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Henry Hub monthly natural gas price forecasting using CEEMDAN–Bagging–HHO–SVR

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As a clean fossil energy source, natural gas plays a crucial role in the global energy transition. Forecasting natural gas prices is an important area of research. This paper aims at developing a novel hybrid model that contributes to the prediction of natural gas prices. We develop a novel hybrid model that combines the “Decomposition Algorithm” (CEEMDAN), “Ensemble Algorithm” (Bagging), “Optimization Algorithm” (HHO), and “Forecasting model” (SVR). The hybrid model is used for monthly Henry Hub natural gas forecasting. To avoid the problem of data leakage caused by decomposing the whole time series, we propose a rolling decomposition algorithm. In addition, we analyzed the factors affecting Henry Hub natural gas prices for multivariate forecasting. Experimental results indicate that the proposed model is more effective than the traditional model at predicting natural gas prices.

KEYWORDS

natural gas price forecasting, Henry Hub, SVR, CEEMDAN decomposition, Bagging, HHO algorithm

1 Introduction

The use of energy is a crucial part of production and consumption processes in all industries. A reliable, affordable, and stable energy supply is essential for industrial production, transportation, home heating, and commercial production. With the growth of the global population and the acceleration of industrialization, energy demand continues to increase, which results in a more complex and competitive energy market (Wang et al., 2021). In the area of data analysis and forecasting, energy price forecasting has received a lot of attention. Accurate energy price forecasts are of great benefit to researchers and policymakers.

As the demand for energy grows, environmental issues resulting from high emissions and pollution from fossil fuels are becoming more serious. The transition to renewable energy has become an urgent issue. Clean energy development and utilization are gradually attracting worldwide attention (Dong et al., 2022). As a low-carbon and clean energy source among fossil fuels, natural gas plays a crucial interim role in the transition to a sustainable energy economy (Rabbi et al., 2022).

To formulate rational energy policies, it is essential to make accurate predictions of natural gas price trends. They also optimize market operations, sustainable economic development, and global energy transition promotion.

Currently, the North American market, the UK market, and the Japanese and Korean markets are dominating the international natural gas market. The price trends of Henry Hub in the North American market, NBP at the Intercontinental Exchange (ICE) in the European market, and Platts Japan LNG import prices in the Asian market have become essential

reference indicators for assessing international natural gas price levels (Geng et al., 2016). Among them, the Henry Hub market is the most liquid, volatile, and unpredictable natural gas market. Research on natural gas price forecasting in the Henry Hub is important due to its importance in natural gas trading, power production planning, and regulatory decisions.

In this paper, the major research purpose is to propose a novel hybrid model to predict natural gas prices more accurately. We constructed a model combining Harris hawks optimization (HHO), Bagging integrated learning, support vector regression (SVR), and complete ensemble empirical mode decomposition with adaptive noise (CEEMDAN). There are many studies about “Decomposition Algorithm” + “Forecasting Model” and “Ensemble Algorithm” + “Forecasting Model.” However, few studies combine the “Decomposition Algorithm,” “Ensemble Algorithm,” “Optimization Algorithm,” and “Forecasting Model.” We conducted this experiment and verified its feasibility.

First, the SVR model is optimized using the HHO algorithm to reduce subjectivity of the parameter settings and improve prediction accuracy, then the Bagging integration strategy is applied to the HHO–SVR model to further enhance model performance, and the Bagging–HHO–SVR model is constructed. A CEEMDAN algorithm was used to decompose natural gas price monthly time series into multiple modal components. The CEEMDAN–Bagging–HHO–SVR prediction model reduces the subjectivity and complex parameter setting of the SVR model. While reducing the variance of the model, it also optimizes the impact of noise on time series data, allowing it to extract the inherent features of the data. When applying CEEMDAN to decompose data, we adopted a rolling decomposition method to avoid the potential problem of data leakage caused by previous methods. The final experimental results indicate that the constructed model has a high level of prediction accuracy and relatively stable performance.

In summary, this paper makes several major contributions:

- (1) To better predict the Henry Hub natural gas price, we integrated “Decomposition Algorithm” + “Ensemble Algorithm” + “Optimization Algorithm” + “Forecasting Model” based on machine learning technology and proposed a novel hybrid prediction model.
- (2) We improved the way CEEMDAN works on datasets in the past and adopted a rolling decomposition approach. This method can avoid data leakage.
- (3) We took into account the external influencing factors of Henry Hub natural gas prices in the input variables, which further improves the prediction accuracy and stability of the model.
- (4) In order to understand the model and which features have the greatest impact on the prediction results of the model, we conducted a feature importance analysis. In addition, we identified significant factors that affect Henry Hub natural gas prices.

The structure of the rest of this paper is as follows: Section 2 is a literature review. Section 3 describes algorithms and models. Section 4 describes the data preparation work, prediction process, and variable screening experiments. Section 5 discusses the data description and experimental results. Section 6 summarizes some conclusions and proposes some suggestions.

2 Literature review

Energy forecasting typically spans different prediction horizons, including short term (hours and days), medium term (weeks), and long term (months and years). As a result of the different prediction ranges, the sample size varies as well. The sample size of daily predictions is usually larger than that of monthly predictions (Arvanitidis et al., 2022), and natural gas price forecasting focuses on daily, weekly, and monthly forecasts. This paper focuses on the monthly price forecast, which is a small sample size for long-term price forecasting. Therefore, this paper chooses the SVR model, which is excellent for small-sample quantity prediction, and compares it to the other benchmarking models.

Additionally, energy price predictions can be classified into univariate and multivariate predictions according to the variables involved (Hou et al., 2022). Most previous studies on natural gas prices have used univariate forecasts. In univariate forecasting, only historical natural gas price data are introduced as input variables into the forecasting model. This forecasting method assumes that external factors are stable, which saves time and effort collecting relevant influencing factors. However, the drawback is that some critical factors are often overlooked, and the forecasting model is not comprehensive enough. This usually results in relatively limited forecasting accuracy. Multivariate forecasting incorporates a variety of other factors that affect changes in natural gas prices. This method can make input variables more comprehensive, although it takes more time and effort to collect and process data. In this paper, we consider and use grey relation analysis (GRA) to examine multiple factors that influence natural gas price changes. In order to improve the quality of input variables, retained factors will be used in conjunction with historical natural gas prices as input variables.

The available literature indicates that energy forecasting models can broadly be categorized into traditional economic models and machine learning models based on artificial intelligence (Lu et al., 2021). Particularly in recent years, as artificial intelligence has seen rapid advancements, more studies have employed machine learning models. Econometric models, which are based on economic principles and statistical methods, build mathematical models to make predictions. Common econometric models include time series models (e.g., autoregressive moving average (ARMA), generalized autoregressive conditional heteroskedasticity (GARCH), and autoregressive integrated moving average (ARIMA)) (Ma and Wang, 2019; Son et al., 2020; Zhang et al., 2021; Sun et al., 2023) and regression models (e.g., multiple linear regression (MLR) and vector autoregression (VAR)) (Youssef et al., 2021; Egbueri J and Agbasi J., 2022; Pannakkong et al., 2022). Although these models can capture trends, seasonality, and periodicity in price series, they are less capable of addressing nonlinear problems and large-scale datasets. Moreover, energy forecasting is usually based on irregular and nonlinear data in real life. Yu and Yang (2022) used China’s electricity demand dataset spanning from 2004 to 2019. They combined the dataset with the ARMA model, to analyze the future electricity situation in China and accurately predict China’s electricity demand in 2020. Alam et al. (2023) used the ARIMA model to predict coal, oil, and natural gas prices in India before and after COVID-19. The empirical results suggest that the ARIMA model is appropriate for forecasting coal, crude oil, and natural gas prices in India. Hou and Nguyen (2018) applied a

Markov switching vector autoregressive model (MS-VAR) to examine the institutional response patterns of the natural gas market to underlying fundamental shocks. Their study identified the presence of four separate regimes within the American natural gas market. Nguyen and Nabney. (2010) first proposed an adaptive multilayer perceptron (MLP)/GARCH model combined with wavelet transform (WT) to predict electricity demand and natural gas prices in the UK, achieving high prediction accuracy.

Comparatively, machine learning models make predictions by learning patterns and regularities from historical data. Over the past few years, significant progress has been made in energy forecasting to address the shortcomings of traditional econometric models. Typical machine learning models encompass SVR models (Jianwei et al., 2019), neural network models (Wang et al., 2020), and decision tree models (Yahşi et al., 2019; Bentéjac et al., 2020). These models have strong nonlinear modeling capabilities, can handle large-scale datasets, and can automatically extract features from the data to better capture complex relationships in energy prediction. Since machine learning models often have many parameters to be set, these parameters significantly impact the predictive performance of the model. Moreover, manual parameter setting involves subjectivity and costs a lot of time. Intelligent optimization algorithms can automatically search the large-scale parameter space and find the best solution. Ma et al. (2019) used grey wolf optimization combined with a novel fractional time-delayed grey model to predict natural gas and coal consumption in Chongqing, China. The results suggest that the optimized model of grey wolf optimization outperforms the rest of the comparative models. Zhu et al. (2023) optimized the model constructed in the paper with the marine predator algorithm and enhanced forecasting performance. Essa et al. (2020) improved the prediction accuracy of conventional artificial neural networks by optimizing their parameters using Harris hawks optimization.

Machine learning models are categorized into single and hybrid models. Single models use only one machine learning algorithm or model for natural gas price forecasting. These models generally focus on a specific algorithm or model structure and are trained on data to obtain predictions. Čeperić et al. (2017) used an SVR model and a feature selection method to forecast Henry Hub natural gas spot prices. Salehnia et al. (2013) used a calibrated ANN model to predict the Henry Hub natural gas price with the help of the gamma test. Zhang and Hamori (2020) integrated the dynamic moving window method with the XGBoost model to forecast the U.S. natural gas crisis.

A single model cannot achieve continuous satisfactory prediction performance when dealing with various data and is prone to ignoring the internal characteristics of the data or overfitting, which means most of them have limitations (Yu et al., 2021; Zhang et al., 2022). The hybrid model refers to the combination of multiple machine learning algorithms or models to achieve better performance and generalization ability. According to previous literature, the prediction performance of the hybrid model is always better than that of the economic model and the single model (Jiang et al., 2022a).

Jung et al. (2020) constructed a hybrid model by combining “bagging” algorithms with “multilayer perceptron.” The final result

analysis shows superior performance. Meira et al. (2022) proposed a novel generalization algorithm by combining the Bagging integration method with a modified regularization technique. The study constructed a novel hybrid model and empirically analyzed monthly natural gas consumption in 18 European countries. Li et al. (2021) constructed a VMD-PSO-DBN model using the VMD algorithm combined with the PSO-optimized DBN model to empirically analyze monthly natural gas prices in Henry Hub. The results suggested that the newly constructed model predicted better than traditional models. Fang et al. (2023) combined EMD with ISBM-FNN and developed an EMD-ISBM-FNN model to decompose and predict crude oil prices. To verify the model's prediction results, a comparison scheme was designed to compare the results. Results indicate that the model had the highest prediction results and outperformed previous research. Zhan et al. (2022) proposed a technique combining LSTM and quadratic decomposition to construct an improved natural gas forecasting hybrid model VMD-EEMD-Res.-LSTM and then selected the monthly natural gas spot price of Henry Hub for empirical analysis. Wang et al. (2022) combined the decomposition algorithm with the multi-objective grasshopper optimization algorithm, and used nine models to predict the decomposed components. Then, they conducted short-term power load forecasting, ultimately achieving satisfactory results in point and interval prediction.

3 Methodology

3.1 Support vector regression

Support vector machine (SVM) was proposed by Cortes and Vapnik for classification tasks (Cherkassky, 1997). Later, SVR was developed based on the SVM. SVR relies on the principle of structural risk minimization, which makes it ideal for solving high-dimensional, small-sample nonlinear problems. Its primary purpose is to convert a nonlinear regression problem with a low dimension into a linear regression problem with a high dimension (Zheng et al., 2023). Based on dataset $K = \{(x_1, y_1), (x_2, y_2), \dots, (x_n, y_n)\}$, where $x_i \in R^n$ is the input feature, $y_i \in R$ is the label, and n denotes the number of training samples. The basic mapping relation of SVR can be expressed as follows:

$$f(x) = W\varphi(x_i) + b, \quad (1)$$

where W and b denote the weight coefficient and bias term (Cai et al., 2023). $\varphi(x_i)$ is the mapping function, mapping x_i to the higher-dimensional space using $\varphi(x_i)$ in Eq. 1. For the determination of W and b , the structural risk minimization principle of Eq. 2 can be implemented.

$$\text{Minimize: } \frac{1}{2} \|W\|^2 + C \sum_{i=1}^n \xi_i + \xi_i^*. \quad (2)$$

The constraints are

$$\begin{cases} y_i - (W\varphi(x_i) + b_i) \leq \varepsilon + \xi_i \\ (W\varphi(x_i) + b_i) - y_i \leq \varepsilon + \xi_i^* \\ \xi_i, \xi_i^* \geq 0 \quad i = 1, 2, \dots, n \end{cases} \quad (3)$$

where C is the penalty function and $\varepsilon > 0$ is the insensitivity factor and ξ_i and ξ_i^* is the slack variable.

Subsequently, the Lagrange multipliers are introduced α_i and α_i^* , at which point the function in Eq. 1 is transformed into $f(x)$:

$$f(x) = \sum_{i=1}^n (\alpha_i - \alpha_i^*)k(x_i, x_j) + b, \quad (4)$$

where $k(x_i, x_j)$ is the kernel function. Linear kernel, polynomial kernel, and radial basis function are some of the most commonly used kernel functions. Radial basis function kernel deals well with nonlinear data. It calculates the similarity between the data points in the high-dimensional feature space by inner product and greatly reduces calculation complexity (Açkkar and Altunkol et al., 2023). Therefore, in this paper, we used the RBF as the kernel function, and its mathematical expression is

$$k(x_i, x_j) = \exp\left(-\frac{\|x_i - x_j\|^2}{2\sigma^2}\right), \sigma > 0, \quad (5)$$

where σ is the parameter of the kernel function. Usually, it is necessary to choose appropriate values for the kernel function's C and σ to improve the prediction accuracy. C is the penalty function, which represents the model's tolerance to error. The higher C indicates that the model is less tolerant to error and easy to overfit. In contrast, it is easy to underfit. σ is a crucial parameter of the radial basis function kernel, which controls the bandwidth of the radial basis function (Li et al., 2022). The selection of σ directly impacts the model's complexity and generalization capability. The choice of these two parameters is crucial for controlling the prediction accuracy of the model. We used three optimization functions to optimize these two SVR parameters and compared the results in this paper.

3.2 Grey wolf optimization algorithm

The grey wolf optimizer (GWO) is a swarm intelligence optimization algorithm proposed in 2014 by Mirjalili et al. (2014), who are scholars from Griffith University, Australia. The algorithm has a simple structure, high convergence, and no excessive parameter settings. The GWO algorithm simulates the leadership hierarchy and hunting mechanisms of grey wolves in nature based on their predatory behavior. It classifies grey wolves into four types. The algorithm consists of three main parts: surrounding the prey, approaching the prey, and attacking the prey.

In the GWO algorithm, four wolves are established with varying social ranks, including α , β , δ , and ω . Among them, α simulates the head wolf (level 1 wolf), which leads the entire grey wolf pack and is responsible for leading the whole pack to hunt for prey. α represents the optimal solution to the problem. β is the level 2 wolf, which is responsible for assisting α . δ is the level 3 wolf, which obeys the commands and decisions of α and β , and is responsible for scouting and standing guard. ω is the level 4 wolf, which is located at the bottom of the entire hierarchy. It obeys the commands from the former level 3 wolf to carry out the position around α , β , or δ update (Liu Z et al., 2023).

(1) Surrounding the prey

The GWO algorithm uses the following formula to encircle its prey before hunting:

$$\vec{D} = |\vec{C} \cdot \vec{X}_p(t) - \vec{X}(t)|, \quad (6)$$

$$\vec{X}(t+1) = \vec{X}_p(t) - \vec{A} \cdot \vec{D}, \quad (7)$$

where \vec{D} is the distance between the wolf and its prey. $\vec{X}(t+1)$ is the position update formula of the grey wolves, and t is the number of iterations. $\vec{X}_p(t)$ represents the position vector of the prey. $\vec{X}(t)$ represents the position vector of grey wolves, and \vec{A} and \vec{C} are the coefficient vectors.

(2) Approaching the prey

The formulas of \vec{A} and \vec{C} are Eq. 8 and Eq. 9.

$$\vec{A} = 2\vec{a} \cdot \vec{r}_1 - \vec{a}, \quad (8)$$

$$\vec{C} = 2 \cdot \vec{r}_2, \quad (9)$$

$$\vec{a} = 2 - 2 \frac{t}{t_{max}}, \quad (10)$$

where \vec{r}_1 and \vec{r}_2 are the random vectors between [0,1]. \vec{a} is the convergence factor, a critical parameter in the GWO that balances the exploration and exploitation capabilities. Its value linearly decreases from 2 to 0 as the number of iterations increases. t_{max} is the maximum number of iterations. Therefore, A takes values in the range $[-a, a]$. To enable the grey wolves to search for prey better, $|A| > 1$ or $|A| < 1$ are used to compel the grey wolves to move away from the prey to continue searching or to approach the prey to prepare for hunting.

(3) Attacking the prey

Grey wolves are expected to begin hunting behavior after identifying the approaching prey. The hunting behavior is generally led by the α -wolf, assisted by the β -wolf and δ -wolf, and ω -wolf update based on their position. The mathematical formula for hunting is as follows:

$$\vec{D}_\alpha = |\vec{C}_1 \cdot \vec{X}_\alpha - \vec{X}|, \quad (11)$$

$$\vec{D}_\beta = |\vec{C}_2 \cdot \vec{X}_\beta - \vec{X}|, \quad (12)$$

$$\vec{D}_\delta = |\vec{C}_3 \cdot \vec{X}_\delta - \vec{X}|, \quad (13)$$

where \vec{D}_α , \vec{D}_β , and \vec{D}_δ denote the distance between the ω -wolf individual and the three former wolves, respectively. \vec{X} represents the current position of the individual ω -wolf.

$$\vec{X}_1 = |\vec{X}_\alpha - \vec{A}_1 \cdot \vec{D}_\alpha|, \quad (14)$$

$$\vec{X}_2 = |\vec{X}_\beta - \vec{A}_2 \cdot \vec{D}_\beta|, \quad (15)$$

$$\vec{X}_3 = |\vec{X}_\delta - \vec{A}_3 \cdot \vec{D}_\delta|, \quad (16)$$

where \vec{X}_α , \vec{X}_β , \vec{X}_δ represent the current positions of the α -, β -, and δ -wolf, respectively. \vec{C}_1 , \vec{C}_2 , \vec{C}_3 are three random numbers. \vec{X}_1 , \vec{X}_2 , and \vec{X}_3 denote the position of the ω -wolf affected by the position of the α -wolf, β -wolf, and δ -wolf, respectively. Here, the average value is taken.

$$\vec{X}(t+1) = \frac{\vec{X}_1 + \vec{X}_2 + \vec{X}_3}{3}. \quad (17)$$

3.3 Marine predator optimization algorithm

Faramarzi et al. (2020) proposed the marine predators algorithm (MPA) in 2020. The algorithm is primarily inspired by foraging behavior in marine predators. Essentially, this involves the Lévy and Brownian movements of marine predators and the optimization of the encounter rate strategy between the predators and prey. It is based on the theory of survival of the fittest in the ocean. The MPA has high optimization search performance. Among them, the Brownian motion search step is large enough to track and explore neighboring regions to achieve global optimization. In contrast, the Lévy motion search step is small enough to effectively explore local regions in depth to achieve local optimization. There are three main phases to the algorithm: the pre-search phase, the mid-search phase, and the post-search phase.

(1) Pre-search phase

During the phase of pre-search, we assume that the prey will move faster than the predator, at which point the predator should remain stationary.

When $Iter < \frac{1}{3} Max_Iter$,

$$\overrightarrow{stepsize}_i = \vec{R}_B \otimes (\overrightarrow{Elite}_i - \vec{R}_B \otimes \overrightarrow{Prey}_i), \tag{18}$$

$$\overrightarrow{Prey}_i = \overrightarrow{Prey}_i + P \cdot \vec{R} \otimes \overrightarrow{stepsize}_i, \tag{19}$$

$i = 1, \dots, n,$

where $\overrightarrow{stepsize}_i$ represents the move step size. \vec{R}_B represents a random vector following a normal distribution. \overrightarrow{Elite}_i represents the elite matrix consisted of the top predators. \overrightarrow{Prey}_i is the prey matrix, which has the same dimension as the elite matrix. \vec{R} is a random vector between [0,1]. P is a 0.5 constant. \otimes is the term-by-term multiplication operator. n is the population size. $Iter$ is the current iteration number, and Max_Iter is the maximum iteration number.

(2) Mid-search phase

In the mid-search stage, we assume that both the predator and the prey are moving at the same speed. During this phase, the predator simulates the hunt for the prey, while the prey, as a potential predator, searches for a prey of a lower rank than itself. At this point, the prey exploits in accordance with a Lévy wandering strategy, while the predator explores in accordance with a Brownian wandering strategy and gradually transitions from an exploration strategy to an exploitation strategy.

When $\frac{1}{3} Max_Iter < Iter < \frac{2}{3} Max_Iter$,

$$\overrightarrow{stepsize}_i = \vec{R}_L \otimes (\overrightarrow{Elite}_i - \vec{R}_L \otimes \overrightarrow{Prey}_i), \tag{20}$$

$$\overrightarrow{Prey}_i = \overrightarrow{Prey}_i + P \cdot \vec{R} \otimes \overrightarrow{stepsize}_i, \tag{21}$$

$i = 1, \dots, \frac{n}{2},$

where \vec{R}_L is the random vector presenting Lévy.

When $\frac{1}{3} Max_Iter < Iter < \frac{2}{3} Max_Iter$,

$$\overrightarrow{stepsize}_i = \vec{R}_B \otimes (\vec{R}_B \otimes \overrightarrow{Elite}_i - \overrightarrow{Prey}_i), \tag{22}$$

$$\overrightarrow{Prey}_i = \overrightarrow{Elite}_i + P \cdot CF \otimes \overrightarrow{stepsize}_i, \tag{23}$$

$i = \frac{n}{2}, \dots, n,$

where $CF = (1 - \frac{Iter}{Max_Iter})^{(2 \frac{Iter}{Max_Iter})}$ represents the adaptive parameter that governs the step size of predator movement.

(3) Post-search phase

At this stage, we assume that the predator has a higher speed compared to the prey, at which point the predator's best strategy is Lévy movement.

When $Iter > \frac{2}{3} Max_Iter$,

$$\overrightarrow{stepsize}_i = \vec{R}_L \otimes (\vec{R}_L \otimes \overrightarrow{Elite}_i - \overrightarrow{Prey}_i), \tag{24}$$

$$\overrightarrow{Prey}_i = \overrightarrow{Elite}_i + P \cdot CF \otimes \overrightarrow{stepsize}_i, \tag{25}$$

$i = 1, \dots, n.$

(4) Addressing vortex effects and FAD effects

Moreover, the algorithm takes into account environmental factors affecting marine predators' behavior to avoid the algorithm converging prematurely, for example, eddy current effects and fish aggregating device (FAD) effects. The mathematical formulation is as follows:

$$\overrightarrow{Prey}_i = \begin{cases} \overrightarrow{Prey}_i + CF[\vec{X}_{min} + \vec{R} \otimes (\vec{X}_{max} - \vec{X}_{min})] \otimes \vec{U}, & \text{if } r \leq FADs \\ \overrightarrow{Prey}_i + [FADs(1-r) + r](\overrightarrow{Prey}_{r1} - \overrightarrow{Prey}_{r2}), & \text{if } r > FADs \end{cases}, \tag{26}$$

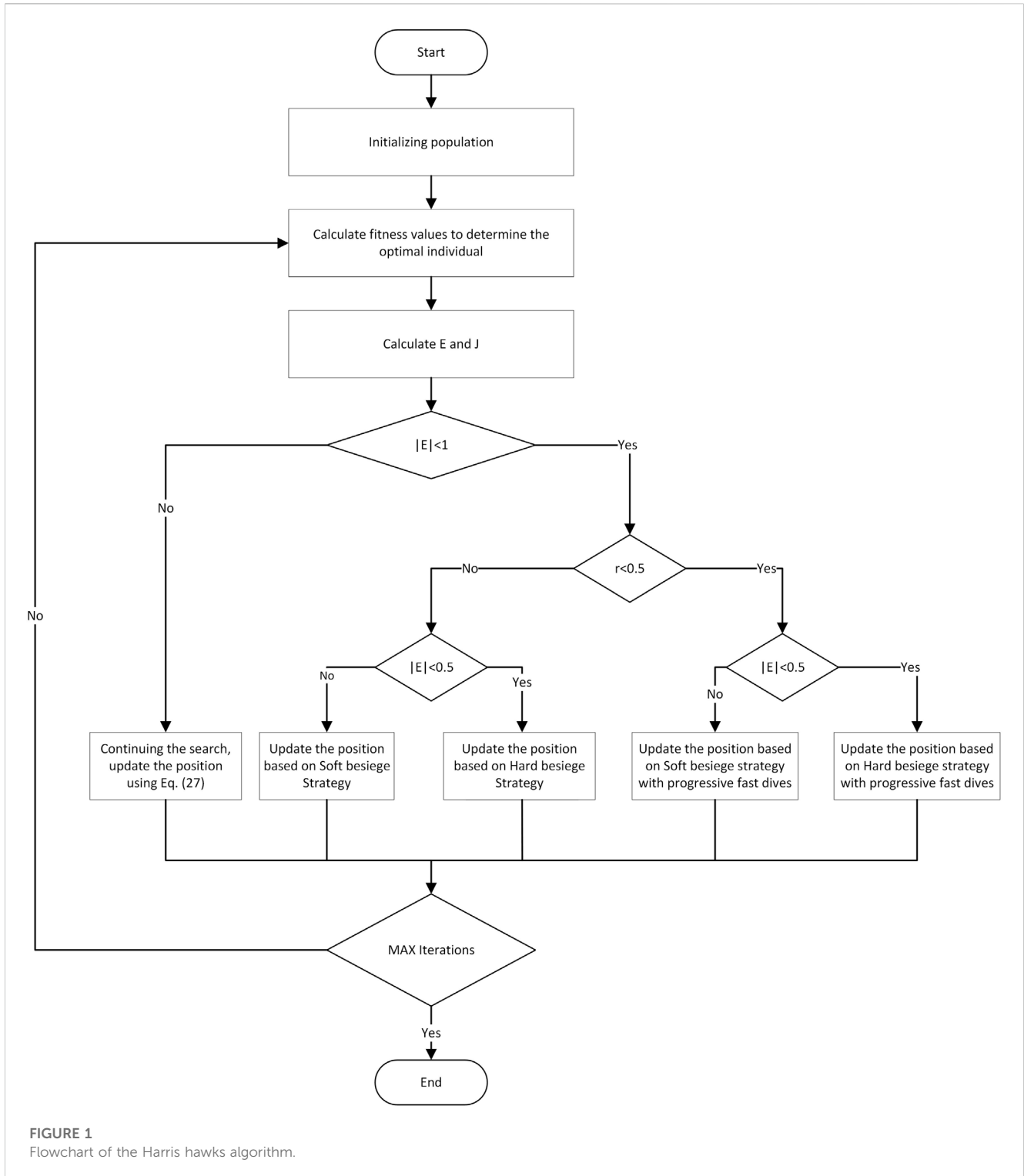
where $FADs = 0.2$ is a fixed value indicating the probability that a predator is affected by FADs. \vec{U} is a binary vector, and r is a random value between [0,1]. \vec{X}_{min} and \vec{X}_{max} are vectors containing the lower and upper bounds of the dimensionality. The subscripts $r1$ and $r2$ of $\overrightarrow{Prey}_{r1}$ and $\overrightarrow{Prey}_{r2}$ are the random indexes of the prey matrix.

(5) Marine memory

The purpose of this step is to update the elite matrix which is the optimal fitness value. After updating the prey matrix, the fitness value of each prey in the matrix is calculated. If it is better than the fitness value of the corresponding position in the elite matrix, it is replaced. Then, the optimal individual fitness value for the elite matrix is calculated.

3.4 Harris hawks optimization algorithm

Heidari et al. (2019) first proposed the HHO algorithm in 2019. The algorithm has strong global search capability and converges quickly with fewer parameters to tune. The algorithm is inspired by the Harris hawk's prey capture process. This process can dynamically adjust its prey capture strategy by considering the dynamic nature of the environment and the prey's escape patterns. The algorithm consists of three main phases: search, conversion between search and exploitation, and exploitation. Figure 1 shows the flowchart of the Harris hawks algorithm.



(1) Search phase

The Harris hawk searches and follows its prey with keen eyes. Considering that the prey is not easy to detect, the authors designed two strategies to simulate the Harris hawk’s prey capture.

$$X(t + 1) = \begin{cases} X_{rand}(t) - r_1|X_{rand}(t) - 2r_2X(t)|, & q \geq 0.5 \\ [X_{rabbit}(t) - X_m(t)] - r_3[lb + r_4(ub - lb)], & q < 0.5 \end{cases} \quad (27)$$

where $X(t+1)$ and $X(t)$ are the position of the $t+1$ iteration and the t iteration of the Harris hawk, respectively. t is the number of iterations. $X_{rabbit}(t)$ is the position of the prey rabbit and also the individual

position of the hawk with the optimal fitness value. $X_{rand}(t)$ represents the position of a randomly selected individual within the hawk population. r_1, r_2, r_3, r_4 , and q are all random values of $[0,1]$, where q is used to determine which strategy to choose. $X_m(t)$ is the average position of an individual and the mathematical formula is

$$X_m(t) = \sum_{k=1}^M \frac{X_k(t)}{M}, \tag{28}$$

where M denotes the population size. $X_k(t)$ denotes the position of the k th Harris hawk individual.

(2) Conversion phase of search and exploitation

In the HHO algorithm, it is assumed that prey escape consumes escape energy. Harris hawk can shift between different exploitation behaviors according to the prey's escape energy. Escape energy is defined as

$$E = 2E_0 \left(1 - \frac{t}{t_{max}} \right), \tag{29}$$

where E is the escape energy of the prey. E_0 is the initial energy value of the prey, a random number between $[0,1]$. t is the current iteration number, and t_{max} is the maximum number of iterations. When $|E| \geq 1$, the search phase is continued; when $|E| < 1$, we enter the exploitation phase.

(3) Exploitation phase

After entering the exploitation phase, hawks will dynamically adopt a capture strategy based on the real-time state of their prey. To choose a strategy, a random number r between $[0,1]$ is defined.

(1) Soft besiege strategy

When $|E| \geq 0.5$ and $r \geq 0.5$, the hawks choose a soft besiege strategy to capture the prey, and the position update equation is as follows:

$$X(t+1) = \Delta X(t) - E |JX_{rabbit}(t) - X(t)|, \tag{30}$$

$$\Delta X(t) = X_{rabbit}(t) - X(t), \tag{31}$$

where $\Delta X(t)$ denotes the distance between the prey's position (the optimal individual) and the individual's current position. J is a random number between $[0,2]$, which denotes the intensity of the prey's random jumps during the escape process, which simulates the rabbit's movement.

(2) Hard besiege strategy

When $|E| < 0.5$ and $r \geq 0.5$, the hard besiege strategy is selected and the position update formula is as follows:

$$X(t+1) = X_{rabbit}(t) - E|\Delta X(t)|. \tag{32}$$

(3) Soft besiege strategy with progressive fast dives

When $r < 0.5$ and $|E| \geq 0.5$, at this point, the prey possesses sufficient energy to evade pursuit and the Harris hawk needs to

softly besiege and quickly dive for an attack. The formula for updating positions is as follows:

$$X(t+1) = \begin{cases} Y, f(Y) < f(X(t)) \\ Z, f(Z) < f(X(t)) \end{cases}, \tag{33}$$

$$Y = X_{rabbit}(t) - E|JX_{rabbit}(t) - X(t)|, \tag{34}$$

$$Z = Y + S \cdot LF(D), \tag{35}$$

where $f()$ is the fitness function and $f(X(t))$ is the current fitness value, D is the problem dimension, and S is a random vector of problem dimensions. $LF()$ is the Levy function. The mathematical expression is

$$LF(x) = 0.01 \cdot \frac{\mu \cdot \sigma}{|v|^{\frac{1}{\beta}}}, \tag{36}$$

$$\sigma = \left(\frac{\Gamma(1+\beta) \cdot \sin(\frac{\pi\beta}{2})}{\Gamma(\frac{1+\beta}{2}) \cdot \beta \cdot 2^{\frac{\beta-1}{2}}} \right)^{\frac{1}{\beta}}, \tag{37}$$

where Γ is the gamma function, u and v are D -dimensional random vectors in $[0,1]$, and β is a default value set to 1.5.

(4) Hard besiege strategy with progressive fast dives

When $r < 0.5$ and $|E| < 0.5$, prey escape energy is not enough, but there is still a chance to escape. At this point, the Harris hawk needs to hard besiege and fast dive for surprise attack. The position update formula is as follows:

$$X(t+1) = \begin{cases} Y, f(Y) < f(X(t)) \\ Z, f(Z) < f(X(t)) \end{cases}, \tag{38}$$

$$Y = X_{rabbit}(t) - E|JX_{rabbit}(t) - X_m(t)|, \tag{39}$$

$$Z = Y + S \cdot LF(D), \tag{40}$$

where Y and Z are updated and are obtained from Eq. 39 and Eq. 40, respectively.

3.5 Bagging integration algorithm

Ensemble learning is a method that can improve generalization performance significantly than a single learner by combining multiple learners. There are many integration algorithms including Boosting, Stacking, and Bagging. In this paper, the Bagging integration learning algorithm is used. The Bagging algorithm (Bootstrap aggregation) is a widely used machine learning technique (Breiman, 1996). The idea is to improve the entire learner's generalization ability by combining multiple homogeneous learners' results. The Bagging algorithm has the capability to enhance accuracy and stability and prevent overfitting when combined with multiple models.

Bagging is suitable for small-sample problems. It is possible to significantly reduce the variance in the model training process by using a subset of the dataset and averaging the results, as well as mitigate the problem of overfitting. Boosting is appropriate for weak learners as it reduces bias. Its training process is serial, which requires training the base classifiers and updating the weights one by one, which can make overfitting a possibility for some problems. Stacking's training process is relatively complex,

requiring the training of multiple models and the fusion of predictions, which increases training time and computational cost. It may also lead to overfitting when the training data are small or the model complexity is high. As the HHO–SVR model is better suited for reducing variance than bias and our dataset is a small sample, Bagging algorithms are more appropriate for this study (Zounemat-Kermani et al., 2021; Mienye and Sun et al., 2022).

By using random sampling with dropouts from the original dataset, multiple subsets of the original dataset that have the same size are extracted from the original dataset. Base learners are trained independently using each subset. Finally, when performing regression predictions, the Bagging algorithm sums up all predictions and averages them in order to arrive at the final prediction.

3.6 Complete ensemble empirical mode decomposition with adaptive noise

EEMD and CEEMD aim to alleviate mode aliasing associated with EMD decomposition due to mode aliasing. They achieve this by introducing pairwise Gaussian white noise with opposite phases to the original signal. Nevertheless, despite these efforts, both algorithms may still retain some residual white noise after signal decomposition, which can impact the accuracy of subsequent decomposition processes. Torres et al. (2011) proposed a novel signal decomposition algorithm CEEMDAN. As part of EEMD (Wu and Huang, 2009), the algorithm averages the components immediately after adding fixed white noise to the original signal and performing the EMD decomposition. CEEMDAN adds adaptive white noise to the residual terms after each order of components and averages the components. Therefore, CEEMDAN has better decomposition performance and denoising ability compared to EEMD. The following are the decomposition steps:

- (1) The K th Gaussian white noise is added to the original signal to be decomposed, and a new signal is constructed.

$$x_{i(t)} = x(t) + \varepsilon \delta_i(t), i = 1, 2, 3, \dots, K, \tag{41}$$

where $x(t)$ is the original signal to be decomposed, $x_{i(t)}$ is the new signal, and ε is the Gaussian white noise adaptive coefficient. $\delta_i(t)$ denotes the i times added Gaussian white noise.

- (2) On each new signal obtained, EMD decomposition is performed to obtain K components. Then, the K components are summed and averaged to obtain the first-order modal components from the CEEMDAN decomposition.

$$IMF_1(t) = \frac{1}{K} \sum_{i=1}^K IMF_1^i(t), \tag{42}$$

$$R_1(t) = x(t) - IMF_1(t), \tag{43}$$

where $IMF_1(t)$ denotes the first-order modal component obtained from the CEEMDAN decomposition. $IMF_1^i(t)$ denotes the component obtained by the EMD decomposition of the i th signal in the first decomposition. $R_1(t)$ denotes the first-order residual term.

- (3) We continue to add the Gaussian white noise to the above residual term $\delta_j(t)$, thus obtaining the new signal again:

$$y_i(t) = R_1(t) + E_j(\varepsilon_j \delta_i(t)). \tag{44}$$

The EMD decomposition is performed again on the new signal to obtain K components, which we sum and average to produce the second-order modal components obtained from the CEEMDAN decomposition:

$$IMF_2(t) = \frac{1}{K} \sum_{i=1}^K IMF_2^i(t), \tag{45}$$

$$R_2(t) = R_1(t) - IMF_1(t), \tag{46}$$

where $y_i(t)$ is the newly obtained signal by adding the Gaussian white noise to the first-order residual term. $E_j(\cdot)$ denotes the j th-order modal component obtained by the EMD decomposition, $IMF_1(t)$ denotes the first-order modal component obtained by CEEMDAN decomposition, and $IMF_2^i(t)$ denotes the modal component obtained by EMD decomposition in the second decomposition of the i th new signal. $R_2(t)$ denotes the second-order residual term.

- (4) These steps are repeated until the residual term becomes a monotonic function that cannot be further decomposed. Finally, the original signal is decomposed into j modal components and one residual term with the following mathematical formula:

$$y(t) = \sum_{i=1}^j IMF_i(t) + R_{j-1}(t). \tag{47}$$

After obtaining the components and residual terms derived from the CEEMDAN decomposition, appropriate prediction models can be used to forecast each component. Finally, the forecasting results are linearly summated to obtain the final results. In this paper, the optimal model in the comparison was used to predict components.

4 Henry Hub natural gas price prediction process and variable screening

4.1 Data preprocessing

- (1) Data difference

The drastic volatility of the raw data will have an impact on the model's prediction. A data difference can eliminate some of the fluctuations and improve the smoothness of the data. The mathematical principle is relatively simple, subtracting the previous value from the next value to get a difference value. The formula is as follows:

$$y'(t) = y(t) - y(t-1), \tag{48}$$

where $y(t)$ is the raw data at moment t and $y(t-1)$ is the raw data at moment $t-1$. $y'(t)$ is the data after the first-order difference.

- (2) Data normalization

Data normalization is often used in machine learning preprocessing. When features in the dataset exhibit varying value

TABLE 1 Model parameter settings.

Model	Parameter setting
ARIMA	$(p, d, q) = (2,0,1)$
BPNN	Hidden layer neurons = 32; epochs = 50; batch_size = 256; activation = "relu"; loss = "mse"; optimizer = "adam"
ELM	Hidden layer neurons = 12; batch_size = 256; activation = "sigmoid"
GWO	Iterations: 30; population: 20; [0.1,1]
MPA	Iterations: 30; population: 20; [0.1,1]
HHO	Iterations: 30; population: 20; [0.1,1]
Bagging	Estimators = 15
VMD	$k = 5, \alpha = 200$

ranges, data normalization becomes crucial. Data normalization aims to standardize features on the same metric scale, to facilitate prediction and improve prediction accuracy. Therefore, the min–max normalization method is used to normalize the dataset so that all data sizes are between [0,1]. Its mathematical formula is as follows:

$$x^* = \frac{x - x_{min}}{x_{max} - x_{min}}, \quad (49)$$

where x^* is the data value after normalization, x is the input data before processing, and x_{min} and x_{max} are the minimum and maximum values in the input data, respectively.

4.2 Parameter setting

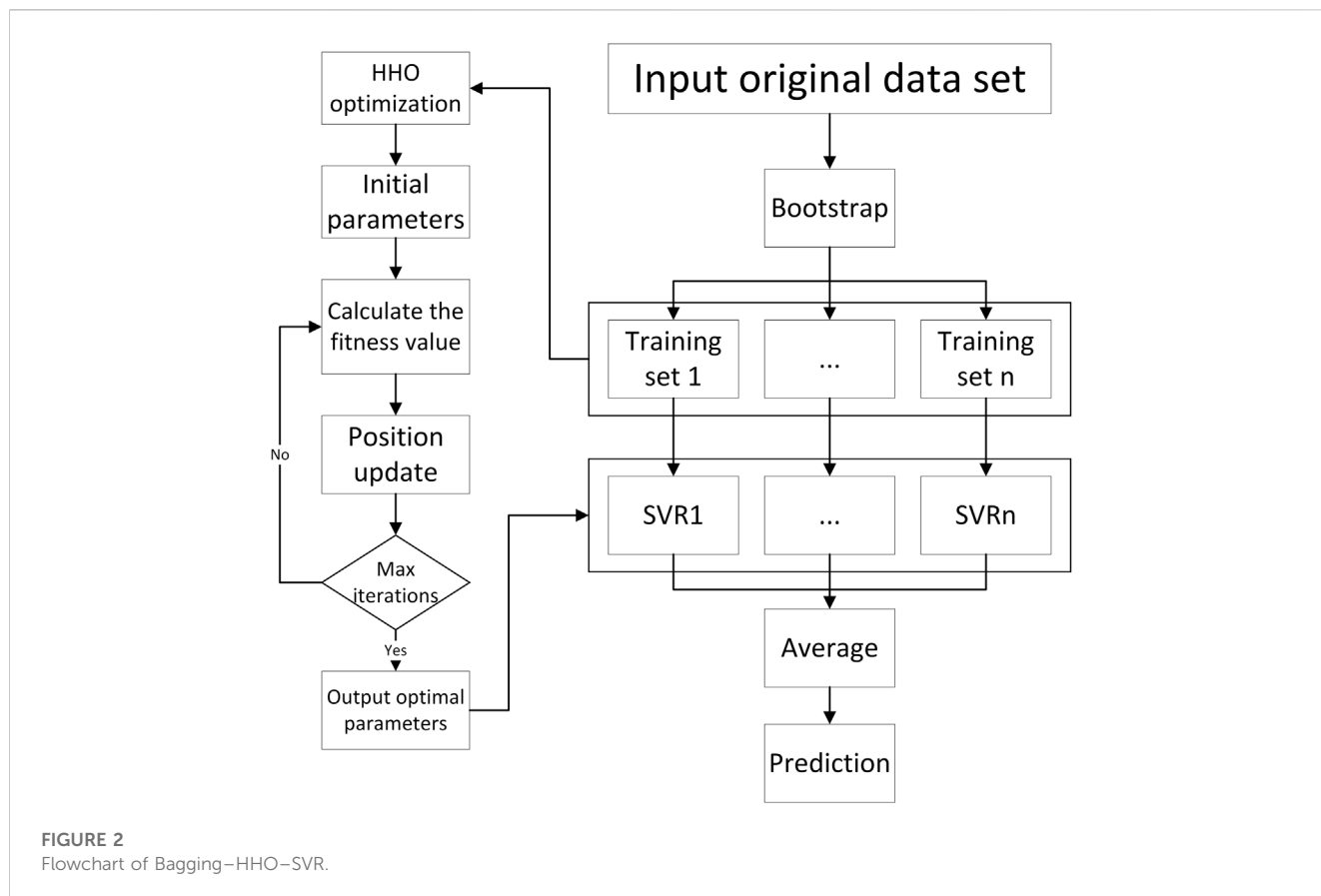
In this paper, we selected a variety of models for multi-level comparisons. Among the single models, we selected persistence, ARIMA, back-propagation neural network (BPNN), extreme learning machine (ELM), XGBoost, and SVR models. Among the optimization algorithms, we chose GWO, MPA, and HHO optimal algorithms. For the ensemble algorithm, we selected the Bagging algorithm. For the decomposition algorithm, we chose EEMD, VMD, and CEEMDAN algorithms. In the following, we explained some of the algorithms that require parameter setting.

The ARIMA model is the most commonly used econometric model. The main parameters of this model are (p, d, q) , where d is determined by the ADF test, and p and q are determined by the AIC and BIC values (Kaur et al., 2023), respectively. We determined $(p, d, q) = (2,0,1)$ by using the ADF test and BIC values. One of the most widely used neural network models is the BPNN, which consists of three layers: the input layer, the hidden layer, and the output layer. The number of neurons in its hidden layer is very important, usually depending on the size and dimension of the dataset, and there is no fixed selection method (Wang et al., 2020). We chose a hidden layer consisting of 32 neurons in this paper. The ELM is a single hidden layer feed-forward neural network that does not require iteration. Similar to other neural networks, the number of neurons in the hidden layer has a significant effect (Chaudhuri and Alkan B., 2021; Jiang et al., 2022b). We set up a single hidden layer with 12 neurons based on the data in this

paper and randomly initialized hidden weights and biases. XGBoost has been a popular gradient boosting model in recent years. Because it is used as a benchmark experiment in this paper, its parameters are the defaults. To facilitate comparisons, the SVR model uses default parameters from the benchmark model. The forecasting performance of SVR is mainly affected by C and γ (Ngo N et al., 2022), so we used optimization algorithms to optimize these two parameters. Based on previous literature and the performance of the three optimization algorithms in this paper, for fairness, we have the same settings for all three algorithms (Lu et al., 2022; Mohammed S et al., 2022; Sharma and Shekhawat et al., 2022; Su X et al., 2022): iterations: 30; population: 20; and lower and upper bound [0.1,1]. In the Bagging algorithm, the main factors that affect its performance include base learners and data samples (Mohammed and Kora et al., 2023). Data samples and the type of base learners were determined in this paper. Therefore, the parameters that need to be manually set in the Bagging algorithm are mainly the number of base learners. Based on the test results of the experiment, we set the number of base learners to 15. The VMD algorithm is mainly influenced by the decomposition modes K and the central frequency bandwidth α impact. The residual increases as α increases, and the larger the K value, the more the components generated by decomposition, which may lead to overdecomposition (Pei Y et al., 2022). We set $k = 5, \alpha = 200$. We list more detailed parameter settings in Table 1.

4.3 Henry Hub natural gas price prediction process

In this paper, we used CEEMDAN to decompose Henry Hub natural gas prices. The HHO algorithm was selected for SVR model parameter optimization, and the Bagging algorithm was used for ensemble learning of the HHO–SVR model. The final prediction model CEEMDAN–Bagging–HHO–SVR hybrid prediction model was constructed. Due to the fact that multi-steps ahead prediction can better mine the unique information contained in historical data, based on the experience of previous literature, we used a three-step ahead prediction method, which selects data from days $t-1$, $t-2$, and $t-3$ as input variables to predict data from day t (Zhang et al., 2021; Wang et al., 2023).



Specifically, the CEEMDAN decomposition method in previous literature usually directly decomposes the entire time series, including the training set and test set. After obtaining the components, each one is predicted separately, and finally, they are summed in order to obtain the predicted value. Due to the fact that the test set belongs to future data, data leakage will occur when all test sets are unknown and training sets are decomposed simultaneously (Qian Z et al., 2019; Gao R et al., 2021). We made improvements to this problem by gradually decomposing and predicting time series using a rolling approach. The process is as follows.

First, the CEEMDAN decomposition is performed on the entire training set and then one step backward is predicted to obtain the first predicted value.

Next, the training set is extended backward by one data point, CEEMDAN decomposition is performed on the new training set, and another backward prediction step is made to obtain the second predicted value.

.....

These steps are repeated until all predicted values are obtained.

For the convenience of comparison, we retained the previous decomposition method for EEMD and VMD and only used the rolling decomposition method for CEEMDAN.

In the following, we provide a detailed introduction to the process of combining rolling decomposition with the Bagging algorithm, HHO algorithm, and SVR. This is the entire prediction process.

(1) The eight screened influencing factors together with the historical natural gas price data were used as input variables to compose the input dataset.

- (2) Data preprocessing work such as data difference and normalization was performed on the input dataset. This can unify data standards and improve data quality and prediction accuracy.
- (3) The processed dataset was divided into training and testing sets, with a ratio of 8:2 between the training and testing sets.
- (4) CEEMDAN decomposition was performed on the current training set to obtain six modal components. Each component was randomly sampled into n subsets as an input dataset for the Bagging algorithm.
- (5) n subsets were input into the HHO algorithm for parameter optimization to obtain the optimal parameters. The optimized parameters were input into the corresponding SVR model for each subset separately.
- (6) n subsets were independently predicted using n SVR models, predicting only one step backward at a time. The arithmetic average of n prediction results was calculated to obtain the predicted value of one component. Finally, the prediction values of the six components were summed to obtain the final single predicted value.
- (7) The training set was extended one step backward to obtain a new training set. Steps 4–6 were repeated to obtain other predicted values.

In the above steps, steps 4–6 include the combination process of the Bagging algorithm, HHO algorithm, and SVR. Figure 2 more intuitively shows the combination process of Bagging, HHO, and SVR. Rolling decomposition prediction is mainly carried out in step 7, and Figure 3 shows this process more intuitively.

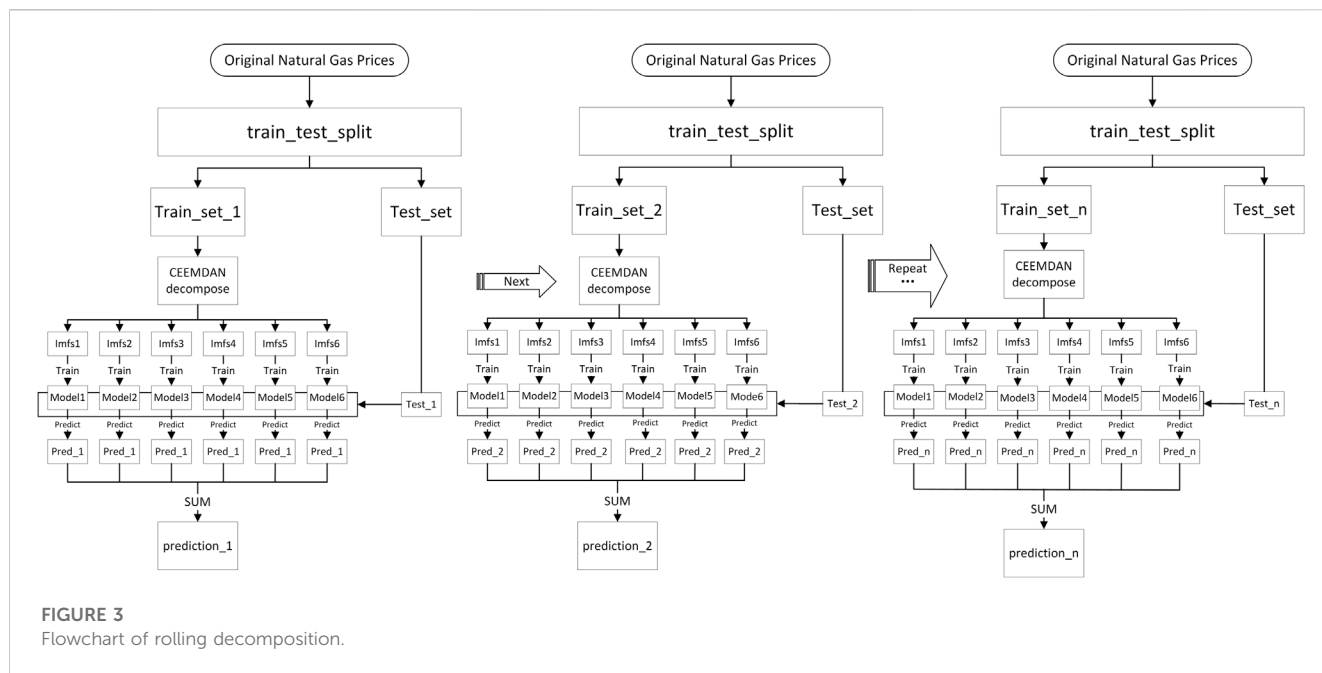


FIGURE 3
Flowchart of rolling decomposition.

TABLE 2 Variables selected initially.

Aspect	Influence factor	Symbol
Economic indicators	Historical natural gas price	X_0
	Coal price	X_1
	Crude oil price	X_2
	Heating oil price	X_3
	GDP	X_4
	CPI	X_5
Natural gas market	Natural gas supply	X_6
	Natural gas demand	X_7
	Natural gas drilling activities	X_8
	Natural gas imports	X_9
	Natural gas storage	X_10
Climatic factors	Maximum temperature	X_11
	Minimum temperature	X_12
	Heating degree days	X_13
	Cold degree days	X_14

global natural gas price volatility. According to their analysis, natural gas prices are robustly correlated with factors such as crude oil prices and natural gas production. Li et al. (2019) investigated the correlation between Henry Hub natural gas prices and WTI crude oil prices through a multi-scale perspective. Zheng et al. (2023) used the feature select algorithm to screen 20 variables affecting natural gas prices. It found that natural gas drilling activities and natural gas import and export prices had the most impact. Azadeh et al. (2012) validated their hybrid model for enhanced natural gas price forecasting in the industrial sector, utilizing input variables such as natural gas consumption, CPI, and GDP. Su et al. (2019) used machine learning on Henry Hub natural gas prices by considering factors such as temperature and heating oil prices as input variables and finally obtained better prediction results.

The choice of input variables significantly influences the forecasting performance of the constructed model. We used the literature analysis method to select 14 external influence factors on natural gas prices from four aspects initially in this paper. These factors included economic indicators, natural gas market, and climatic factors. Table 2 shows the 14 influence factors with the historical natural gas price. Table 3 shows descriptive statistics for all variables we initially selected.

(1) Economic indicators

4.4 Variable screening

4.4.1 Initial variable selection

Natural gas price prediction is affected by numerous complex external factors besides historical natural gas price data. Li et al. (2017) analyzed 20 variables affecting Henry Hub’s natural gas prices using factor analysis and found that natural gas demand and economic conditions were more prominent. Stajic et al. (2021) employed multiple linear regression to analyze the critical drivers of

Concurrently, overall economic performance and inflation levels also directly or indirectly affect natural gas supply and demand dynamics, subsequently influencing its price. GDP and CPI are primary indicators reflecting a country’s economic status and need to be considered comprehensively among the factors affecting natural gas prices. Energy prices and economic indicators are significantly correlated. Natural gas, as a cleaner energy source, is directly influenced by factors such as coal prices, crude oil prices, and heating oil prices, and when

TABLE 3 Descriptive statistics of variables.

Variable	Count	Mean	Std.	Min.	25%	50%	75%	Max.
X_0	252.000	4.434	2.179	1.630	2.850	3.835	5.635	13.420
X_1	252.000	62.260	18.039	31.530	50.673	62.800	69.885	122.680
X_2	252.000	62.480	25.237	16.550	44.275	59.275	81.270	133.880
X_3	252.000	1.834	0.761	0.524	1.310	1.812	2.250	3.801
X_4	252.000	2.119	5.718	-34.870	1.068	2.390	3.400	39.140
X_5	252.000	222.134	26.8758	175.100	201.075	225.822	241.372	278.802
X_6	252.000	2,119,370.000	465,425.000	1,368,370.000	1,742,510.000	2,068,740.000	2,417,590.000	3,424,300.000
X_7	252.000	2,119,370.000	465,425.000	1,368,370.000	1,742,510.000	2,068,740.000	2,417,590.000	3,424,300.000
X_8	252.000	1,246.050	493.095	250.000	881.750	1,168.000	1749.250	2017.000
X_9	252.000	288,645.000	58,466.200	174,225.000	238,316.000	282,064.000	334,002.000	426,534.000
X_10	252.000	6,911,110.000	804,148.000	5,041,970.000	6,289,200.000	7,007,010.000	7,548,360.000	8,384,090.000
X_11	252.000	65.415	16.008	38.980	50.680	65.705	80.658	89.960
X_12	252.000	41.706	14.185	18.680	28.620	41.055	55.745	63.550
X_13	252.000	349.821	308.601	3.000	39.000	282.500	627.500	968.000
X_14	252.000	116.869	125.040	2.000	14.000	51.500	220.000	407.000

prices of other energy sources rise, businesses and consumers may seek to use natural gas as an alternative energy source, thereby increasing its demand and driving up its price. Therefore, when analyzing the fluctuations and trends in natural gas prices, these economic indicators and related energy price factors must be taken into account. Preliminarily, we selected GDP, CPI, coal prices, heating oil prices, and crude oil prices as factors in economic indicators in this paper.

(2) Natural gas market

Supply and demand are the major factors determining commodity prices. Therefore, the balance of supply and demand is critical to maintaining stable natural gas prices. Natural gas drilling and production activities directly influence the supply of natural gas, which plays a significant role in determining the price of natural gas. In addition, natural gas import and storage have a direct or indirect impact on natural gas supply and demand. Preliminarily, we selected natural gas supply and demand, natural gas drilling activities, natural gas imports, and natural gas storage as factors in the natural gas market in this paper.

(3) Climatic factor

Due to the seasonal nature of natural gas, temperature and climate changes will have a direct impact on the seasonal demand for natural gas, the stability of the supply chain, and the storage requirements, which will in turn impact the price of natural gas. Preliminarily, we selected the maximum temperature and the minimum temperature and heating degree days (HHDs) and cold degree days (CCDs) as factors in this paper.

4.4.2 Grey relation analysis

As a result of the preliminary selection of variables, it is necessary to further screen them to determine which variables have a higher correlation with Henry Hub natural gas prices to reduce the subjectivity of the input variables and improve prediction accuracy. Using the 14 variables selected initially in this paper, we conducted a GRA on natural gas prices and ultimately identified eight external influencing factors as input variables to the model along with historical natural gas prices. GRA is a method for conducting system analysis and determining the importance of factors that affect the development of the system (Arce et al., 2015). The basic idea is to establish a reference sequence that changes over time according to certain rules. Then, we need to treat each influence factor as an analysis sequence and compute the correlation between each analysis sequence and the reference sequence. A higher correlation indicates a stronger relationship between the reference sequence and the analysis sequence. The specific flow of the algorithm is as follows:

(1) Determination of analysis and reference sequences

The natural gas price data are taken as the reference sequence $Y = Y(k), k = 1, 2, \dots, n$; the input variables are taken as the analysis sequences $X_i = X_i(k), k = 1, 2, \dots, n, i = 1, 2, \dots, m$, where n is the number of data contained in each variable and m is the number of variables contained in the analysis sequence.

(2) Programmability

Since the individual factor columns in the analysis series may be inconvenient to compare due to different magnitudes, this paper adopts the min-max method to perform dimensionless operations on the above series.

TABLE 4 Grey correlation ranking of variables.

Variable	Grey correlation
X_4	0.8
X_9	0.8
X_1	0.78
X_8	0.78
X_2	0.74
X_3	0.72
X_7	0.72
X_14	0.72
X_13	0.69
X_10	0.68
X_11	0.68
X_12	0.68
X_6	0.66
X_5	0.64

The meaning of the bold values is the first eight variables filtered in the grey correlation analysis.

(3) Grey relation calculation

The correlation coefficient is calculated between each analysis sequence and reference sequence separately. The mathematical formula is

$$\xi_i(k) = \frac{\min_i \min_k |Y(k) - X_i(k)| + \rho \max_i \max_k |Y(k) - X_i(k)|}{|Y(k) - X_i(k)| + \rho \max_i \max_k |Y(k) - X_i(k)|}, \tag{50}$$

where ρ is the resolution coefficient, the value interval is (0, 1), which is usually taken as 0.5, and in this paper, it is taken as 0.5.

(4) Average correlation coefficient

The correlation coefficient is the level of correlation between the analysis sequence and the reference sequence at different time points. It is necessary to concentrate them into a final value (average them) to facilitate holistic comparisons. The mathematical formula is as follows:

$$r_i = \sum_{k=1}^n \xi_i(k), \tag{51}$$

where r_i is the grey correlation between the analysis sequence and each reference sequence, and the closer its value is to 1, the greater is the correlation of the analysis sequence to the reference sequence.

Table 4 shows the grey correlation between natural gas price and the remaining 14 variables in this paper. A grey correlation less than 0.7 indicates a low correlation between the series. So, this paper eliminates the grey correlations less than 0.7 and filters out the final eight variables that will be used together with the Henry Hub historical natural gas price as input variables.

5 Empirical analysis and discussion

5.1 Data description

Historical Henry Hub natural gas price data, coal price data, crude oil price data, heating oil price data, natural gas demand data, natural gas drilling activities data, and natural gas import data were acquired from the U.S. Energy Information Administration website (<https://www.eia.gov>). The GDP data were acquired from the U.S. Bureau of Economic Analysis website (<https://www.bea.gov>). The CDD data were acquired from the National Oceanic and Atmospheric Administration website (<https://www.ncdc.noaa.gov>). Table 5 describes variables in detail. All of the above data are monthly data from January 2001 to December 2021, totaling 252 data. Figure 4 shows the strong volatility and nonlinear characteristics of the natural gas price data.

In energy price forecasting, the raw data are mostly divided into training and test sets, and there is no uniformity in the division ratio (Lu H et al., 2021). In particular, we use a total of 202 (top 80%) monthly data from January 2001 to October 2017 as the training set and a total of 50 (bottom 20%) monthly data from November 2017 to December 2021 as the test set. The reason for selecting this time interval in this paper is that the natural gas price during this period has experienced two peak periods and three trough periods, with great volatility. Due to the forecasting process, there are always invariably unforeseen and uncontrollable “black swan” events that may occur. Due to this, we selected a period of time that avoids the uncontrollable factor of the Russian Ukrainian war during 2022. Since the collected coal price data are annual data and GDP data are quarterly data, this paper uses the EViews software to convert their frequencies to monthly data. Model training and testing are conducted with Spyder 5.4.3 (Python 3.9) software. The code in this study is implemented in Python. The experimental environment includes Windows 10 (64-bit), a Core (TM) i5-8250U CPU @1.80 GHz and 12.0 GB of RAM. For the plotting part, we used Origin 2022 and Visio software.

5.2 Evaluation criteria

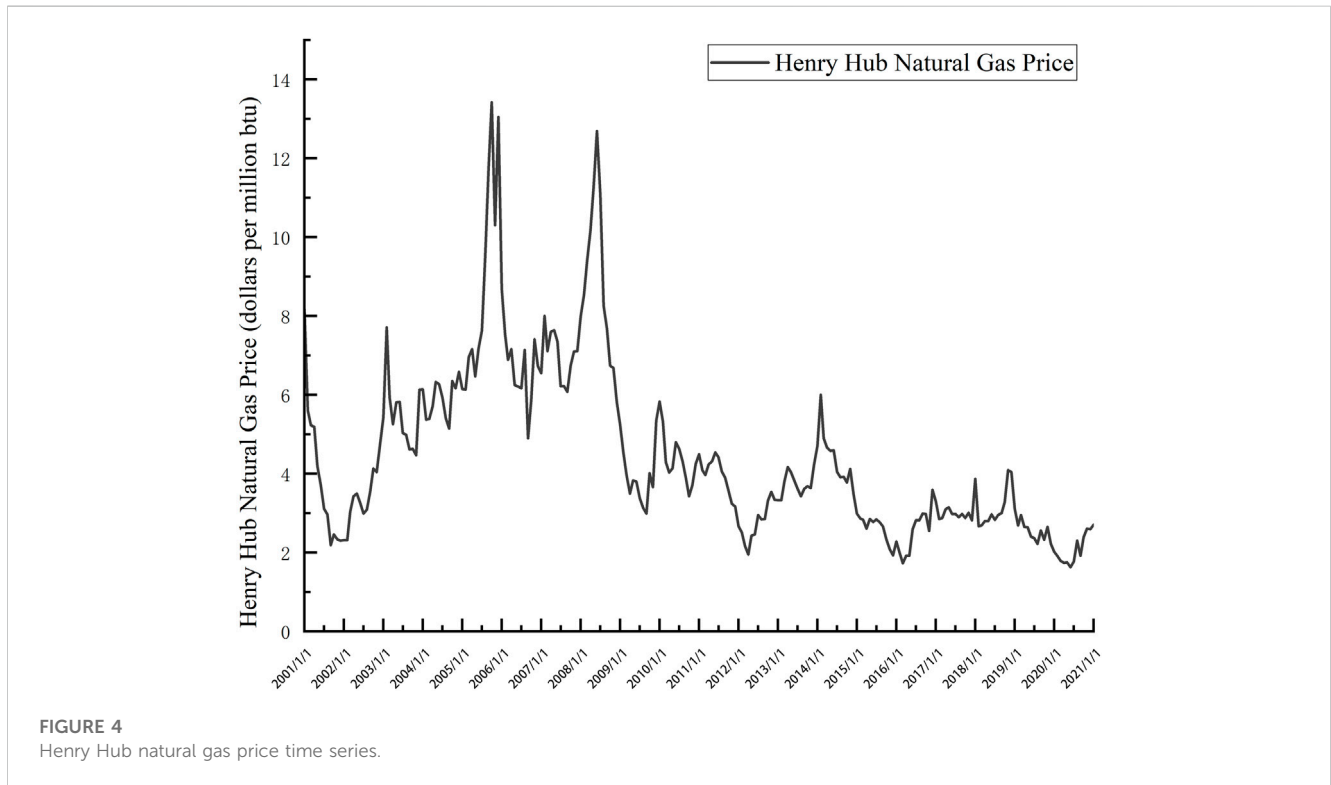
In past research, multiple evaluation indicators were usually used to compare the developed model and other models for forecasting capacity. However, there is no specific standard that exists for model evaluation (Dong Y et al., 2020).

To better compare the prediction effect of models, we used five evaluation metrics to evaluate the prediction performance of models. They are the mean square error (MSE), mean absolute error (MAE), coefficient of determination (R^2), root mean square error (RMSE), and mean absolute percentage error (MAPE). Among them, the lower values of MSE, MAE, RMSE, and MAPE signify the higher prediction accuracy of the model. Contrary to this, a greater R^2 value indicates a more accurate fitting of the model. The mathematical formulas for each evaluation criteria are shown as follows:

$$MSE = \frac{1}{N} \sum_{i=1}^N (y_i - \hat{y}_i)^2, \tag{52}$$

TABLE 5 Details of input variables.

Variable	Data description	Unit	Source
Historical natural gas price	Historical Henry Hub natural gas spot price	Dollars/million Btu	EIA
Coal price	Central Appalachia spot prices	Dollars/ton	EIA
Crude oil price	Cushing, OK WTI spot price FOB	Dollars/barrel	EIA
Heating oil price	New York Harbor No. 2 heating oil spot price FOB	Dollars/gallon	EIA
Natural gas demand	US total natural gas consumption	Million cubic feet	EIA
GDP	Real gross domestic product: percent change from quarter one year ago	Percentage	BEA
Natural gas drilling activity	U.S. crude oil and natural gas rotary rigs in operation	Count	EIA
Natural gas import	U.S. total natural gas imports	Million cubic feet	EIA
Cooling degree days	Contiguous U.S. cooling degree days	°DF	NOAA



$$MAE = \frac{1}{N} \sum_{i=1}^N |y_i - \hat{y}_i|, \tag{53}$$

$$R^2 = \frac{[\sum_{i=1}^N (y_i - \bar{y}_i)(\hat{y}_i - \widehat{\bar{y}}_i)]^2}{[\sum_{i=1}^N (y_i - \bar{y}_i)^2][\sum_{i=1}^N (\hat{y}_i - \widehat{\bar{y}}_i)^2]}, \tag{54}$$

$$RMSE = \sqrt{\frac{1}{N} \sum_{i=1}^N (y_i - \hat{y}_i)^2}, \tag{55}$$

$$MAPE = \frac{1}{N} \sum_{i=1}^N \frac{|y_i - \hat{y}_i|}{y_i} * 100, \tag{56}$$

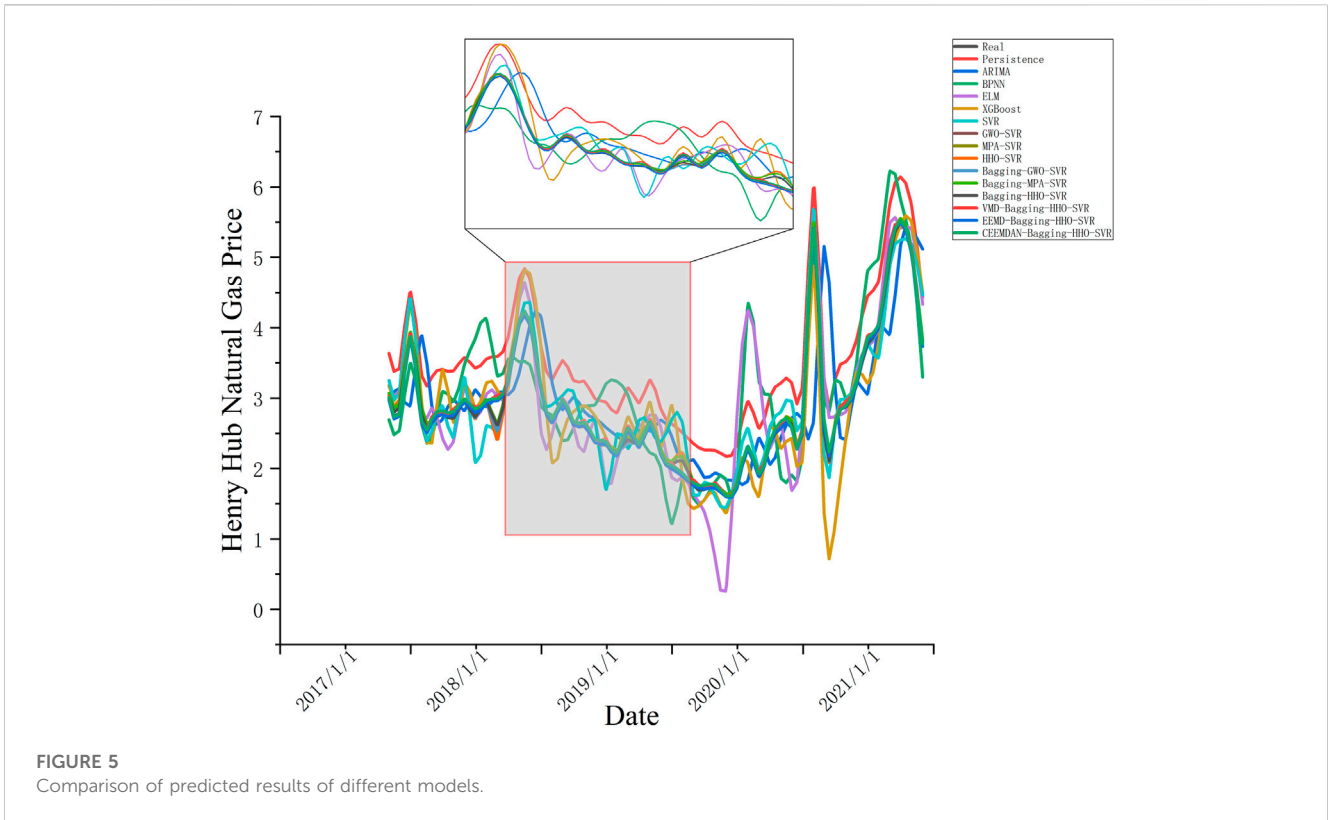
where y_i is the actual value and \hat{y}_i is the model's forecasting value. N is the total number of samples. \bar{y}_i is the mean of the real values, and $\widehat{\bar{y}}_i$ is the mean of the forecasting values.

5.3 Experimental results

5.3.1 Comparative analysis of forecast accuracy

To compare the performance of the different models clearly, a multi-level comparative analysis is performed in this paper. Figure 5 shows the fitting curves of different models. Figure 6 shows the histograms of the comparison of each model on five evaluation indicators. Table 6 demonstrates the detailed prediction accuracy of each model across the five evaluation indicators.

The five evaluation indicators of the model are comprehensively compared. In the single model comparison, the values of MSE, RMSE, and R^2 gradually decreased from the persistence model to the SVR model. However, the values of MAE improved from the



persistence model to the BPNN model, and the values of MAPE increased from the persistence model to the ELM model. Generally, forecasting performance tends to improve. The economic model ARIMA performed only slightly better than the most basic persistence model in time series forecasting.

This may be because traditional economic models usually cannot fully capture the nonlinear characteristics of data and have certain limitations when facing long-term predictions and complex data. Moreover, ARIMA requires tedious parameter settings, which is a significant drawback compared to machine models. BPNN and ELM are both neural network models in machine learning. BPNN usually requires multiple iterations to adjust the weights and reduce the loss value. ELM can automatically adjust the hidden layer weights and bias, which trained only once without iterations. In this paper, ELM has better performance compared to BPNN. XGBoost has also been widely used in recent years in major research fields. It is suitable for medium and large sample data, and its performance in this study prediction is moderate. The regularization term added to it reduces the overfitting performance of the model. R^2 is improved to 0.8241, but the rest of the evaluation metrics are general. This indicates that XGBoost may not be suitable for the dataset in this paper. The SVR model, a longstanding prediction model that has maintained stability with small-sample data over the decades, exhibits the same reliability in this paper. Compared with other single machine learning models, SVR showed high prediction accuracy. Therefore, the SVR model is selected for the subsequent study.

In the optimization model, three different optimization algorithms are combined with the SVR model for parameter

finding. Compared to the single SVR model, the forecasting performance of all three optimization models has been improved. However, the performance of all three algorithms is almost the same. Therefore, we performed ensemble learning on all three algorithms.

In the ensemble model, the three optimization models GWO-SVR, MPA-SVR, and HHO-SVR are integrated and learned. In the comparison between the three ensemble models and the optimization model, all five evaluation indicators have improved. This is mainly a benefit by the Bagging algorithm reducing the variance of the model. The Bagging-HHO-SVR model performs most accurately among them, with better prediction accuracy for all five evaluation indicators compared to the others. This indicates that HHO combined with Bagging algorithm has better performance than the other two optimization algorithms. Therefore, we choose the Bagging-HHO-SVR model as the decomposed prediction model.

In the decomposition algorithms, we first used both EEMD and VMD decomposition methods for comparison. In order to compare with the new rolling decomposition method, we applied the old method to the EEMD and VMD decomposition which decomposes the whole time series. There is no significant difference in performance between the two algorithms, and both are stronger than the ensemble model, with EEMD performing slightly better than VMD. However, due to the problem of data leakage that this method may cause, we used the new rolling forecasting approach in the CEEMDAN decomposition algorithm. In this way, the dataset is decomposed many times and a large amount of future data is not included in the decomposition process. The prediction performance of this method is the best among all the algorithms. The CEEMDAN-Bagging-HHO-SVR model improves nearly 92% on MSE compared to the Bagging-HHO-SVR model.

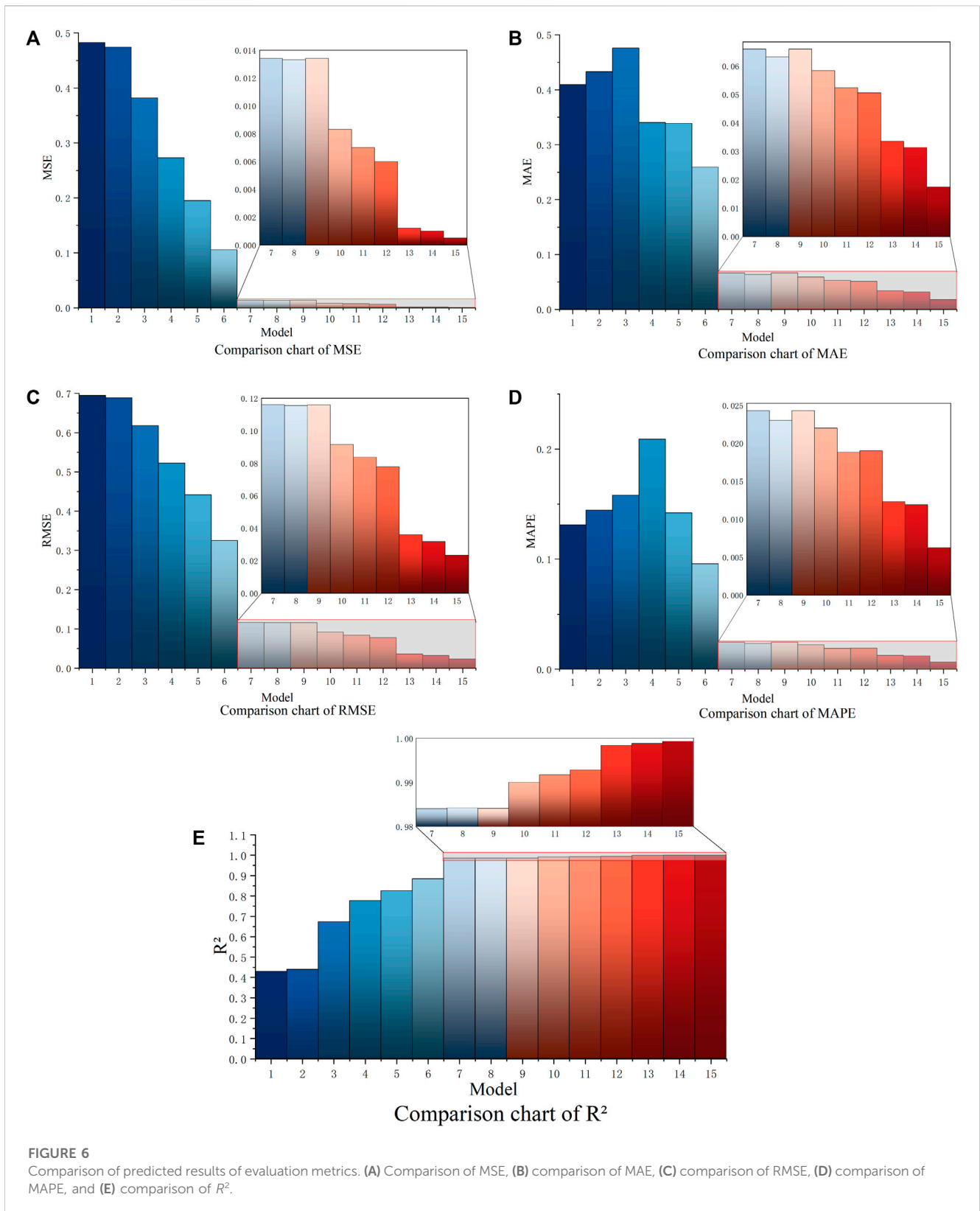


FIGURE 6 Comparison of predicted results of evaluation metrics. (A) Comparison of MSE, (B) comparison of MAE, (C) comparison of RMSE, (D) comparison of MAPE, and (E) comparison of R².

Moreover, we conducted predictions and comparisons using different features before and after GRA screening as input variables for the CEEMDAN–Bagging–HHO–SVR model to demonstrate the effect of GRA on model performance. Table 7

shows the predicted results. From the table, we can see that in the prediction using GRA, the five evaluation indicators have significantly improved. Specifically, MSE values decreased from 0.0027 to 0.0005, MSE values decreased from 0.0468 to

TABLE 6 Prediction accuracy comparison of different models.

Model	MSE	MAE	R^2	RMSE	MAPE	Rank
Persistence (Model_1)	0.8447	0.6487	0.9725	0.9191	0.0967	15
ARIMA (Model_2)	0.6429	0.6011	0.9791	0.8018	0.0881	14
BPNN (Model_3)	0.5368	0.6016	0.5953	0.7327	1.0359	13
ELM (Model_4)	0.2730	0.3405	0.7762	0.5224	0.2090	12
XGBoost (Model_5)	0.1948	0.3389	0.8241	0.4414	0.1420	11
SVR (Model_6)	0.1055	0.2592	0.8835	0.3248	0.0956	10
GWO-SVR (Model_7)	0.0134	0.0660	0.9840	0.1160	0.0243	9
MPA-SVR (Model_8)	0.0133	0.0632	0.9842	0.1155	0.0230	8
HHO-SVR (Model_9)	0.0134	0.0660	0.9841	0.1159	0.0243	7
Bagging-GWO-SVR (Model_10)	0.0083	0.0584	0.9900	0.0915	0.0220	6
Bagging-MPA-SVR (Model_11)	0.0070	0.0524	0.9917	0.0837	0.0188	5
Bagging-HHO-SVR (Model_12)	0.0060	0.0506	0.9928	0.0778	0.0190	4
VMD-Bagging-HHO-SVR (Model_13)	0.0012	0.0335	0.9984	0.0359	0.0123	3
EEMD-Bagging-HHO-SVR (Model_14)	0.0010	0.0313	0.9988	0.0317	0.0119	2
CEEMDAN-Bagging-HHO-SVR (Model_15)	0.0005	0.0174	0.9993	0.0233	0.0062	1

The meaning of the bold values is the best model in the comparison of the different types of models.

TABLE 7 Comparison of prediction results before and after input variable screening.

Model	MSE	MAE	R^2	RMSE	MAPE
CEEMDAN-Bagging-HHO-SVR (NO-GRA)	0.0027	0.0468	0.9966	0.0528	0.0159
CEEMDAN-Bagging-HHO-SVR (GRA)	0.0005	0.0174	0.9993	0.0233	0.0062

TABLE 8 Prediction results of the proposed model for different regions.

Region	Model	MSE	MAE	R^2	RMSE	MAPE
Henry Hub	CEEMDAN-Bagging-HHO-SVR	0.0005	0.0174	0.9993	0.0233	0.0062
UK NBP	CEEMDAN-Bagging-HHO-SVR	0.0309	0.1669	0.9989	0.1758	0.0338
Japan LNG	CEEMDAN-Bagging-HHO-SVR	0.0078	0.0797	0.9943	0.0883	0.0084

0.0174, RMSE values decreased from 0.0528 to 0.0233, MAPE values decreased from 0.0159 to 0.0062, and R^2 values increased from 0.9966 to 0.9993. This is mainly because we removed variables with low correlation through GRA, reduced the input dimension of the model, and thus improved prediction performance. As we can see, this method is indeed very effective, and this proves that the input variables we selected are reasonable and effective for the model.

The proposed hybrid model demonstrated excellent prediction results in Henry Hub’s empirical study of monthly natural gas prices. Furthermore, we also predicted NBP natural gas prices and Japan LNG prices to verify whether the model has the same excellent performance in other regions. Table 8 shows the prediction accuracy of different regions. The results show that the proposed model performed well in forecasting different regions. Therefore, the

proposed model is not only applicable to Henry Hub natural gas prices but also has reference value for natural gas price research in other regions.

5.3.2 Characteristic importance analysis

Many current machine learning models can make accurate predictions, but they do not explain how they make them because complex problems often have black-box properties, although they can give high-accuracy results. It is difficult to explain the inner principles and which features have the most significant impact on prediction results. Therefore, we use the permutation importance method to analyze the feature importance of the Bagging-HHO-SVR model to assess how much each feature affects Henry Hub natural gas price prediction. The basic idea of the permutation importance

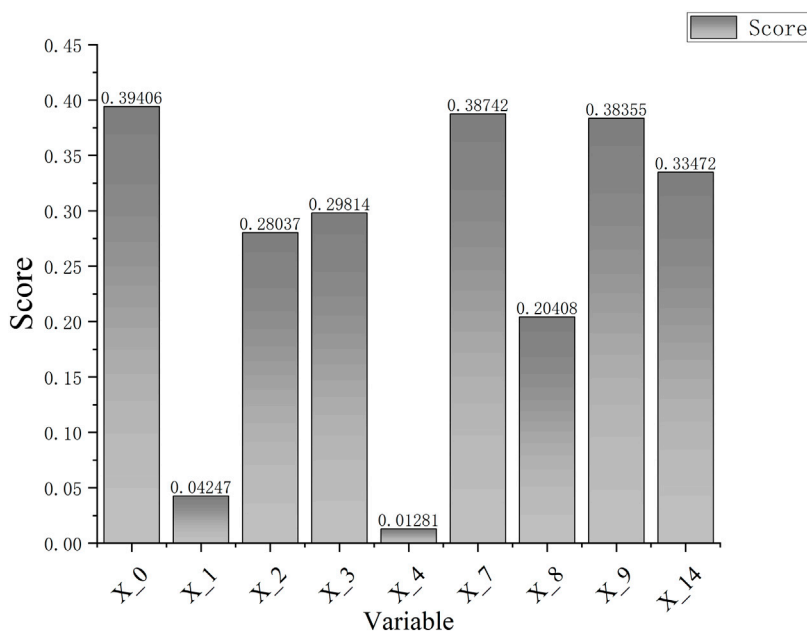


FIGURE 7
Histogram of feature importance.

method is to sequentially shuffle the sample order of each feature. Then, it evaluates the error size of the disordered feature compared to the normal prediction results. The larger the error, the more significant the effect of the feature on the prediction result. Figure 7 shows the result of permutation importance, which demonstrates the extent to which each feature influences Henry Hub natural gas prices.

According to the analysis results, historical natural gas prices, natural gas imports, and natural gas demand are among the top three factors. These factors are significant factors affecting Henry Hub’s natural gas price prediction. Among them, historical natural gas prices have the highest score. In univariate forecasts, historical natural gas prices are usually used as the only input variable. In multivariate forecasts, although many external influences are added as input variables, historical natural gas prices are still critical factors. It implies potential features such as long-term trends and seasonal fluctuations in natural gas prices, which are not present in external factors. Natural gas demand ranks second, with demand being a major component of the market’s supply and demand balance. When the demand for natural gas increases, the supply of natural gas is delayed and the market supply of natural gas may fall short of demand. Then, natural gas prices will increase. Conversely, when demand decreases, supply may exceed demand and the natural gas prices will decrease. Natural gas imports rank third. When there is a sudden increase in natural gas demand and the country cannot meet supply from its domestic natural gas production, it needs to import natural gas from abroad to bridge the demand gap. Consequently, natural gas imports alter natural gas prices by impacting supply and demand equilibrium, then influencing natural gas prices.

6 Conclusion and recommendations

Focusing on the nonlinearity and nonstationarity of natural gas prices caused by multiple influence factors and the limitations of single models, we proposed a CEEMDAN–Bagging–HHO–SVR hybrid model that considered various natural gas price influence factors and empirically analyzed the monthly natural gas price in Henry Hub in this paper. From the results of the empirical analysis over a 20-year period from January 2001 to December 2021, we can draw some conclusions:

- (1) The CEEMDAN–Bagging–HHO–SVR model combines four algorithms: “decomposition algorithm,” “ensemble algorithm,” “optimization algorithm,” and “prediction model.” The addition of each algorithm further improves the forecasting performance of the model. The constructed model has extremely high prediction accuracy in forecasting natural gas prices in Henry Hub and also performs well in other regions. This indicates that the constructed model has universal applicability.
- (2) In multivariate prediction, the choice of input variables is extremely important. We used GRA in this experiment to analyze the influence factors, which significantly improved the prediction accuracy of the model while reducing the subjectivity of input variable selection. Consequently, the input variables selected in this paper are very suitable for the forecasting of Henry Hub natural gas.
- (3) Using a characteristic importance analysis, we conclude that historical natural gas prices, natural gas demand, and natural gas imports influence natural gas prices at Henry Hub greatly. This can provide some reference for relevant personnel.

Natural gas is emerging as a valuable, clean energy source, playing a vital economic and environmental role on a global scale as global natural gas trade expands. Energy market participants and policymakers require accurate natural gas price predictions. Energy companies can increase their competitiveness by formulating procurement strategies and pricing policies based on natural gas price predictions. For consumers, accurate natural gas price predictions can help them rationalize energy expenditures and reduce energy costs. Government agencies can also use natural gas price forecasts to optimize their energy policies and promote clean energy and sustainable development. As the most influential natural gas trading center in North America, the Henry Hub natural gas price fluctuations have a wide impact on the global energy market. The Henry Hub natural gas price is a major wind vane for international natural gas prices. Energy traders, investors, and energy users need to accurately forecast Henry Hub natural gas prices. Therefore, the proposed hybrid model is a potential analytical tool for investors interested in developing a strategic approach. Moreover, we put forward some recommendations based on the experimental results of this paper:

- (1) For countries, the constantly changing international situation has a significant impact on the import and export of natural gas. The leaders of countries should always pay attention to the dynamics of major natural gas import and export countries. They should strengthen connections with these countries or sign strategic agreements to ensure the stability of their own natural gas import and export.
- (2) For governments, it is necessary to strengthen its regulatory strategy on the natural gas market and strive to ensure the rationality of natural gas prices and the stability of the industrial chain. It is also important for the government to formulate energy diversification development strategies in the future in order to reduce its dependence on fossil fuels, for example, increasing policy incentives for the development of renewable energy sources such as solar and wind energy and developing various alternative energy sources to ensure the stability of the energy supply.
- (3) For investors, they should adhere to long-term investment strategies and study the long-term development trends of historical prices. Investors should closely monitor government policy adjustments and international relations between countries to adjust their investment plans on time. In addition, investors can consider an investment portfolio that includes different types of energy to reduce the risk of natural gas price fluctuations on the investment.

There are still limitations to the experiment, even though the constructed model has extremely high accuracy in forecasting Henry Hub natural gas prices. There is inevitable subjectivity in the setting of some parameters due to the complexity of the experiment, such as the selection of multi-steps ahead and the selection of parameters for certain algorithms. To address this issue, more objective selection methods should be explored in future research.

Geopolitical risks are usually unforeseeable and have contingency. However, it cannot be denied that they have an unignored impact on natural gas price prediction, such as regional conflicts or policy changes in natural gas-producing countries that can lead to significant price fluctuations.

In addition, with the development of renewable energy technology and increased policy support, the competitiveness of renewable energy will affect the demand and price of natural gas. Although this paper considers some long-term factors affecting natural gas price changes, it cannot avoid the impact of policy factors and black swan events on prediction results. Thus, we did not consider some unexpected events such as geopolitical factors in this paper. Moreover, natural gas influence factors may change over time. Therefore, future research could try considering geopolitical factors and other influential factors with increasing importance to improve the applicability of models.

Data availability statement

The raw data supporting the conclusion of this article will be made available by the authors, without undue reservation.

Author contributions

YD: conceptualization and writing–review and editing. JZ: data curation, formal analysis, and writing–original draft. XW: methodology, supervision, and writing–review and editing.

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Conflict of interest

The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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Supplementary material

The Supplementary Material for this article can be found online at: <https://www.frontiersin.org/articles/10.3389/fenrg.2023.1323073/full#supplementary-material>

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