 2008; Durgam et al., 2022; Yahyaoui et al., 2022; Kesavan et al., 2024). However, recent studies have emphasized the importance of developing advanced control strategies to mitigate uncertainties in wind turbine modeling (Dao et al., 2020; Fekih et al., 2022; Gonzaga et al., 2022). These strategies aim to ensure an optimized and stable operational state despite the erratic and inconsistent nature of the energy source, while considering the Betz limit constraint (Gbadega and Saha, 2021). Overall, the development of robust control mechanisms that account for uncertainties in wind turbine modeling and enhance performance is essential for the successful implementation of wind energy conversion systems.

Therefore, to achieve the optimal production point of the wind system, a nonlinear control approach is required. Several robust control techniques have been developed to optimize desired wind turbine parameters, especially aerodynamic power and rotor speed (Shaker and Patton, 2014; Azar and Serrano, 2015; Gao and Gao, 2016; Meghni et al., 2017; Meghni et al., 2018; Abdelmalek et al., 2018; Gorripotu et al., 2019; Yin et al., 2019; Jiao et al., 2020; Saha et al., 2022). A promising control alternative is SMC, which has been proposed in numerous studies (Torchani et al., 2016; Ammar et al., 2019; Berrada et al., 2020; Colombo et al., 2020; Deng and Xu, 2022). In this context, improving effective control approaches for wind turbine systems is crucial to enhance their performance and energy generation efficiency. Wind speed variability poses a significant challenge to wind power generation. This paper addresses this

challenge by introducing a PI-SMC approach for a VSWT to enhance its aerodynamic power. The primary goal of this work is to create a control strategy that optimizes power and torque through Maximum Power Point Tracking (MPPT) for rotational speed and aerodynamic power. Developing a nonlinear model of wind turbine dynamics that considers wind speed variability is crucial. The PI-SMC technique provides a reliable solution to address wind power generation challenges and enhance wind turbine system performance. This technique utilizes SMC for MPPT and PID for system output stabilization (Singh et al., 2017; Xia et al., 2021; Chatri et al., 2022; Chehaidia et al., 2022; Periyanyagam and Joo, 2022).

The development of a SMC strategy for a VSWT is critical in achieving maximum aerodynamic power. The surface of the SMC plays a vital role in minimizing the tracking error and reducing the control system's chattering. The SMC technique also offers robustness to system uncertainties, making it an ideal control strategy for wind turbines. By using a SMC approach, the wind turbine can reach MPPT with high accuracy, thus ensuring the optimal energy production efficiency. By optimizing power and torque, the wind turbines performance is significantly improved, making it a reliable source of renewable energy.

The purpose of this article is to establish a PI-SMC control for VSWT system. The key point is to demonstrate the ability of this control to control the system from an arbitrary initial condition in a relatively short time while preserving system stability. The turbine is considered as a two-mass mechanical transmission system, which imposes a more or less slow response. Additionally, the main control is materialized through aerodynamic power, which tends to drive the system into an imposing dynamic to rotate the generator shaft. The generator, through its electromagnetic power, plays the role of a disturbance opposing the control that gave rise to it.

This work is arranged as follows: Section 2 will present the turbine model using development of the aerodynamic power relations and the power coefficient of the turbine as a function of wind speed and power. Subsequently, in Section 3, the modeling of the mechanical part of the turbine will be established. The aerodynamic turbine is considered as a two-mass gear train system, a transmission model. This modeling is based on different equations of the system's dynamics, which will then allow for the establishment of a state-space modeling. The objectives of the proposed control will be mentioned in Section 4, specifying the parameters we will work on and potentially the commands to be developed for the turbine system. In Section 5, the proposed SMC scheme for the two-mass transmission turbine system will be established, along with the verification of the system's stability using this control. The integration of the Proportional integrator controller component with the SMC, as well as the stability verification, will be addressed in Section 6. To apply the theory of this work, numerical simulations of the turbine system using various controls, including the PI-SMC control, will be presented in Section 7. Lastly, a conclusion will be given in Section 8.

2 Wind turbine model

As established in Zheng et al. (2009), the wind power across area A_v , is given as

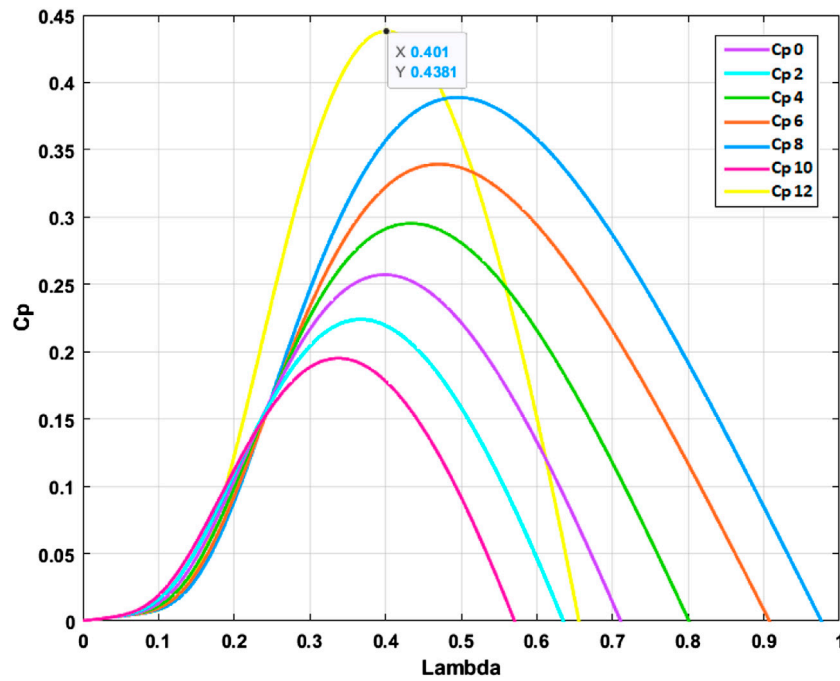


FIGURE 1
Cp against λ and β.

$$P_w = \frac{1}{2} \rho A v^3 \tag{1}$$

where v denotes the wind speed and ρ represents the air density. Then, the aerodynamic power received by the wind turbine is then:

$$P_a = \frac{1}{2} \rho \pi R^2 C_p(\lambda, \beta) v^3 \tag{2}$$

The rotor radius is denoted by the symbol R . Meanwhile, the aerodynamic efficacy of a wind turbine is expressed by C_p , which is influenced by the turbine’s unique characteristics. This power coefficient is generally bounded by a maximum limit called the Betz limit, which is 59.3% (Freris, 1990). The blade pitch attack angle is symbolized by β , while λ refers to the tip speed ratio, or the ratio between the blade speed and wind speed. Figure 1 illustrates the $C_p(\lambda, \beta)$ with respect to tip speed ratio and pitch angle.

To calculate the power coefficient, one must divide a certain ratio:

$$C_p = \frac{P_a}{P_{wind}} \tag{3}$$

The power that the wind turbine receives can be stated as follows:

$$P_a = w_t T a \tag{4}$$

where w_t is the rotor angular speed at the wind turbine. From Eqs 3, 4, the aerodynamic torque can be realized as:

$$T_a = \frac{\pi}{2\lambda} \rho R^3 C_p(\lambda, \beta) v^2 \tag{5}$$

The C_p coefficient or the Betz limit, is typically approximated using numerical methods (Alami et al., 2016; Singh et al., 2017). This work proposes employing the following forms of the C_p coefficient:

$$C_p(\lambda, \beta) = 0, 22 \left(\frac{116}{\lambda'} - 0, 4\beta - 5 \right) e^{\left(\frac{-12\beta}{\lambda'} \right)} \tag{6}$$

with $\frac{1}{\lambda'} = \frac{1}{\lambda + 0.08\beta} - \frac{0.035}{\beta^3 + 1}$.

3 Mechanical part of the turbine modelling

In this section, we describe the mechanical modelling of the wind turbine system, consisting mainly of the turbine and the gearbox, as shown in Figure 2. The two-mass system is the most used approach to express a wind turbine system (Boukhezzar and Siguierdidjane, 2011; Habibi et al., 2017), which comprises the blades and gearbox. As a result, the proposed two-mass model consists of two main rotors, which represent the wind turbine and the generator. Between these two parts, a flexible shaft is mounted to connect the two components of the wind turbine, namely the aerodynamic turbine side and the generator side. Furthermore, on the generator side, the modeling is based on the arrangement of the moment of inertia of the gears and the stiffness of the high-speed shaft w_{hs} . The latter will be considered negligible and subsequently only the inertia J_g and the effect of the high-speed damping B_g will be included in the modeling. On the turbine side, the low-speed shaft is subject to a damping B_{ls} , it connects the rotor which is equipped with an inertia J_r and a damping B_r and the gearbox at the same time. It should be noted that the moments of

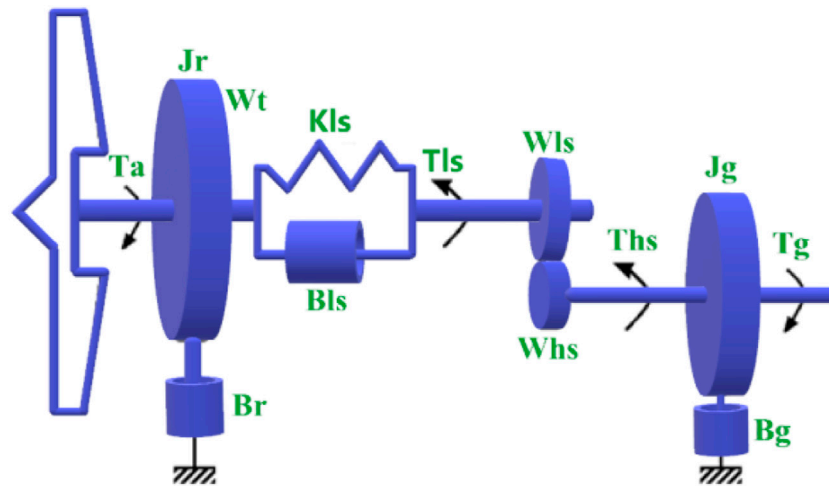


FIGURE 2 Two-mass gear model.

inertia of the shafts and the gearbox will be neglected as they do not have a significant impact on the dynamic behavior of the system.

This system is used to further model the wind turbine and establish a mathematical dynamical model of the control system, which is applicable to wind turbines of different dimensions.

The similar approach is applied to the multiplier, and the different relationships are expressed as follows after establishing Eqs 5, 6 and by applying various energy principles to the rotor and Newton's second law, we obtain:

$$J_r \dot{w}_t + B_r w_t = T_a - T_{ls} \tag{7}$$

where J_r is the rotor moment of inertia, w_t is the rotor angular speed, B_r is the rotor damping effect, T_a is the applied torque on the rotor and T_{ls} is the low speed shaft torque.

The low speed shaft results from the torsion and friction effects due to the difference between w_{topt} and w_{ls} :

$$T_{ls} = J_{ls} \dot{w}_{ls} + B_{ls} (w_t - w_{ls}) + K_{ls} (\theta_t - \theta_{ls}) \tag{8}$$

where J_{ls} represents the driver moment of inertia, w_{ls} denotes the angular speed of the low speed shaft, K_{ls} expresses stiffness of low speed shaft, B_{ls} shows the low speed damping effect, θ_t represents the rotor angular displacement and θ_{ls} denotes the low speed angular displacement.

We consider that the moment of inertia J_{ls} of the gear box is zero, so the previous relation will be given as follows:

$$T_{ls} = B_{ls} (w_t - w_{ls}) + K_{ls} (\theta_t - \theta_{ls}) \tag{9}$$

The dynamics of the rotor is characterized by the motion of the high-speed shaft torque T_{hs} and braked by the generator electromagnetic T_g , it is defined as:

$$J_g \dot{w}_g + B_g w_g = T_{hs} - T_g \tag{10}$$

with w_g is the angular speed of the high speed shaft, T_{hs} is the high speed shaft torque, J_g is the generator moment of inertia, B_g is the high speed damping effect, and T_g is the generator electromagnetic torque. Then, the gear box ration is:

$$n_g = \frac{T_{ls}}{T_{hs}} = \frac{w_g}{w_t} = \frac{\theta_g}{\theta_{ls}} \tag{11}$$

where θ_g is the angular displacement of high speed shaft. It is often confused with the displacement of the generator since it rotates at the same speed.

After some calculations and using the Eqs 7, 9, 11, we obtain the following state system describing the multi-input/multi-output system:

$$\begin{bmatrix} \dot{w}_t \\ \dot{w}_g \\ \dot{T}_{ls} \end{bmatrix} = \begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{bmatrix} \begin{bmatrix} w_t \\ w_g \\ T_{ls} \end{bmatrix} + \begin{bmatrix} b_{11} & b_{12} \\ b_{21} & b_{22} \\ b_{31} & b_{32} \end{bmatrix} \begin{bmatrix} T_a \\ T_g \end{bmatrix} \tag{12}$$

where

$$\begin{aligned} a_{11} &= \frac{-B_r}{J_r}, a_{12} = 0, a_{13} = \frac{-1}{J_r} \\ a_{21} &= 0, a_{22} = \frac{-B_g}{J_g}, a_{23} = \frac{1}{n_g J_g} \\ a_{31} &= \left(K_{ls} - \frac{B_r B_{ls}}{J_r} \right), a_{32} = \frac{1}{n_g} \left(\frac{B_r B_{ls}}{J_g} - K_{ls} \right), \\ a_{33} &= -B_{ls} \left(\frac{J_g n_g^2 + J_r}{J_g J_r n_g^2} \right) \\ b_{11} &= \frac{1}{J_r}, b_{12} = 0, b_{21} = 0, b_{22} = \frac{-1}{J_g}, b_{31} = \frac{B_{ls}}{J_r}, b_{32} = \frac{B_{ls}}{J_g n_g} \end{aligned}$$

4 Objectives of the control

Wind speed does not follow a constant pattern, but rather varies randomly. Therefore, it is essential to optimize the process of wind turbines during times when the wind speed is minimal or insufficient. The goal of wind energy systems is to maintain the turbine at nominal speed to ensure profitable and efficient power generation. Therefore, it is crucial to take into account the mechanical pieces of the turbine, namely the gearbox and the blades, in order to maximize the aerodynamic power.

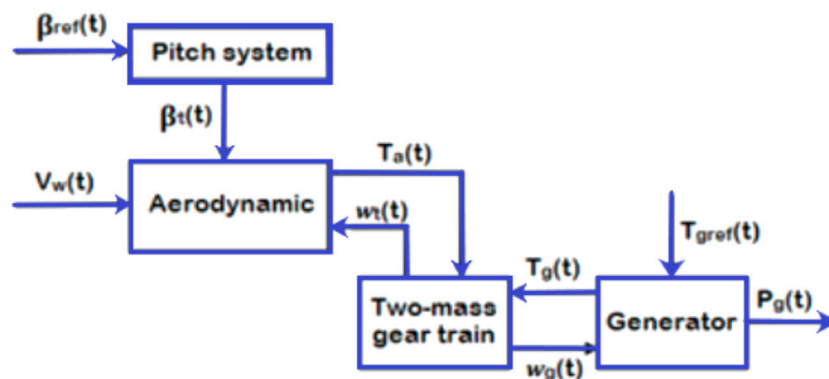


FIGURE 3 Subsystem-level block diagram of a variable-speed variable-pitch.

Figure 3 shows the control strategy principle applied to the turbine system with pitch control optimization. It illustrates the arrangement of the different parts of the transmission chain that receives the kinetic energy of the wind and converts it into electromechanical energy. Initially, the aerodynamic turbine receives the wind speed v to create an aerodynamic torque T_a that drives the two-mass gearbox. Of course, it must be known that T_a is closely linked to the choice of the pitch angle β of the wind turbine blades according to wind conditions and nacelle orientation. Through the rotor, the gearbox and the turbine rotate at low speed w_t . Under the constraint of the aerodynamic torque T_a , which drives the motion of the gearbox, the generator shaft is equipped with a high-speed rotation w_g , consequently creating an opposing generator torque T_g and therefore the generator power P_g .

The aim is to use PI-SMC scheme to command the wind turbine system. However, MPPT problems are always studied in close connection with the electromechanical generator without involving the aerodynamic part of the turbine when modeling and especially in optimizing the obtained electrical power. Since the turbine part, shaft, and gearbox consist of purely mechanical elements, it responds relatively slowly compared to the electrical part. This necessitates the use of the chosen control. Furthermore, the classical PI control is preferred due to its relatively simple implementation and tuning, which makes it commonly used in many applications. Moreover, precision is well controlled through the integral component, which corrects static errors and ensures high system accuracy. Additionally, stabilization is fast due to the proportional action of the system, minimizing real-time errors.

Since the turbine system is highly influenced by highly variable dynamics caused by the varying wind speed model, which is stochastically unpredictable, it is imperative to subject the characteristics of the PI controller to a command that can guarantee insensitivity to external disturbances and parameter variations that may arise in the turbine system. For this purpose, the use of SMC control ensures robustness, especially in the presence of uncertainties. In terms of control, SMC also allows precise reference tracking even under external disturbances, particularly the random wind speed and the internal structure, such as the shaft stiffness coefficient B_{Is} and shaft damping coefficient K_{Is} , which make the system non-rigid. Another strength of SMC control is its

fast dynamic response time, which is beneficial for real-time performance applications.

Overall, the automatic adaptability of control gains based on changing system conditions improves its ability to adjust to variations.

The aerodynamic power is maximized through its torque coefficient $C_p(\lambda, \beta)$ is optimized, given as:

$$C_{popt} = C_{popt}(\lambda_{opt}, \beta_{opt}) \tag{13}$$

The optimal tip-speed ratio λ , is defined as:

$$\lambda_{opt} = \frac{w_{topt}R}{V} \tag{14}$$

The value of λ is constant for all MPPT. To maximize the power extraction of the wind, we fix the value of the blades pitch angle β to an optimal value β_{opt} .

Then the Eq. 8 is verified if the rotor speed w_t tracks the desired speed w_{topt} given as

$$w_{topt} = \frac{\lambda_{opt}V}{R} \tag{15}$$

Using the Eqs 2, 4, the T_{aopt} and P_{aopt} can be expressed as:

$$\begin{cases} P_{aopt} = \frac{1}{2} \rho \pi R^5 \frac{C_{popt}(\lambda_{opt}, \beta_{opt})}{\lambda_{opt}^3} w_{topt}^3 \\ T_{aopt} = \frac{1}{2} \rho \pi R^5 \frac{C_{popt}(\lambda_{opt}, \beta_{opt})}{\lambda_{opt}^3} w_{topt}^2 \end{cases} \tag{16}$$

with $T_{aopt} = \frac{P_{aopt}}{w_{topt}}$

Since the rotation speed is the control parameter to be controlled, we can write the previous expressions as follows:

$$\begin{cases} P_{aopt} = G_{opt} w_{topt}^3 \\ T_{aopt} = G_{opt} w_{topt}^2 \end{cases} \tag{17}$$

with $G_{opt} = \frac{1}{2} \rho \pi R^5 \frac{C_{popt}(\lambda_{opt}, \beta_{opt})}{\lambda_{opt}^3}$.

Using Eqs 13–17, the aim of this section is to achieve an optimal rotational speed that produces the maximum power output without exceeding the nominal power rating of the turbine. Thus, it is crucial to regulate the turbine's speed to maintain this condition as shown

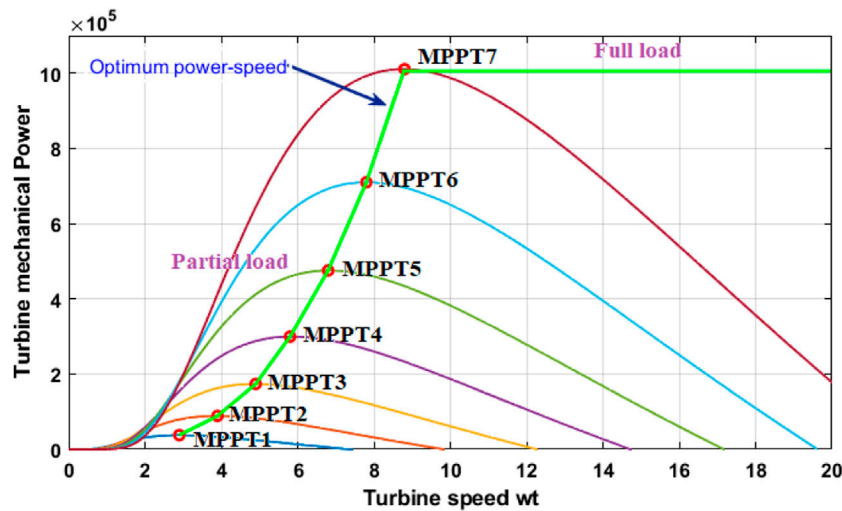


FIGURE 4 Turbine mechanical power.

in Figure 4. In order to capture the maximum power from the wind, it is necessary to keep the pitch angle at zero, which provides an optimal orientation to the wind speed.

Generally, in the design of control systems for wind energy systems, the focus is mainly on the modeling and control of the electrical part, particularly the asynchronous machine, rather than on the detailed modeling of the mechanical part (turbine and gearbox). The reason is that the mechanical dynamics usually have a much slower time constant than the electrical dynamics, which allows for simplifying assumptions on the mechanical part without significantly affecting the performance of the overall control system.

In our study, we focused on the modeling of the aerodynamic part of the wind turbine in order to design our PI-SMC control aimed at optimizing the generator’s power and torque. This approach allowed us to focus on the most critical aspect of the system, namely the maximum extraction of wind power, without the need to model the mechanical part in detail.

Although we did not specifically address the implementation of MPPT in this article, this technique is generally used to track the maximum power point by adjusting the turbine’s rotational speed according to the wind speed.

5 Sliding mode control design

In this section, the design of SMC for the wind turbine system is provided. Firstly, the rotational speed is controlled to maintain an optimal value. The main aim is to increase the C_p as close as possible to the Betz limit by optimizing the beta and lambda parameters. Secondly, the mechanical system of the turbine, modelled as a two-mass system, is controlled by SMC to obtain an optimal electromagnetic torque that generates sufficient power to enable the generator to produce the optimal electrical energy. In previous research, J. J. Slotine has proposed a sliding surface (Slotine et al., 1986; Slotine and Hong, 1986; Kelkoul and Boumediene, 2021; Yao

et al., 2021) that ensures the attraction of a variable to its optimal or predetermined reference value.

The sliding manifold is defined as:

$$S(x) = \left(\frac{d}{dt} + \alpha \right)^{n-1} e \tag{18}$$

with $\alpha > 0$, n is the system’s order defined in Behnamgol and Vali (2015) and the tracking error is given as

$$e = w_{tref} - w_t \tag{19}$$

The sliding surface given in Eq. 18, is given as:

$$S = w_{tref} - w_t \tag{20}$$

Differentiating the expression of S , we obtain:

$$\dot{S} = \dot{w}_{tref} - \dot{w}_t \tag{21}$$

Using Eqs 10, 11, we obtain:

$$J_g \dot{w}_t = T_{ls} - B_g w_t - \frac{1}{n_g} T_g \tag{22}$$

Substituting Eq. 22 in Eq. 7, we obtain:

$$J_t \dot{w}_t = T_a - B_t w_t - J_g T_g \tag{23}$$

with

$$\begin{cases} J_t = J_r + J_g \\ J_g = \frac{1}{n_g} \\ B_t = B_r + B_g \end{cases} \tag{24}$$

Using Eqs 21, 24 the expression of S is given as:

$$\dot{S} = \dot{w}_{tref} - \frac{1}{J_t} (T_a - B_t w_t - J_g T_g) \tag{25}$$

In sliding mode, we have the following conditions:

$$S = \dot{S} = 0 \tag{26}$$

Using the Eq. 25 to verify the Eq. 26 and to preserve $S = 0$, the equivalent control is designed to guarantee the high performance of the trajectory tracking, u_{eq} is given as:

$$u_{eq} = T_{geq} = aT_a + bw_t + c\dot{w}_{tref} \tag{27}$$

with

$$\begin{cases} a = n_g \\ b = -n_g(B_r + B_g) \\ c = -n_g(J_r + J_g) \end{cases} \tag{28}$$

The equivalent control, given in Eq. 28, will ensure that the system tracks the desired reference value. The nonlinear control will guarantee the system reaches the sliding surface and remains attractive to it. In fact this aspect of the SMC will require the system's dynamics to stay on the sliding surface previously defined by tracking the selected error value.

The sign function is commonly used to represent this aspect, as shown below:

$$u_{nl} = K_sgn(S) \tag{29}$$

Combining Eqs 27, 29 one obtains the following Eq. 30 describing the expression of the SMC:

$$u = aT_a + bw_t + c\dot{w}_{tref} + K_sgn(S) \tag{30}$$

To verify the stability of the wind turbine system using the Lyapunov function, we need to first define a candidate Lyapunov function $V(x)$ that satisfies the following conditions:

- Condition 1: $V(x)$ is positive definite, i.e., $V(x) > 0$ for all $x \neq 0$.
- Condition 2: $V(x)$ is radially unbounded, i.e., $V(x) \rightarrow \infty$ as $\|x\| \rightarrow \infty$.
- Condition 3: $V(x)$ has a negative definite derivative along the states of the system, i.e., $\dot{V}(x) < 0$ for all $x \neq 0$.

Assuming $x = [w_t \ w_g \ T_{ls}]^T$ is the states of the system; we can define suitable Lyapunov function as:

$$V(x) = \frac{1}{2}(w_{tref} - w_t)^2 \tag{31}$$

This function meets the first two conditions of a Lyapunov function.

To verify the third condition, we need to compute $\dot{V}(x)$, it can be derived as

$$\dot{V}(x) = (w_{tref} - w_t)\dot{w}_t \tag{32}$$

Substituting the expression for \dot{w}_t from Eq. 23, we get:

$$\dot{V}(x) = (w_{tref} - w_t) \frac{(T_a - B_t w_t - J_g T_g)}{J_t} \tag{33}$$

Substituting the expression for T_g from Eq. 27, we get:

$$\dot{V}(x) = (w_{tref} - w_t) \frac{(T_a - B_t w_t - aT_a - bw_t - c\dot{w}_{tref} - K_sgn(w_{tref} - w_t))}{J_t} \tag{34}$$

Simplifying and using the fact that $sgn(w_{tref} - w_t)$ is bounded between -1 and 1 , we can write:

$$\dot{V}(x) \leq -\frac{B_t}{J_t}(w_{tref} - w_t)^2 + |a| \frac{|T_a|}{J_t} + |b| \frac{|w_t|}{J_t} + |c| \frac{|\dot{w}_{tref}|}{J_t} + \frac{|K|}{J_t} \tag{35}$$

Checking Eqs 31–35 the is negative semi-definite, and the other terms are all positive. Therefore, it can be determined the system is globally asymptotically stable, it indicates the trajectories converge to the sliding surface and remain on it.

6 PI-SMC design

Our control strategy uses PI-SMC to track the maximum power trajectory. Subsequently, the PI-SMC operating algorithm is designed based on the aerodynamic model of the wind turbine, by defining an appropriate sliding surface S that allows regulating the turbine's rotational speed w_t from the reference rotation speed w_{tref} of the turbine, to extract the maximum wind power P_{amax} . The control laws are derived using Lyapunov method to ensure the stability and convergence of the system towards the MPPT. The implementation of the PI-SMC control requires tuning of several key parameters, such as the gains of the sliding surface namely α, n , the integral gain K_i and the gain K of nonlinear component of the control and the equivalent control. These parameters have been optimized using numerical optimization techniques in order to minimize the maximum power tracking error, while ensuring the robustness of the system to disturbances.

The numerical values of the PI-SMC controller parameters have been selected based on an analysis of the wind turbine aerodynamic model, as well as in-depth simulations of the overall system. This iterative process of parameter tuning has allowed obtaining good performance in terms of MPPT, disturbance rejection and system stability.

Using the SMC strategy, we can integrate the PI controller into the sliding surface expression to obtain improved control of the wind turbine system. Similarly, as presented in the previous section, the sliding surface is given by Eqs 19, 20. To integrate the PI, we add an integral term to the sliding surface as follows:

$$S = w_{tref} - w_t + \frac{1}{K_i} \int e.dt \tag{36}$$

where K_i is constant.

The time derivative of the sliding surface, given in Eq. 36, is obtained as

$$\dot{S} = \dot{w}_{tref} - \dot{w}_t + \frac{1}{K_i} e \tag{37}$$

Substituting from Eq. 10 and w_t from Eq. 37, the sliding surface is given in Eq. 38 as:

$$\dot{S} = -\frac{B_t}{J_t} w_t + \frac{T_a}{J_t} - \frac{J_g}{J_t} T_g - \dot{w}_t + \frac{1}{K_i} e \tag{38}$$

where T_g is the generator torque.

The control input is given by:

$$u = aT_a + bw_t + c\dot{w}_{tref} + K_sgn(S) + K_i e \tag{39}$$

TABLE 1 Two mass drive train system.

Parameter	Value
Rotor radius	$R = 21.65 \text{ m}$
Gearbox ration	$n_g = 43.165$
Shaft stiffness coefficient	$B_{Is} = 2.691 \cdot 10^5 \text{ N.m/rad}$
Shaft damping coefficient	$K_{Is} = 9500 \text{ N.m/rad/s}$
Rotor inertia	$J_r = 3.25 \cdot 10^5 \text{ kg.m}^2$
Rotor friction coefficient	$K_r = 27.36 \text{ N.m/rad/s}$
Generator inertia	$J_g = 34.4 \text{ kg.m}^2$
Generator friction coefficient	$K_g = 0.2 \text{ N.m/rad/s}$
Air density	$\rho = 1.204 \text{ kg/m}^3$

where a, b and c are constants, K is the sliding mode gain, and $sgn(S)$ is the sign function.

Substituting Eq. 7 into Eq. 39, we obtain Eq. 40:

$$J_t \dot{w}_t = T_a - B_t w_t - J_g T_g - a T_a - b w_t - c \dot{w}_{tref} - K sgn(S) - K_i e \tag{40}$$

To investigate the stability of the system, the Lyapunov function and its derivative are given in Eq. 41 and Eq. 42 as follow:

$$V(x) = \frac{1}{2} (w_{tref} - w_t)^2 + \frac{1}{2} K_i \int e^2 dt \tag{41}$$

Taking the $\dot{V}(x)$ along the trajectories of the system, we get:

$$\begin{aligned} \dot{V}(x) = & (w_{tref} - w_t) \\ & \times (T_a - B_t w_t - J_g T_g - a T_a - b w_t - c \dot{w}_{tref} - K sgn(S) - K_i e) \\ & + K_i e^2 \end{aligned} \tag{42}$$

Using the inequality $e|ab| \leq \frac{1}{2}a^2 + \frac{1}{2}b^2$, we can simplify Eq. 42 as follows:

$$\dot{V}(x) \leq -\frac{B_t}{J_t} (w_{tref} - w_t)^2 + |a| \frac{|T_a|}{J_t} + |b| \frac{|w_t|}{J_t} + |c| \frac{|\dot{w}_{tref}|}{J_t} + \frac{|K|}{J_t} + K_i e^2 \tag{43}$$

Since $B_t, J_t, |a|, |T_a|, |b|, |w_t|, |c|, |\dot{w}_{tref}|, |K|$ and K_i are all positive constants, the right-hand side of Eq. 43 is negative semi-definite. Hence, it is concluded that the proposed closed-loop system is stable.

7 Numerical simulation and results

To evaluate the proposed control performance on the two-mass gear train model, simulations will be conducted in the Matlab/Simulink environment. Simulation results will be presented through a series of figures, showcasing the behavior of the multivariable system under PI-SMC. The parameters of turbine system are given in Table 1:

Using the values of the turbine parameters in Table 2 and Eq. 12, we obtain the following state equation:

TABLE 2 The values of the turbine speed w_t and the generator speed w_g as a function of the wind speed v .

$v [m.s^{-1}]$	12	18	25
$w_t [rpm]$	2.12	3.18	4.424
$w_g [rpm]$	91.51	137.27	191.65

$$A = \begin{bmatrix} -8.418 \cdot 10^{-6} & 0 & -0.307 \cdot 10^{-6} \\ 0 & -581.400 \cdot 10^{-6} & 484.500 \cdot 10^{-6} \\ 9477.350 & 3408.800 & -3 \end{bmatrix}$$

$$B = \begin{bmatrix} 0.307 \cdot 10^{-6} & 0 \\ 0 & -0.307 \cdot 10^{-6} \\ 0.828 & 130.378 \end{bmatrix}$$

$$C = [1 \ 0 \ 0]$$

$$D = [0 \ 0] \begin{bmatrix} w_t \\ w_g \\ T_{Is} \end{bmatrix}$$

Final simulation time:

$$t = 10 \text{ s}$$

Simulation step:

$$dt = 0.001 \text{ s}$$

Initial condition:

$$x_0 = [0.010 \ 0.10 \ 0]^T$$

Control parameter values a, b, c, K and K_i :

$$a = 43.165$$

$$b = -1192.3834$$

$$c = -14.030 \cdot 10^6$$

$$K_i = 0.5$$

$$K = 12$$

Figures 5, 6 present the evolution of the state variables (w_t, w_g, T_{Is}), while Figure 7 shows the evolution of the different control laws T_a and T_g from different initial conditions. Small fluctuations appear at the beginning of the signals in Figures 5, 7, but they are quickly damped out and the control has a very smooth appearance without exhibiting any chattering phenomenon. The control is also responsive to variations in the input wind speed.

The evolution of the sliding surface, which shows the fluctuation of the rotor speed error controlled by its optimal reference value, is presented in Figure 8. The simulations demonstrate the controller's effectiveness in mitigating deviations between the system's behavior w_t and the desired reference values w_{tref} .

Moreover, these simulations demonstrate a stable convergence of the sliding mode system in both cases. The evolution of the norm of the sliding surface verifies the robustness of the control by converging to zero in a relatively short time, thus showing the control's ability to eliminate the error between the rotation speed and its optimal value. This demonstrates the effectiveness of the proposed approach in solving the windup problem that can be generated by classical control systems such as PID, if used alone.

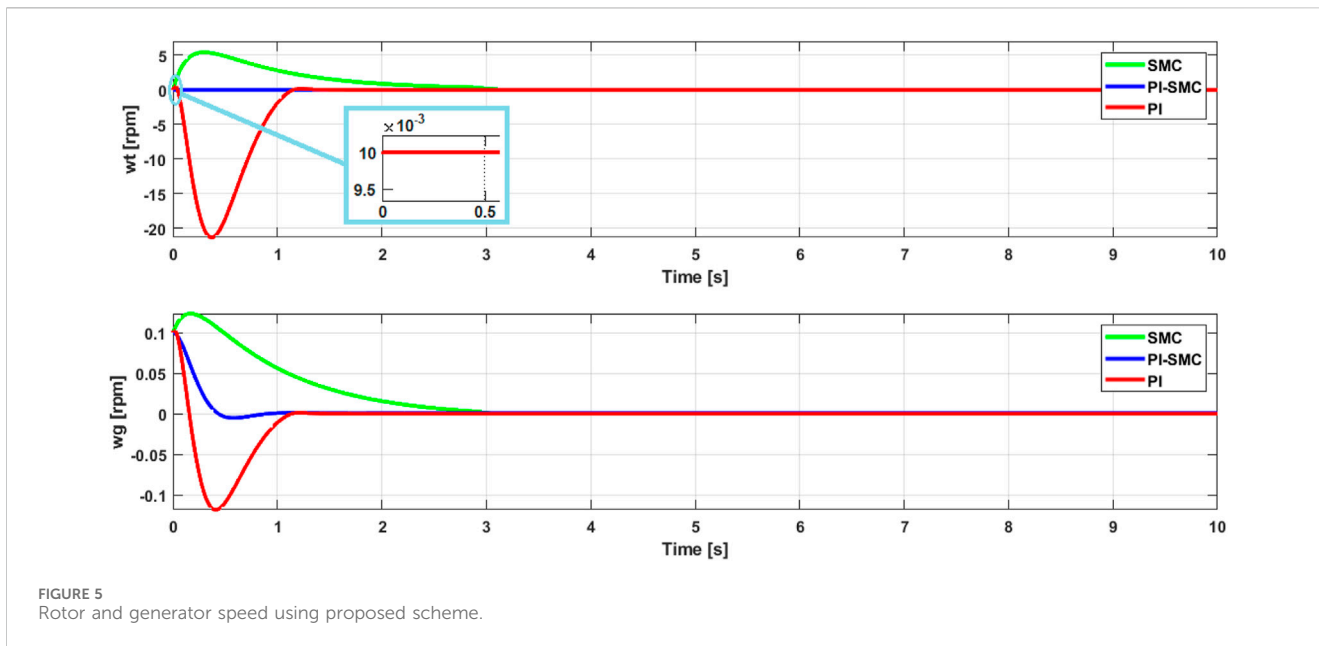


FIGURE 5 Rotor and generator speed using proposed scheme.

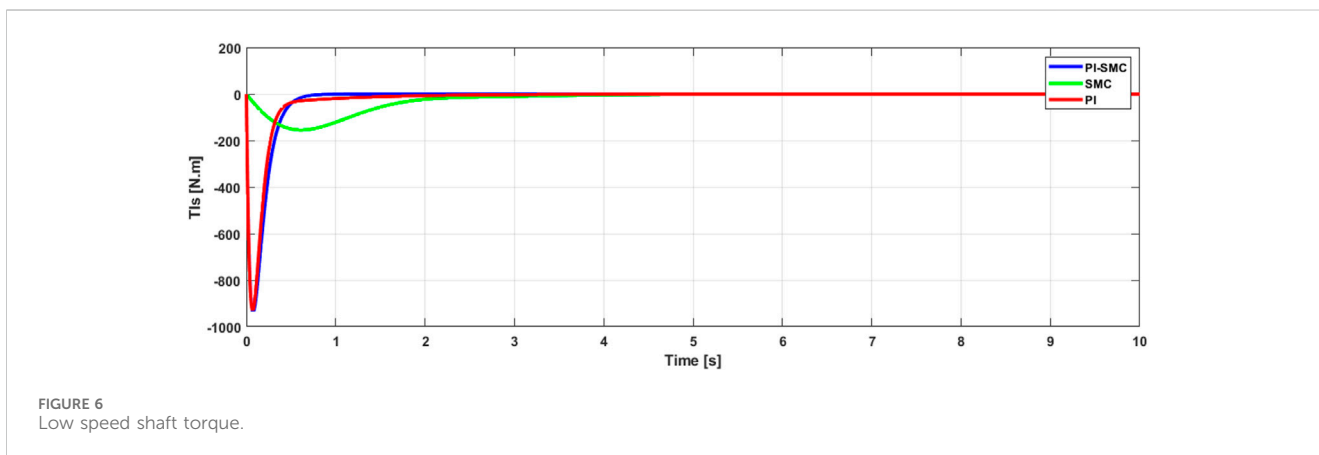


FIGURE 6 Low speed shaft torque.

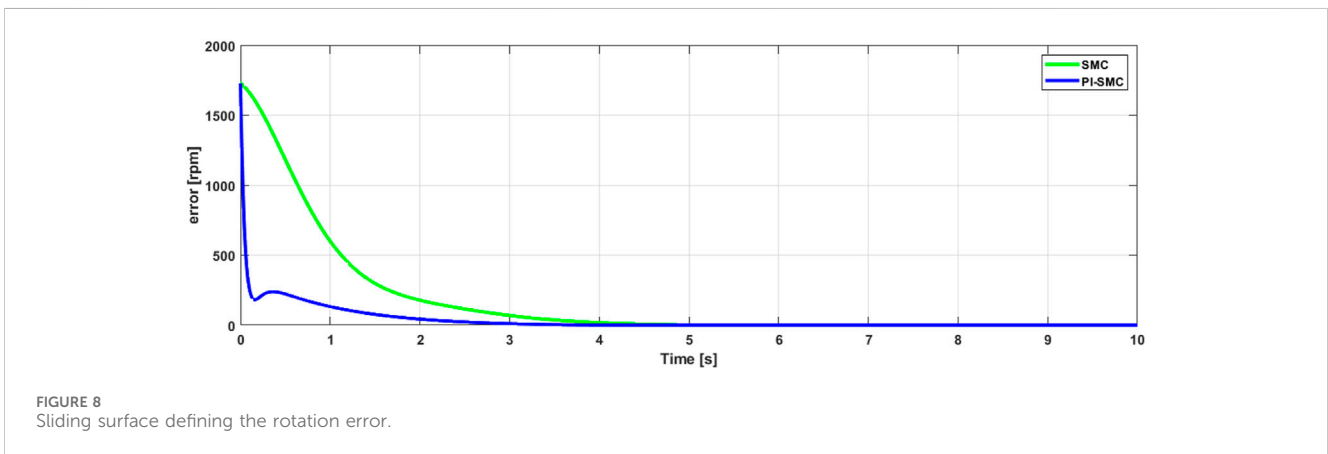
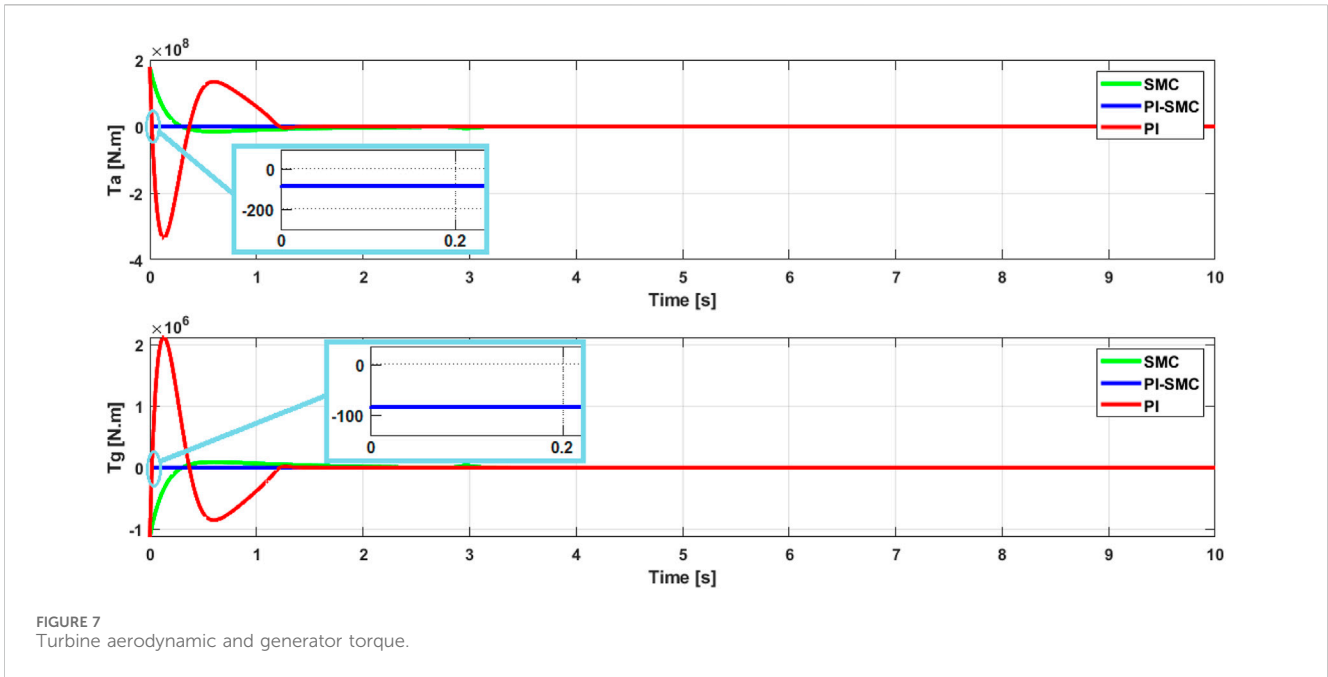
The results of the aerodynamic and generator power control are presented in Figure 9, respectively. These figures depict that the proposed control strategy is satisfactory, i.e., the generator power is sufficient and reaches the objective through the MPPT control strategy. The behavior of the two powers shows good convergence in a short time, which proves the robustness of the PI-SMC. The aerodynamic power figure is characteristic of a slow mechanical system, but the convergence is fast even in the presence of chattering. Despite the randomness of the wind and turbine rotation, the speed variation is controlled by MPPT and provides excellent control responses through the generator power scheme.

The strategy used in the simulation section is essentially based on the behavior of the PI-SMC controls of the various turbine system variables. That is to say, instead of following a classical servo control of the system variables with respect to their references, we have designed the control in such a way that to track the evolution of the control resulting from the dynamic behavior of the system. The simulations have shown us typical sliding mode figures and a transient behavior well adapted to the PI controller. The stability

of the system is verified each time. The performance of the dynamic behavior of the PI-SMC controlled system in terms of accuracy and speed is also well verified by a response time of 0.01 s and 0.5 s in the worst case.

In this part, we will perform a test to validate the proposed PI-SMC control with respect to other controls used in the control of wind turbines and in particular the two-mass models. In the literature, several control approaches have been explored, in this work, we have opted for the model predictive control (MPC) and the LQR. Several authors have proposed works on the LQR regulator (Haneesh and Raghunathan, 2021; Didier et al., 2024; Wang et al., 2024) and the MPC control (Gaamouche et al., 2020; Moness and Moustafa, 2020; Jiang et al., 2023).

Indeed, according to the literature, both LQR and MPC controls have shown efficiency and optimization in the control management of wind turbines. On the one hand, as a linear quadratic regulation method, the LQR allows high performance for the wind turbine system in the presence of disturbances, namely sudden changes in wind. The servomechanism of the wind turbine variables, primarily



the rotor speed and the blade pitch angle, aims to maximize the power. On the other hand, the MPC control uses a predictive model for the wind turbine, in order, to anticipate the behavior of the future dynamics and subsequently calculate the optimal control strategy over a sliding horizon. This control technique allows for appropriate management of the turbine while maximizing production.

The values of the MPC control parameters, are given as:

Prediction horizon:

$$N_p = 30$$

Control horizon:

$$N_c = 5$$

State error weighting matrix:

$$Q = [1000; 0 \ 1000; 0 \ 0 \ 10]$$

Control variation weighting matrix:

$$R = \text{eye}(3)$$

Reference to follow:

$$r = \text{ones}(3, T_{sim})$$

where T_{sim} is the simulation time.

The LQR regulator parameters, are given as:

State weighting matrix:

$$Q = [100; 0 \ 1000; 0 \ 0 \ 1]$$

Control weighting matrix:

$$R [0.01 \ 0 \ 0; 0 \ 0.1 \ 0; 0 \ 0 \ 0.01]$$

In Figures 10, 11, the shapes of the curves show a typical behavior of the controls. The simulations are performed with the initial conditions given earlier. The results show that all the curves are stable and converge in a relatively short time of 1s for a

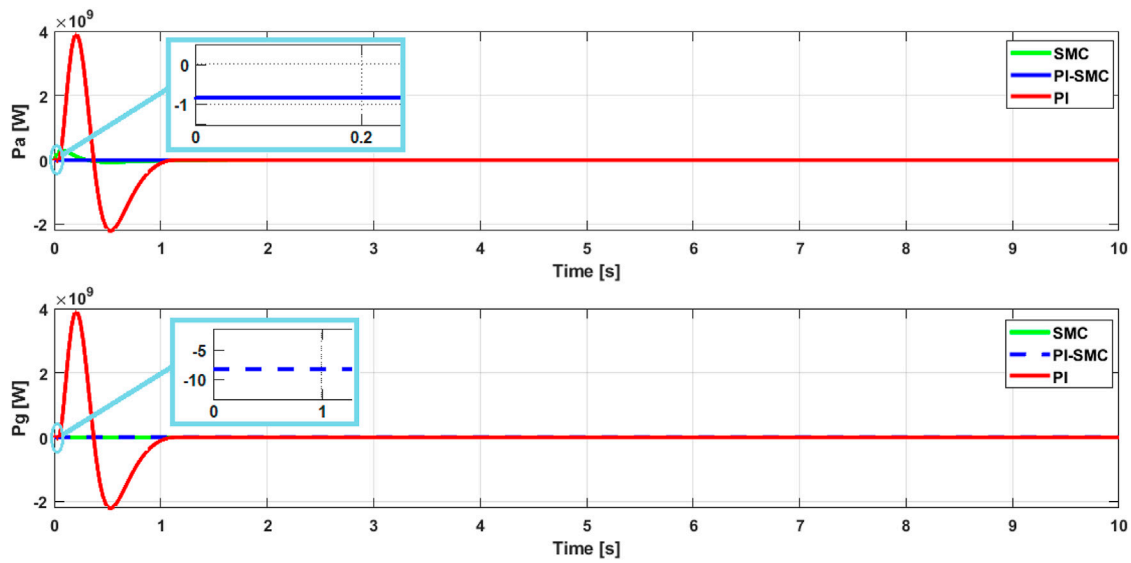


FIGURE 9 Aerodynamic and generator power.

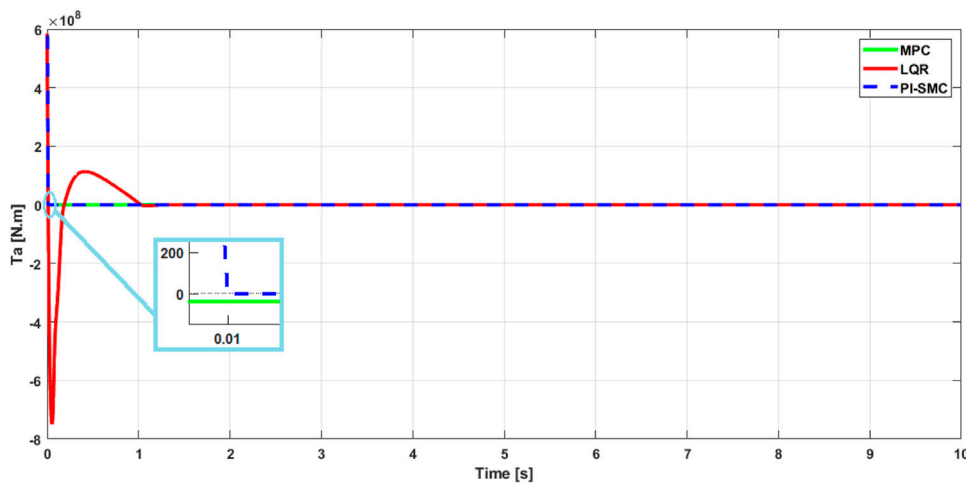


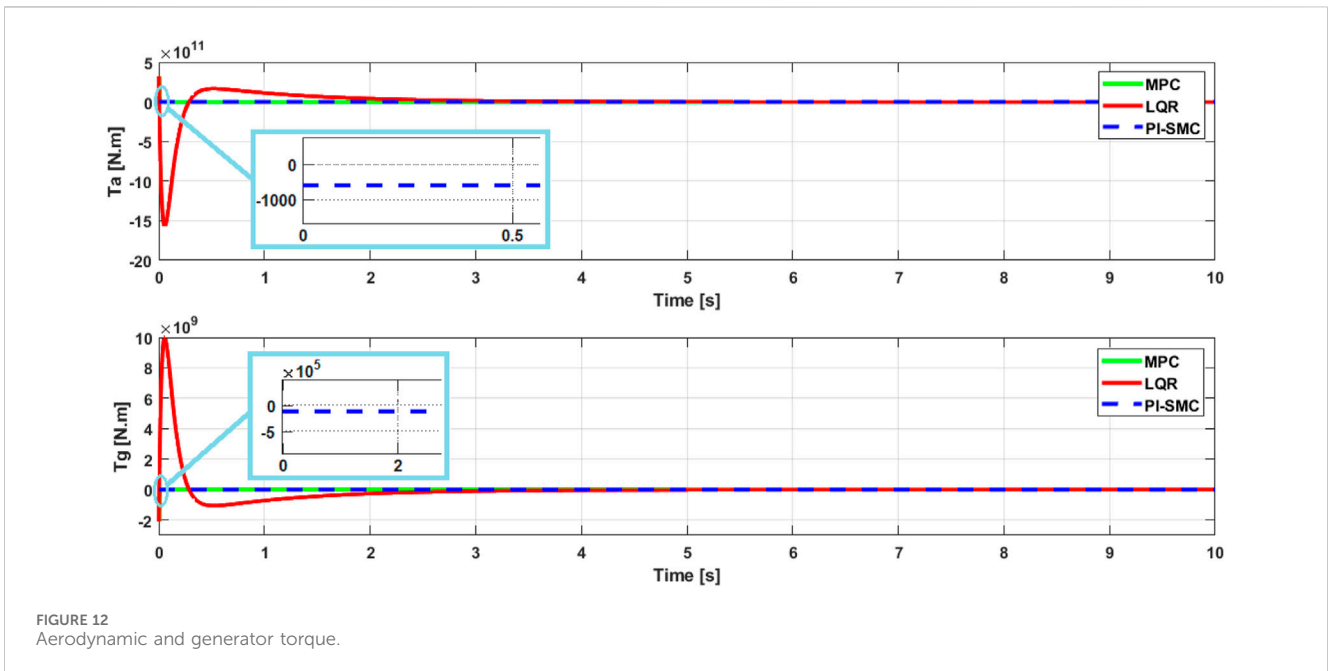
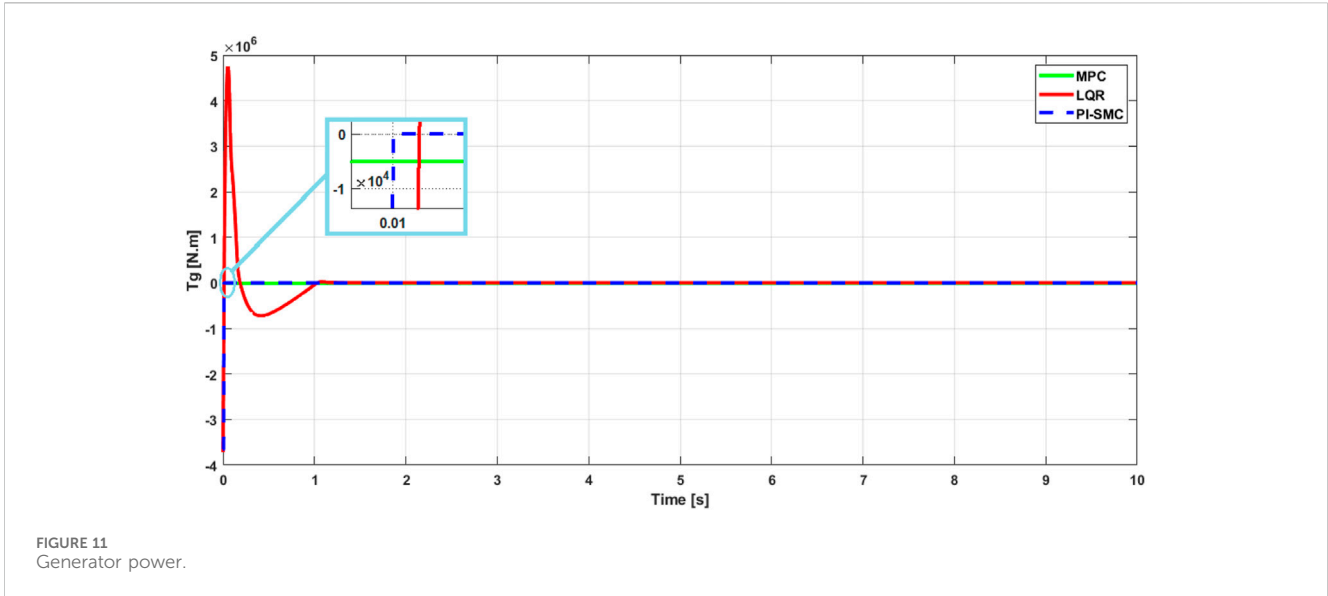
FIGURE 10 Aerodynamic torque.

mechanical system with a considered slow dynamics. Only the LQR control has a transient phase with fluctuations before stabilization, which is normal since it is known for its weakness in stabilizing systems with dynamics and sensitivity to modeling uncertainties. On the other hand, although the MPC control has a fast and stable response, the PI-SMC control responds in just 0.01 seconde. However, the PI-SMC presents somewhat large amplitudes due to the nonlinear component of the SMC control. Of course, saturation blocks can be added so that the control does not affect the integrity of the actuators.

This series of simulations will demonstrate the ability of the controls to overcome constraint perturbations, namely parameter variations and external disturbances, such as changes in wind speed v which directly affects the rotor speed w_t . The results will be

presented in Figure 12. To do this, we will carry out robustness tests to verify the reliability and effectiveness of the proposed control. A series of simulations is carried out by introducing parametric variations on the dynamics of the system. The chosen system parameters are those of the low-speed part since this part is the most affected by the dynamics of the system. So, we have set the values of $B_{I_s} = 1 N.m/rad$ and $K_{I_s} = 1 N.m/rad/s$ with differ from their original values given in Table 1. This severe parametric variation is intended to change the dynamics of the simulated system and subsequently observe the behavior of the different proposed controls with respect to such disturbance.

In Figure 12, the behavior of the aerodynamic torque and generator torque controls is very stable and typical. However, the LQR control presents a settling time of 4 s as well as a large overshoot



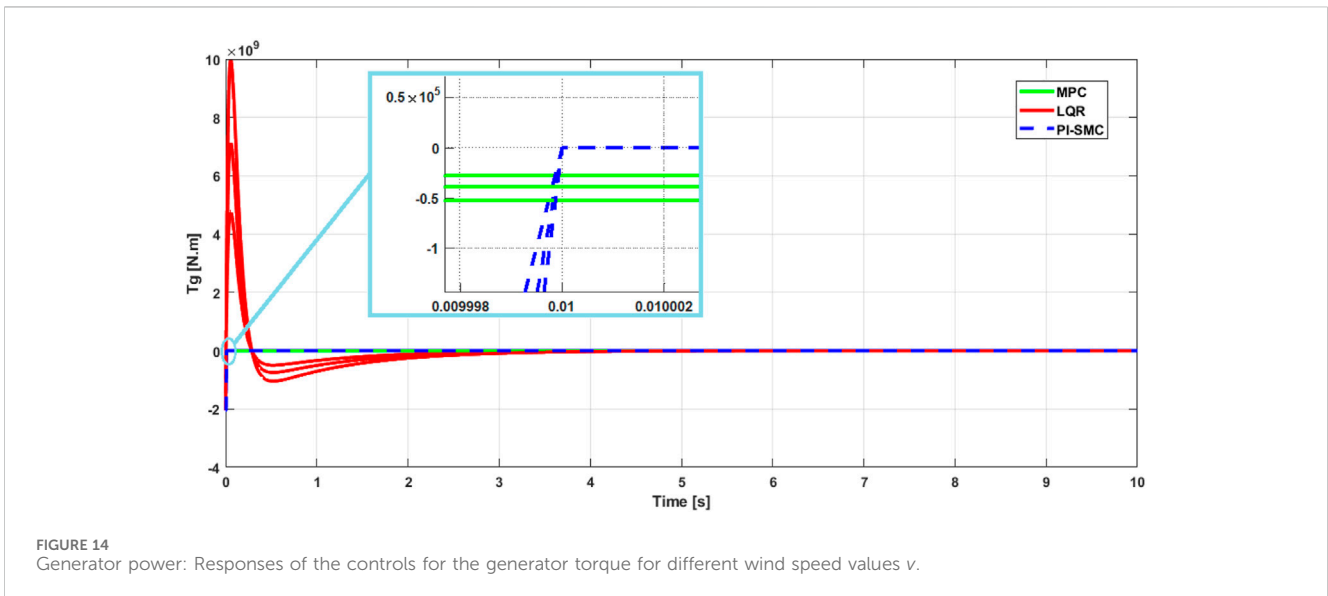
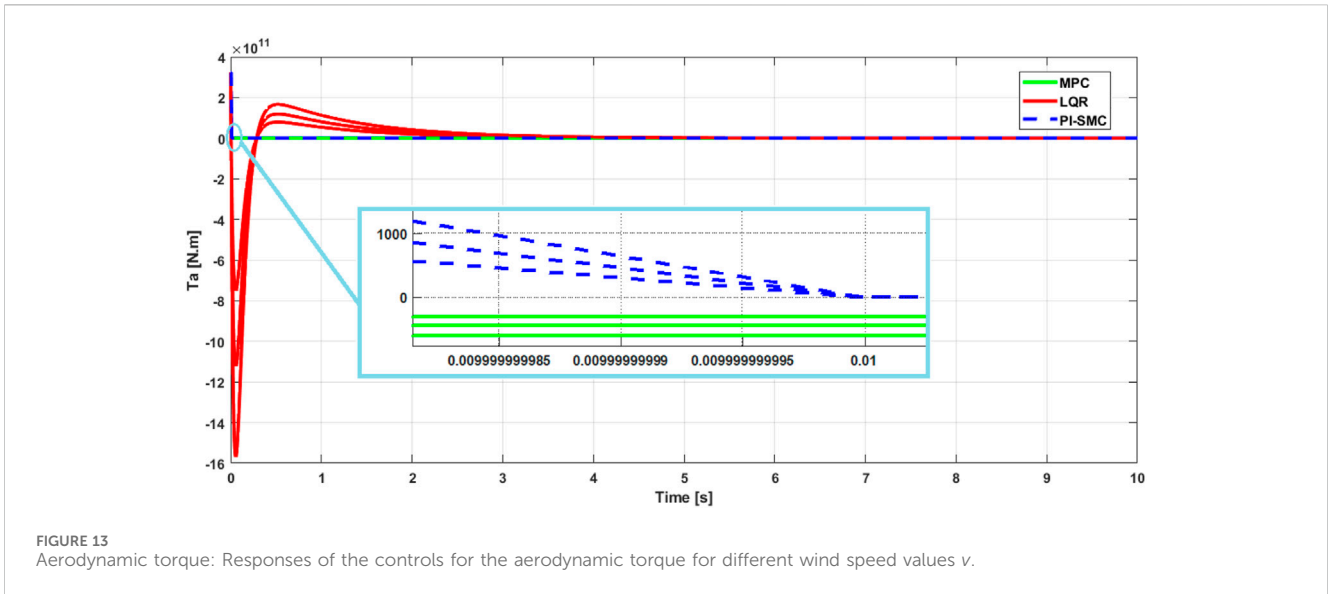
of $3 \cdot 10^8 N.m$ and $3 \cdot 10^{11} N.m$ for the two responses of the aerodynamic torque and the generator.

The PI-SMC control shows a fast behavior and, most importantly, it has maintained the same settling time of $0.01 s$. From this, we can conclude that this control was not influenced by the parametric variations made on the system model. This is quite normal since it is a characteristic of the SMC control which is insensitive to these variations, hence its robustness.

In this section we move on to the second test, which consists of evaluating the different MPC, LQR and PI-SMC controls by varying the wind speed v . Since the rotor speed is given as $w_t = \frac{\lambda v}{R}$ and using Figure 1, we can identify the value of λ for which the C_p coefficient is maximized. In addition, Eq. 15 allows us to determine each time the turbine speed w_t corresponding to the maximum C_p . Once the

values of w_t are obtained, we can directly calculate the values of w_g using Eq. 1. The numerical values of w_t and w_g as a function of the wind speed v are given in the table below:

Figures 13, 14 show the behavior of the PI-SMC control compared to the MPC and LQR controls. Each figure presents the simulation of each control with the 3 wind speed values of $12 ms^{-1}$, $18 ms^{-1}$ and $25 ms^{-1}$. The responses are also typical and stable, clearly showing the ability of all the controls to stabilize the system at different settling times each time. The variation of the wind speed v directly influences the response times of the LQR control, which are $7.5 s$, $8 s$ and $8.5 s$, increasing proportionally with the value of v . The same is true for MPC, the settling time is proportional to the wind speed value. For the PI-SMC control, it is clear that this control is also insensitive to



external disturbances. Indeed, the curves show a proportionality to the speed v , but as soon as the control stabilizes, the settling time is the same, which is 0.01 s. This confirms the robustness and insensitivity of the PI-SMC control. In conclusion, we can say that the behavior of the PI-SMC control is that of a high-performance, fast and robust control with respect to external disturbances and parametric variations.

Overall, the key strengths of our approach are its robustness and the high accuracy. However, the major downsides of SMC in general are the complexity of implementation and sensitivity to internal disturbances in general. Additionally, the problem of actuator windup remains a drawback of the PI control. Nevertheless, we acknowledge that other control approaches, such as the fuzzy controllers or artificial intelligence techniques, may also be effective in certain specific situations or for particular applications.

8 Conclusion

The objective of this study was to develop and analyze a control strategy for a wind turbine system that could optimize power output while minimizing electromagnetic torque variations. To achieve this, a PI-SMC (Proportional-Integral Sliding Mode Control) approach was implemented and evaluated. Specifically, the MPPT (Maximum Power Point Tracking) technique was used to ensure a fast and accurate coincidence between the turbine speed and reference speed. The PI-SMC approach was used to define a sliding surface representing the error between these speeds and systematically eliminate the chattering phenomenon and windup that often occur in traditional PID controllers.

The results showed that the proposed PI-SMC control strategy was effective in correcting deviations between the system behavior and its reference values. The PI-SMC exhibited typical SMC

characteristics, including robustness to mechanical variations, insensitivity to disturbances, and quick convergence. This approach was found to be superior to classical control systems like PID, which are prone to generating windup problems. Overall, the proposed PI-SMC control strategy was shown to be effective in optimizing the power output of the wind turbine system while minimizing electromagnetic torque variations. The approach was robust and stable, and maintained good convergence even in the presence of parametric variations and external disturbances.

However, the study also identified limitations of the PI-SMC strategy. It may not be suitable for wind turbine systems with large delays or significant nonlinearities, as these can make it more difficult to achieve the desired control performance. Ultimately, the PI-SMC is not always the most efficient or optimal control solution for every wind turbine system and other control techniques may be more appropriate depending on the specific application and requirements. Consequently, it would be interesting to integrate other optimal and intelligent control techniques into this control strategy to better manage the PI-SMC control parameters and subsequently optimize its performance.

Data availability statement

The original contributions presented in the study are included in the article/Supplementary Material, further inquiries can be directed to the corresponding author.

Author contributions

BT: Conceptualization, Formal Analysis, Methodology, Resources, Software, Visualization, Writing—original draft, Writing—review and editing. AA: Conceptualization, Formal Analysis, Investigation, Methodology, Supervision, Validation, Writing—original draft, Writing—review and editing. SA: Formal Analysis, Investigation, Methodology, Resources, Validation, Visualization, Writing—review and editing. AM: Formal Analysis, Funding acquisition, Investigation, Methodology, Resources, Validation, Writing—review and editing. II: Formal Analysis,

Investigation, Methodology, Resources, Validation, Visualization, Writing—review and editing.

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Conflict of interest

The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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